

Package ‘CaDENCE’

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Type Package

Title Conditional Density Estimation Network Construction and Evaluation

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Description Parameters of a user-specified probability distribution are modelled by a multi-layer perceptron artificial neural network. This framework can be used to implement probabilistic nonlinear models including mixture density networks, heteroscedastic regression models, zero-inflated models, etc. following Cannon (2012) <doi:10.1016/j.cageo.2011.08.023>.

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CaDENCE-package	<i>Conditional Density Estimation Network Construction and Evaluation (CaDENCE)</i>
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Description

A conditional density estimation network (CDEN) is a probabilistic extension of the standard multi-layer perceptron neural network (MLP) (Neuneier et al., 1994). A CDEN model allows users to estimate parameters of a specified probability distribution conditioned upon values of a set of predictors using the MLP architecture. The result is a flexible nonlinear model that can be used to calculate the conditional mean, variance, prediction intervals, etc. based on the specified distribution. Because the CDEN is based on the MLP, nonlinear relationships, including those involving complicated interactions between predictors, can be described by the modelling framework. The CaDENCE (Conditional Density Estimation Network Creation & Evaluation) package provides routines for creating and evaluating CDEN models in the R programming language.

Details

Procedures for fitting CaDENCE models are provided by `cadence.fit`, which relies on the standard `optim` function, the CaDENCE `rprop` function, or, optionally, the `psoptim` function from the `pso` package. Once a model has been developed, `cadence.predict` is used to evaluate the distribution parameters as a function of predictors.

The package also provides a variety of zero-inflated distributions, including the Bernoulli-gamma (`bgamma`), Bernoulli-Weibull (`bweibull`), Bernoulli-Pareto 2 (`bpareto2`), and Bernoulli-lognormal (`blnorm`), for use in the CaDENCE models.

`gam.style`, `dummy.code`, `xval.buffer`, and `rbf` are helper functions that may be useful for data preprocessing, model evaluation, and interpretation of fitted relationships.

Most other functions are used internally and should not normally need to be called directly by the user.

References

- Cannon, A.J., 2012. Neural networks for probabilistic environmental prediction: Conditional Density Estimation Network Creation & Evaluation (CaDENCE) in R. *Computers & Geosciences* 41: 126-135. doi:10.1016/j.cageo.2011.08.023
- Neuneier, R., F. Hergert, W. Finnoff, and D. Ormoneit, 1994., Estimation of conditional densities: a comparison of neural network approaches. In: M. Marinaro and P. Morasso (eds.), *Proceedings of ICANN 94*, Berlin, Springer, p. 689-692.

bgamma	<i>Bernoulli-gamma distribution</i>
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Description

Functions implementing the Bernoulli-gamma distribution, in which zero values occur with probability $1 - \text{prob}$ and non-zero values follow a gamma distribution with scale and shape parameters. `dbgamma` gives a probability density function (pdf), `pbgamma` gives the cumulative distribution function (cdf), `qbgamma` gives the quantile function (inverse cdf), and `rbgamma` is used for generating random variates.

Usage

```
dbgamma(x, prob, scale, shape)
pbgamma(q, prob, scale, shape)
qbgamma(p, prob, scale, shape)
rbgamma(n, prob, scale, shape)
```

Arguments

<code>x, q</code>	vector of quantiles.
<code>p</code>	vector of cumulative probabilities.
<code>n</code>	number of random samples.
<code>prob</code>	probability of a non-zero value.
<code>scale</code>	scale parameter of the gamma distribution.
<code>shape</code>	shape parameter of the gamma distribution.

Value

`dbgamma` gives the pdf, `pbgamma` gives the cdf, `qbgamma` gives the inverse cdf (or quantile function), and `rbgamma` generates random deviates.

References

Cannon, A.J., 2008. Probabilistic multi-site precipitation downscaling by an expanded Bernoulli-gamma density network. *Journal of Hydrometeorology*, 9(6): 1284-1300.

See Also

[dgamma](#), [bweibull](#), [bpareto2](#), [blnorm](#)

Examples

```
plot(rbgamma(365, prob = 0.2, scale = 1, shape = 1), type = "h")
```

blnorm *Bernoulli-lognormal distribution*

Description

Functions implementing the Bernoulli-lognormal distribution, in which zero values occur with probability $1 - \text{prob}$ and non-zero values follow a lognormal distribution with `meanlog` and `sdlog` parameters. `dblnorm` gives a probability density function (pdf), `pblnorm` gives the cumulative distribution function (cdf), `qblnorm` gives the quantile function (inverse cdf), and `rblnorm` is used for generating random variates.

