

Package ‘LindleyPowerSeries’

July 10, 2021

Type Package

Title Lindley Power Series Distribution

Version 1.0.1

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Description Computes the probability density function, the cumulative distribution function, the hazard rate function, the quantile function and random generation for Lindley Power Series distributions, see Nadarajah and Si (2018) <[doi:10.1007/s13171-018-0150-x](https://doi.org/10.1007/s13171-018-0150-x)>.

License GPL (>= 2)

Encoding UTF-8

RoxygenNote 7.1.1

Imports stats, lamW(>= 1.3.0)

NeedsCompilation no

Repository CRAN

Date/Publication 2021-07-10 16:50:02 UTC

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plindleybinomial *LindleyBinomial*

Description

distribution function, density function, hazard rate function, quantile function, random number generation

Usage

plindleybinomial(x, lambda, theta, m, log.p = FALSE)

dlindleybinomial(x, lambda, theta, m)

hlindleybinomial(x, lambda, theta, m)

qlindleybinomial(p, lambda, theta, m)

rlindleybinomial(n, lambda, theta, m)

Arguments

x	vector of positive quantiles.
lambda	positive parameter
theta	positive parameter.
m	number of trails.
log.p	logical; If TRUE, probabilities p are given as $\log(p)$.
p	vector of probabilities.
n	number of observations.

Details

Probability density function

$$f(x) = \frac{\theta \lambda^2}{(\lambda + 1)A(\theta)} (1 + x) \exp(-\lambda x) A'(\phi)$$

Cumulative distribution function

$$F(x) = \frac{A(\phi)}{A(\theta)}$$

Quantile function

$$F^{-1}(p) = -1 - \frac{1}{\lambda} - \frac{1}{\lambda} W_{-1} \left\{ \frac{\lambda + 1}{\exp(\lambda + 1)} \left[\frac{1}{\theta} A^{-1}\{pA(\theta)\} - 1 \right] \right\}$$

Hazard rate function

$$h(x) = \frac{\theta\lambda^2}{1+\lambda}(1+x)\exp(-\lambda x)\frac{A'(\phi)}{A(\theta) - A(\phi)}$$

where W_{-1} denotes the negative branch of the Lambert W function. $A(\theta) = \sum_{n=1}^{\infty} a_n\theta^n$ is given by specific power series distribution. Note that $x > 0, \lambda > 0$ for all members in Lindley Power Series distribution. $0 < \theta < 1$ for Lindley-Geometric distribution, Lindley-logarithmic distribution, Lindley-Negative Binomial distribution. $\theta > 0$ for Lindley-Poisson distribution, Lindley-Binomial distribution.

Value

plindleybinomial gives the culmulative distribution function

dlindleybinomial gives the probability density function

hlindleybinomial gives the hazard rate function

qlindleybinomial gives the quantile function

rlindleybinomial gives the random number generated by distribution

Invalid arguments will return an error message.

Author(s)

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References

- Si, Y. & Nadarajah, S., (2018). Lindley Power Series Distributions. *Sankhya A*, **9**, pp1-15.
- Ghitany, M. E., Atieh, B., Nadarajah, S., (2008). Lindley distribution and its application. *Mathematics and Computers in Simulation*, **78**, (4), 49-506.
- Jodra, P., (2010). Computer generation of random variables with Lindley or Poisson-Lindley distribution via the Lambert W function. *Mathematics and Computers in Simulation*, **81**, (4), 851-859.
- Lindley, D. V., (1958). Fiducial distributions and Bayes' theorem. *Journal of the Royal Statistical Society. Series B. Methodological*, **20**, 102-107.
- Lindley, D. V., (1965). *Introduction to Probability and Statistics from a Bayesian View-point, Part II: Inference*. Cambridge University Press, New York.