Usage

```
dblnorm(x, prob, meanlog, sdlog)
pblnorm(q, prob, meanlog, sdlog)
qblnorm(p, prob, meanlog, sdlog)
rblnorm(n, prob, meanlog, sdlog)
```

Arguments

<code>x, q</code>	vector of quantiles.
<code>p</code>	vector of cumulative probabilities.
<code>n</code>	number of random samples.
<code>prob</code>	probability of a non-zero value.
<code>meanlog</code>	meanlog parameter of the lognormal distribution.
<code>sdlog</code>	sdlog parameter of the lognormal distribution.

Value

`dblnorm` gives the pdf, `pblnorm` gives the cdf, `qblnorm` gives the inverse cdf (or quantile function), and `rblnorm` generates random variates.

See Also

[dlnorm](#), [bweibull](#), [bpareto2](#), [bgamma](#)

Examples

```
plot(rblnorm(365, prob = 0.2, meanlog = 1, sdlog = 1), type = "h")
```

`bweibull`*Bernoulli-Weibull distribution*

Description

Functions implementing the Bernoulli-Weibull distribution, in which zero values occur with probability $1 - \text{prob}$ and non-zero values follow a Weibull distribution with scale and shape parameters. `dbweibull` gives a probability density function (pdf), `pbweibull` gives the cumulative distribution function (cdf), `qbweibull` gives the quantile function (inverse cdf), and `rbweibull` is used for generating random variates.

Usage

```
dbweibull(x, prob, scale, shape)
pbweibull(q, prob, scale, shape)
qbweibull(p, prob, scale, shape)
rbweibull(n, prob, scale, shape)
```

Arguments

<code>x, q</code>	vector of quantiles.
<code>p</code>	vector of cumulative probabilities.
<code>n</code>	number of random samples.
<code>prob</code>	probability of a non-zero value.
<code>scale</code>	scale parameter of the weibull distribution.
<code>shape</code>	shape parameter of the weibull distribution.

Value

`dbweibull` gives the pdf, `pbweibull` gives the cdf, `qbweibull` gives the inverse cdf (or quantile function), and `rbweibull` generates random variates.

See Also

[dweibull](#), [bgamma](#), [bpareto2](#), [blnorm](#)

Examples

```
plot(rbweibull(365, prob = 0.2, scale = 1, shape = 1), type = "h")
```

cadence.cost	<i>Cost function for CDEN model fitting</i>
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Description

The maximum likelihood cost function used for CDEN model fitting. Calculates the negative of the logarithm of the likelihood. A normal distribution prior can be set for the magnitude of the input-hidden layer weights, thus leading to weight penalty regularization.

Usage

```
cadence.cost(weights, x, y, n.hidden, hidden.fcn, distribution, sd.norm,
             valid)
```

Arguments

weights	weight vector of length returned by cadence.initialize .
x	matrix with number of rows equal to the number of samples and number of columns equal to the number of predictor variables.
y	column matrix of predictand values with number of rows equal to the number of samples.
n.hidden	number of hidden nodes in the CDEN model.
hidden.fcn	hidden layer transfer function.
distribution	a list that describes the probability density function associated with the predictand.
sd.norm	sd parameter for normal distribution prior for the magnitude of input-hidden layer weights; equivalent to weight penalty regularization.
valid	valid logical vector indicating which weights are non-zero or fixed at zero, i.e., due to use of parameters.fixed in distribution.

See Also

[cadence.fit](#), [optim](#), [rprop](#)

cadence.fit	<i>Fit a CDEN model</i>
-------------	-------------------------

Description

Fit a CDEN model via nonlinear optimization of the maximum likelihood cost function.

Usage

```
cadence.fit(x, y, iter.max = 500, n.hidden = 2, hidden.fcn = tanh,
           distribution = NULL, sd.norm = Inf, init.range = c(-0.5, 0.5),
           method = c("optim", "psoptim", "Rprop"), n.trials = 1,
           trace = 0, maxit.Nelder = 2000, trace.Nelder = 0,
           swarm.size = NULL, vectorize = TRUE,
           delta.0 = 0.1, delta.min = 1e-06, delta.max = 50, epsilon = 1e-08,
           range.mult = 2, step.tol = 1e-08, f.target = -Inf,
           f.cost = cadence.cost, max.exceptions = 500)
```

Arguments

x	matrix with number of rows equal to the number of samples and number of columns equal to the number of predictor variables.
y	column matrix of predictand values with number of rows equal to the number of samples.
iter.max	maximum number of iterations of the optimization function.
n.hidden	number of hidden nodes in the CDEN model; can be a vector indicating a range of values to fit.
hidden.fcn	hidden layer transfer function.
distribution	a list that describes the probability density function associated with the predictand.
sd.norm	sd parameter for normal distribution prior for the magnitude of input-hidden layer weights; equivalent to weight penalty regularization.
init.range	range for random weights on $[\min(\text{init.range}), \max(\text{init.range})]$
method	specifies the optimization method used to minimize <code>cadence.cost</code> ; must be chosen from <code>c("optim", "psoptim", "Rprop")</code> .
n.trials	number of repeated trials used to avoid shallow local minima during optimization.
trace	the level of printing which is done during optimization. A value of 0 suppresses any progress reporting.
maxit.Nelder	maximum number of iterations of the Nelder-Mead optimization function prior to main calling method.
trace.Nelder	the level of printing which is done during Nelder-Mead optimization. A value of 0 suppresses any progress reporting.
swarm.size	swarm.size if <code>psoptim</code> is used for optimization.
vectorize	vectorize if <code>psoptim</code> is used for optimization.
delta.0	size of the initial update-value if <code>rprop</code> is used for optimization.
delta.min	minimum value for the adaptive update-value if <code>rprop</code> is used for optimization.
delta.max	maximum value for the adaptive update-value if <code>rprop</code> is used for optimization.
epsilon	step-size used in the finite difference calculation of the gradient if <code>rprop</code> is used for optimization.

<code>range.mult</code>	if <code>psoptim</code> is used for optimization, sets the search space boundaries to <code>range.mult</code> times the range of weights found by the Nelder-Mead algorithm.
<code>step.tol</code>	convergence criterion if <code>rprop</code> is used for optimization. Optimization will stop if the change in <code>f</code> over the previous three iterations falls below this value.
<code>f.target</code>	target value of <code>f</code> if <code>rprop</code> is used for optimization. Optimization will stop if <code>f</code> falls below this value.
<code>f.cost</code>	cost function to be optimized.
<code>max.exceptions</code>	maximum number of repeated exceptions allowed during optimization.

Details

Fit a CDEN model by optimizing the maximum likelihood cost function `f.cost`, which is set by default to `cadence.cost`. Optimization relies on the standard `optim` function, the built-in `rprop` function, or, optionally, the `psoptim` function from the `pso` package.

The hidden layer transfer function `hidden.fcn` should be set to `tanh` for a nonlinear model and to `identity` for a linear model. In the nonlinear case, the number of hidden nodes `n.hidden` controls the overall complexity of the model. The predictand distribution is set by the `distribution` argument. Parameters of the specified distribution can be held constant via the `parameters.fixed` element `distribution`. Weight penalty regularization for the magnitude of the input-hidden layer weights can be applied by setting `sd.norm` to a value less than `Inf`.

The `distribution` argument in `cadence.fit` is the most important part of the CaDENCE modelling framework and has been designed to be as flexible as possible. To this end, `distribution` is a list with three mandatory elements: `density.fcn`, which specifies the R density function for the predictand distribution; `parameters`, which specifies the names of the parameters used as arguments in `density.fcn`; and `output.fcns`, which specifies the functions used to constrain the density function parameters to their allowable ranges (i.e., inverse link functions). If not specified, `distribution` defaults to a normal distribution. Note: the order of `parameters` and `output.fcns` must match the order of arguments in the specified `density.fcn`.

A fourth element of `distribution`, `parameters.fixed`, is optional. Setting `parameters.fixed="sd"` for the normal distribution would, for example, force the `sd` parameter to take a constant value.