Examples

```
set.seed(1)
lambda = 1
theta = 0.5
n = 10
m = 10
x <- seq(from = 0.1, to = 6, by = 0.5)
p <- seq(from = 0.1, to = 1, by = 0.1)
plindleybinomial(x, lambda, theta, m, log.p = FALSE)
dlindleybinomial(x, lambda, theta, m)
```

```

hlindleybinomial(x, lambda, theta, m)
qlindleybinomial(p, lambda, theta, m)
rlindleybinomial(n, lambda, theta, m)

```

plindleygeometric *LindleyGeometric*

Description

distribution function, density function, hazard rate function, quantile function, random number generation

Usage

```

plindleygeometric(x, lambda, theta, log.p = FALSE)

dlindleygeometric(x, lambda, theta)

hlindleygeometric(x, lambda, theta)

qlindleygeometric(p, lambda, theta)

rlindleygeometric(n, lambda, theta)

```

Arguments

x	vector of positive quantiles.
lambda	positive parameter
theta	positive parameter.
log.p	logical; If TRUE, probabilities p are given as $\log(p)$.
p	vector of probabilities.
n	number of observations.

Details

Probability density function

$$f(x) = \frac{\theta\lambda^2}{(\lambda+1)A(\theta)}(1+x)\exp(-\lambda x)A'(\phi)$$

Cumulative distribution function

$$F(x) = \frac{A(\phi)}{A(\theta)}$$

Quantile function

$$F^{-1}(p) = -1 - \frac{1}{\lambda} - \frac{1}{\lambda} W_{-1} \left\{ \frac{\lambda+1}{\exp(\lambda+1)} \left[\frac{1}{\theta} A^{-1}\{pA(\theta)\} - 1 \right] \right\}$$

Hazard rate function

$$h(x) = \frac{\theta\lambda^2}{1+\lambda}(1+x)\exp(-\lambda x)\frac{A'(\phi)}{A(\theta) - A(\phi)}$$

where W_{-1} denotes the negative branch of the Lambert W function. $A(\theta) = \sum_{n=1}^{\infty} a_n\theta^n$ is given by specific power series distribution. Note that $x > 0, \lambda > 0$ for all members in Lindley Power Series distribution. $0 < \theta < 1$ for Lindley-Geometric distribution, Lindley-logarithmic distribution, Lindley-Negative Binomial distribution. $\theta > 0$ for Lindley-Poisson distribution, Lindley-Binomial distribution.

Value

plindleygeometric gives the culmulative distribution function

dlindleygeometric gives the probability density function

hlindleygeometric gives the hazard rate function

qlindleygeometric gives the quantile function

rlindleygeometric gives the random number generatedy by distribution

Invalid arguments will return an error message.

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References

- Si, Y. & Nadarajah, S., (2018). Lindley Power Series Distributions. *Sankhya A*, **9**, pp1-15.
- Ghitany, M. E., Atieh, B., Nadarajah, S., (2008). Lindley distribution and its application. *Mathematics and Computers in Simulation*, **78**, (4), 49-506.
- Jodra, P., (2010). Computer generation of random variables with Lindley or Poisson-Lindley distribution via the Lambert W function. *Mathematics and Computers in Simulation*, **81**, (4), 851-859.
- Lindley, D. V., (1958). Fiducial distributions and Bayes' theorem. *Journal of the Royal Statistical Society. Series B. Methodological*, **20**, 102-107.
- Lindley, D. V., (1965). *Introduction to Probability and Statistics from a Bayesian View-point, Part II: Inference*. Cambridge University Press, New York.

Examples

```
set.seed(1)
lambda = 1
theta = 0.5
n = 10
x <- seq(from = 0.1, to = 6, by = 0.5)
p <- seq(from = 0.1, to = 1, by = 0.1)
plindleygeometric(x, lambda, theta, log.p = FALSE)
dlindleygeometric(x, lambda, theta)
hlindleygeometric(x, lambda, theta)
```

```
qlindleygeometric(p, lambda, theta)
rlindleygeometric(n, lambda, theta)
```

```
plindleylogarithmic LindleyLogarithmic
```

Description

distribution function, density function, hazard rate function, quantile function, random number generation

Usage

```
plindleylogarithmic(x, lambda, theta, log.p = FALSE)

dlindleylogarithmic(x, lambda, theta)

hlindleylogarithmic(x, lambda, theta)

qlindleylogarithmic(p, lambda, theta)

rlindleylogarithmic(n, lambda, theta)
```

Arguments

x	vector of positive quantiles.
lambda	positive parameter
theta	positive parameter.
log.p	logical; If TRUE, probabilities p are given as $\log(p)$.
p	vector of probabilities.
n	number of observations.