Samples of distribution lists for a variety of probability distributions are given below for reference:

```
# normal distribution
norm.distribution <- list(density.fcn = dnorm,
                        parameters = c("mean", "sd"),
                        parameters.fixed = NULL,
                        output.fcns = c(identity, exp))

# lognormal distribution
lnorm.distribution <- list(density.fcn = dlnorm,
                        parameters = c("meanlog", "sdlog"),
                        parameters.fixed = NULL,
                        output.fcns = c(identity, exp))

# exponential distribution
```



```

# mixture of two normal distributions (mixture density network)
library(nor1mix)
dnormix <- function(x, mu1, mu2, sig1, sig2, w1){
  if(length(x) > 1){
    dens <- mapply(dnormix, x, mu1 = mu1, mu2 = mu2,
                  sig1 = sig1, sig2 = sig2, w1 = w1)
  } else{
    mix <- norMix(mu = c(mu1, mu2), sigma = c(sig1, sig2),
                w = c(w1, 1-w1))
    dens <- dnorMix(x, mix)
  }
  dens
}
normix.distribution <- list(density.fcn = dnormix,
                          parameters = c("mu1", "mu2", "sig1",
                                          "sig2", "w1"),
                          parameters.fixed = NULL,
                          output.fcns = c(identity, identity,
                                          exp, exp, logistic))

```

Values of the Akaike information criterion with small sample size correction (AICc), and Bayesian information criterion (BIC) are calculated to assist in model selection. It is possible for such criteria to fail in the face of overfitting, for example with a nonlinear model and `n.hidden` set too high, as the distribution may converge on one or more samples. This can usually be diagnosed by inspecting the scale parameter of the distribution for near zero values. In this case, one can apply a weight penalty (via `sd.norm`), although this rules out the straightforward use of AICc/BIC for model selection as the effective number of model parameters will no longer equal the number of weights in the CDEN model.

Note: values of `x` need not be standardized or rescaled by the user. Predictors are automatically scaled to zero mean and unit standard deviation and are rescaled by [cadence.predict](#).

Value

a list of with number of elements equal to the length of `n.hidden`; each list consists of:

W1	input-hidden layer weights
W2	hidden-output layer weights. Attributes indicating the mean and standard deviation of columns of <code>x</code> ; the value of <code>hidden.fcn</code> ; the value of <code>hidden.fcn</code> ; the negative log-likelihood NLL; the number of model parameters <code>k</code> ; the value of the weight penalty <code>penalty</code> (if <code>sd.norm</code> is less than infinity); the value of the BIC, AIC, and AICc cost-complexity criteria; and the predictand distribution list are also returned.

References

Cannon, A.J., 2012. Neural networks for probabilistic environmental prediction: Conditional Density Estimation Network Creation & Evaluation (CaDENCE) in R. *Computers & Geosciences* 41: 126-135. doi:10.1016/j.cageo.2011.08.023

Neuneier, R., F. Hergert, W. Finnoff, and D. Ormoneit, 1994., Estimation of conditional densities: a comparison of neural network approaches. In: M. Marinaro and P. Morasso (eds.), Proceedings of ICANN 94, Berlin, Springer, p. 689-692.

See Also

[cadence.predict](#), [optim](#), [rprop](#), [xval.buffer](#), [logistic](#)

Examples

```
data(FraserSediment)
set.seed(1)
lnorm.distribution <- list(density.fcn = dlnorm,
                          parameters = c("meanlog", "sdlog"),
                          parameters.fixed = NULL,
                          output.fcns = c(identity, exp))
fit <- cadence.fit(x = FraserSediment$x.1970.1976[c(TRUE, rep(FALSE, 19))],,
                  y = FraserSediment$y.1970.1976[c(TRUE, rep(FALSE, 19))],,
                  drop=FALSE], n.hidden = 3, n.trials = 1,
                  maxit.Nelder = 100, trace.Nelder = 1, hidden.fcn = tanh,
                  distribution = lnorm.distribution, trace = 1)
pred <- cadence.predict(x = FraserSediment$x.1977.1979, fit = fit)
matplot(pred, type = "l")
```

`cadence.initialize` *Initialize a CDEN weight vector*

Description

Random initialization of the weight vector used during fitting of the CDEN model.

Usage

```
cadence.initialize(x, n.hidden, init.range, distribution)
```

Arguments

<code>x</code>	matrix with number of rows equal to the number of samples and number of columns equal to the number of predictors.
<code>n.hidden</code>	number of hidden nodes in the CDEN model.
<code>init.range</code>	range for random weights on $[\min(\text{init.range}), \max(\text{init.range})]$
<code>distribution</code>	list used to specify the predictand distribution

cadence.predict	<i>Predict conditional distribution parameters from a fitted CDEN model</i>
-----------------	---

Description

Predict conditional distribution parameters from a fitted CDEN model. The returned value is a matrix with columns corresponding to the parameters of the probability distribution specified in the distribution argument passed to [cadence.fit](#).

Usage

```
cadence.predict(x, fit)
```

Arguments

x	matrix with number of rows equal to the number of samples and number of columns equal to the number of predictor variables.
fit	list returned by cadence.fit .

Value

a matrix with number of rows equal to that of x and columns corresponding to the parameters of the distribution argument passed to [cadence.fit](#).

See Also

[cadence.fit](#), [optim](#), [rprop](#)

Examples

```
data(FraserSediment)
lnorm.distribution.fixed <- list(density.fcn = dlnorm,
                               parameters = c("meanlog", "sdlog"),
                               parameters.fixed = "sdlog",
                               output.fcns = c(identity, exp))
fit <- cadence.fit(x = FraserSediment$x.1970.1976,
                  y = FraserSediment$y.1970.1976,
                  hidden.fcn = identity, maxit.Nelder = 100,
                  trace.Nelder = 1, trace = 1,
                  distribution = lnorm.distribution.fixed)
pred <- cadence.predict(x = FraserSediment$x.1977.1979, fit = fit)
matplot(pred, type = "l")
```

 dummy.code

Convert a factor to a matrix of dummy codes

Description

Converts a factor (categorical) variable to a matrix of dummy codes using a 1 of C-1 binary coding scheme.

Usage

```
dummy.code(x)
```

Arguments

x a factor variable.

Value

a matrix with the number of rows equal to the number of cases in x and the number of columns equal to one minus the number of factors in x. The last factor serves as the reference group.

Examples

```
print(dummy.code(iris$Species))
```

 FraserSediment

Sediment and stream discharge data for Fraser River at Hope

Description

A dataset consisting of daily observations of suspended sediment concentration (SSC) (mg/L) and stream discharge (Q) (cu. m/s) for the years 1970-1979 at the Fraser River at Hope station in British Columbia, Canada (Water Survey of Canada station 08MF005). Samples are split into a seven year training period (1970-1976) and a three year testing period (1977-1979).

In terms of structure, FraserSediment is a list with four elements: x.1970.1976, y.1970.1976, x.1977.1979, and y.1977.1979. x.1970.1976 and x.1977.1979 are matrices with predictor variables: logQ, log-transformed Q; and dQ5, dQ30, and dQ90, 5-, 30-, and 90-day moving averages of daily changes in Q. y.1970.1976 and y.1977.1979 are matrices with the predictand variable SSC.

Examples

```
data(FraserSediment)
pairs(cbind(FraserSediment$x.1970.1976, FraserSediment$y.1970.1976))
```

gam.style

*GAM-style effects plots for interpreting CDEN models***Description**

GAM-style effects plots provide a graphical means of interpreting relationships between predictors and conditional pdf parameter values predicted by a CDEN. From Plate et al. (2000): The effect of the i th input variable at a particular input point $\Delta_{i,x}$ is the change in f resulting from changing X_1 to x_1 from b_1 (the baseline value [...]) while keeping the other inputs constant. The effects are plotted as short line segments, centered at $(x_i, \Delta_{i,x})$, where the slope of the segment is given by the partial derivative. Variables that strongly influence the function value have a large total vertical range of effects. Functions without interactions appear as possibly broken straight lines (linear functions) or curves (nonlinear functions). Interactions show up as vertical spread at a particular horizontal location, that is, a vertical scattering of segments. Interactions are present when the effect of a variable depends on the values of other variables.

Usage

```
gam.style(x, fit, column, baseline = mean(x[,column]),
         additive.scale = FALSE, epsilon = 1e-5,
         seg.len = 0.02, seg.cols = "black", plot = TRUE,
         return.results = FALSE, ...)
```

Arguments

<code>x</code>	matrix with number of rows equal to the number of samples and number of columns equal to the number of predictor variables.
<code>fit</code>	element from list returned by <code>cadence.fit</code> .
<code>column</code>	column of <code>x</code> for which effects plots should be returned.
<code>baseline</code>	value of <code>x[, column]</code> to be used as the baseline for calculation of predictor effects; defaults to <code>mean(x[, column])</code> .
<code>additive.scale</code>	if TRUE then predictor effects and partial derivatives are calculated before the inverse link functions for the distribution parameters are applied; if FALSE (the default) then values are calculated after the inverse link functions are applied.
<code>epsilon</code>	step-size used in the finite difference calculation of the partial derivatives.
<code>seg.len</code>	length of effects line segments expressed as a fraction of the range of <code>x[, column]</code> .
<code>seg.cols</code>	colors of effects line segments.
<code>plot</code>	if TRUE (the default) then an effects plots for each distribution parameter is produced.
<code>return.results</code>	if TRUE then values of effects and partial derivatives for each distribution parameter are returned.
<code>...</code>	further arguments to be passed to <code>plot</code> .

Value

A list with elements:

effects a matrix of predictor effects.
 partials a matrix of predictor partial derivatives.

References

Cannon, A.J. and I.G. McKendry, 2002. A graphical sensitivity analysis for interpreting statistical climate models: Application to Indian monsoon rainfall prediction by artificial neural networks and multiple linear regression models. *International Journal of Climatology*, 22:1687-1708.

Plate, T., J. Bert, J. Grace, and P. Band, 2000. Visualizing the function computed by a feedforward neural network. *Neural Computation*, 12(6): 1337-1354.

See Also

[cadence.fit](#), [cadence.predict](#)

Examples

```
data(FraserSediment)
set.seed(1)
lnorm.distribution <- list(density.fcn = dlnorm,
                          parameters = c("meanlog", "sdlog"),
                          parameters.fixed = NULL,
                          output.fcns = c(identity, exp))
x <- FraserSediment$x.1970.1976[c(TRUE, rep(FALSE, 24)),]
y <- FraserSediment$y.1970.1976[c(TRUE, rep(FALSE, 24)),,drop=FALSE]
fit.nlin <- cadence.fit(x, y, n.hidden = 2, n.trials = 1,
                      hidden.fcn = tanh, distribution =
                        lnorm.distribution, maxit.Nelder = 100,
                        trace.Nelder = 1, trace = 1)
fit.lin <- cadence.fit(x, y, hidden.fcn = identity, n.trials = 1,
                    distribution = lnorm.distribution,
                    maxit.Nelder = 100, trace.Nelder = 1,
                    trace = 1)
gam.style(x, fit = fit.nlin[[1]], column = 1,
          main = "Nonlinear")
gam.style(x, fit = fit.lin[[1]], column = 1,
          additive.scale = TRUE,
          main = "Linear (additive.scale = TRUE)")
```

logistic

Logistic sigmoid function

Description

logistic computes a logistic sigmoid (S-shaped) function bounded between 0 and 1.

Usage

```
logistic(x)
```

Arguments

x a numeric vector

pareto2

Pareto 2 (Lomax) and Bernoulli-Pareto 2 distributions

Description

Functions implementing the Pareto 2 (Lomax) and Bernoulli-Pareto 2 distributions. In the latter case, zero values occur with probability $1 - \text{prob}$ and non-zero values follow the Pareto 2 distribution with scale and shape parameters. `dpareto2` and `dbpareto2` give the probability density functions (pdf); `ppareto2` and `pbpareto2` give the cumulative distribution functions (cdf); `qpareto2` and `qbpareto2` give the quantile functions (inverse cdfs), and `rpareto2` and `rbpareto2` are used for generating random variates.

Usage

```
dpareto2(x, scale, shape)
ppareto2(q, scale, shape)
qpareto2(p, scale, shape)
rpareto2(n, scale, shape)
dbpareto2(x, prob, scale, shape)
pbpareto2(q, prob, scale, shape)
qbpareto2(p, prob, scale, shape)
rbpareto2(n, prob, scale, shape)
```

Arguments

x, q vector of quantiles.
 p vector of cumulative probabilities.
 n number of random samples.
 prob probability of a non-zero value.
 scale scale parameter of the pareto2 distribution.
 shape shape parameter of the pareto2 distribution.

Value

`dpareto2` and `dbpareto2` gives the pdfs; `ppareto2` and `pbpareto2` gives the cdfs; `qpareto2` and `qbpareto2` gives the inverse cdfs (or quantile functions); and `rpareto2` and `rbpareto2` generate random variates.

References

- Arnold, B.C., 1983. The Pareto Distributions, International Co-operative Publishing House, Fairland, MD.
- Lomax, K.S., 1954. Business failures: another example of the analysis of failure data. Journal of the American Statistical Association, 49(268): 847-852.

See Also

[bgamma](#), [bweibull](#), [blnorm](#)

Examples

```
plot(rbpareto2(365, prob = 0.2, scale = 1, shape = 1), type = "h")
```

rbf	<i>Radial basis function kernel</i>
-----	-------------------------------------

Description

Evaluate a kernel matrix based on the radial basis function kernel. Can be used in conjunction with [cadence.fit](#) with `hidden.fcn` set to [identity](#) and `sd.norm` set to a value less than infinity to implement a kernel CDEN model.

Usage

```
rbf(x, x.basis, sigma)
```

Arguments

x	matrix with number of rows equal to the number of samples and number of columns equal to the number of predictors.
x.basis	matrix with number of rows equal to the number of basis functions and number of columns equal to the number of predictors.
sigma	kernel width

Value

kernel matrix with number of rows equal to the number of samples and number of columns equal to the number of basis functions.

See Also

[cadence.fit](#)

rprop

Resilient backpropagation (Rprop) optimization algorithm

Description

From Riedmiller (1994): Rprop stands for 'Resilient backpropagation' and is a local adaptive learning scheme. The basic principle of Rprop is to eliminate the harmful influence of the size of the partial derivative on the weight step. As a consequence, only the sign of the derivative is considered to indicate the direction of the weight update. The size of the weight change is exclusively determined by a weight-specific, so called 'update-value'.

This function implements the iRprop+ algorithm from Igel and Huesken (2003).

Usage

```
rprop(w, f, iterlim = 100, print.level = 1, delta.0 = 0.1,
      delta.min = 1e-06, delta.max = 50, epsilon = 1e-08,
      step.tol = 1e-06, f.target = -Inf, ...)
```

Arguments

w	the starting parameters for the minimization.
f	the function to be minimized. If the function value has an attribute called <code>gradient</code> , this will be used in the calculation of updated parameter values. Otherwise, numerical derivatives will be used.
iterlim	the maximum number of iterations before the optimization is stopped.
print.level	the level of printing which is done during optimization. A value of 0 suppresses any progress reporting, whereas positive values report the value of <code>f</code> and the mean change in <code>f</code> over the previous three iterations.
delta.0	size of the initial Rprop update-value.
delta.min	minimum value for the adaptive Rprop update-value.
delta.max	maximum value for the adaptive Rprop update-value.
epsilon	step-size used in the finite difference calculation of the gradient.
step.tol	convergence criterion. Optimization will stop if the change in <code>f</code> over the previous three iterations falls below this value.
f.target	target value of <code>f</code> . Optimization will stop if <code>f</code> falls below this value.
...	further arguments to be passed to <code>f</code> .

Value

A list with elements:

par	The best set of parameters found.
value	The value of <code>f</code> corresponding to <code>par</code> .
gradient	An estimate of the gradient at the solution found.

References

- Igel, C. and M. Huesken, 2003. Empirical evaluation of the improved Rprop learning algorithms. *Neurocomputing* 50: 105-123.
- Riedmiller, M., 1994. Advanced supervised learning in multilayer perceptrons - from backpropagation to adaptive learning techniques. *Computer Standards and Interfaces* 16(3): 265-278.

xval.buffer	<i>Cross-validation indices with a buffer between training/validation datasets</i>
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Description

Calculates training/validation indices for N-fold cross-validation of a dataset. Cross-validation folds are taken as contiguous blocks of cases with an optional buffer to prevent leakage of information between training/validation subsets due to the presence of autocorrelation.

Usage

```
xval.buffer(n.cases, n.xval=5, buffer.length=0)
```

Arguments

n.cases	an integer specifying the length of the dataset.
n.xval	an integer specifying the desired number of cross-validation folds.
buffer.length	an integer specifying the number of cases to be left out as a buffer between the training/validation subsets.

Value

a list with n.xval elements, each containing:

train	indices of training cases
valid	indices of validation cases

References

- Shabbar, A. and V. Kharin. 2007. An assessment of cross-validation for estimating skill of empirical seasonal forecasts using a global coupled model simulation. *CLIVAR Exchanges*. 12(4): 10-12.
- Zeng, Z., W.W. Hsieh, A. Shabbar, and W.W. Burrows, 2011. Seasonal prediction of winter extreme precipitation over Canada by support vector regression, *Hydrology and Earth System Sciences*, 15: 65-74.

Examples

```
print(xval.buffer(100, n.xval = 3, buffer.length = 10))
```

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