Details

Probability density function

$$f(x) = \frac{\theta\lambda^2}{(\lambda+1)A(\theta)}(1+x)\exp(-\lambda x)A'(\phi)$$

Cumulative distribution function

$$F(x) = \frac{A(\phi)}{A(\theta)}$$

Quantile function

$$F^{-1}(p) = -1 - \frac{1}{\lambda} - \frac{1}{\lambda}W_{-1}\left\{\frac{\lambda+1}{\exp(\lambda+1)}\left[\frac{1}{\theta}A^{-1}\{pA(\theta)\}-1\right]\right\}$$

Hazard rate function

$$h(x) = \frac{\theta\lambda^2}{1+\lambda}(1+x)\exp(-\lambda x)\frac{A'(\phi)}{A(\theta) - A(\phi)}$$

where W_{-1} denotes the negative branch of the Lambert W function. $A(\theta) = \sum_{n=1}^{\infty} a_n\theta^n$ is given by specific power series distribution. Note that $x > 0, \lambda > 0$ for all members in Lindley Power Series distribution. $0 < \theta < 1$ for Lindley-Geometric distribution, Lindley-logarithmic distribution, Lindley-Negative Binomial distribution. $\theta > 0$ for Lindley-Poisson distribution, Lindley-Binomial distribution.

Value

plindleylogarithmic gives the cumulative distribution function

dlindleylogarithmic gives the probability density function

hlindleylogarithmic gives the hazard rate function

qlindleylogarithmic gives the quantile function

rlindleylogarithmic gives the random number generated by distribution

Invalid arguments will return an error message.

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References

- Si, Y. & Nadarajah, S., (2018). Lindley Power Series Distributions. *Sankhya A*, **9**, pp1-15.
- Ghitany, M. E., Atieh, B., Nadarajah, S., (2008). Lindley distribution and its application. *Mathematics and Computers in Simulation*, **78**, (4), 49-506.
- Jodra, P., (2010). Computer generation of random variables with Lindley or Poisson-Lindley distribution via the Lambert W function. *Mathematics and Computers in Simulation*, **81**, (4), 851-859.
- Lindley, D. V., (1958). Fiducial distributions and Bayes' theorem. *Journal of the Royal Statistical Society. Series B. Methodological*, **20**, 102-107.
- Lindley, D. V., (1965). *Introduction to Probability and Statistics from a Bayesian View-point, Part II: Inference*. Cambridge University Press, New York.

Examples

```
set.seed(1)
lambda = 1
theta = 0.5
n = 10
x <- seq(from = 0.1, to = 6, by = 0.5)
p <- seq(from = 0.1, to = 1, by = 0.1)
plindleylogarithmic(x, lambda, theta, log.p = FALSE)
dlindleylogarithmic(x, lambda, theta)
hlindleylogarithmic(x, lambda, theta)
```

```
qlindleylogarithmic(p, lambda, theta)
rlindleylogarithmic(n, lambda, theta)
```

```
plindleynb LindleyNegativeBinomial
```

Description

distribution function, density function, hazard rate function, quantile function, random number generation

Usage

```
plindleynb(x, lambda, theta, m, log.p = FALSE)

dlindleynb(x, lambda, theta, m)

qlindleynb(p, lambda, theta, m)

rlindleynb(n, lambda, theta, m)
```

Arguments

x	vector of positive quantiles.
lambda	positive parameter
theta	positive parameter.
m	target for number of successful trials. Must be strictly positive, need not be integer.
log.p	logical; If TRUE, probabilities p are given as $\log(p)$.
p	vector of probabilities.
n	number of observations.

Details

Probability density function

$$f(x) = \frac{\theta\lambda^2}{(\lambda+1)A(\theta)}(1+x)\exp(-\lambda x)A'(\phi)$$

Cumulative distribution function

$$F(x) = \frac{A(\phi)}{A(\theta)}$$

Quantile function

$$F^{-1}(p) = -1 - \frac{1}{\lambda} - \frac{1}{\lambda} W_{-1} \left\{ \frac{\lambda+1}{\exp(\lambda+1)} \left[\frac{1}{\theta} A^{-1}\{pA(\theta)\} - 1 \right] \right\}$$

Hazard rate function

$$h(x) = \frac{\theta\lambda^2}{1+\lambda}(1+x)\exp(-\lambda x)\frac{A'(\phi)}{A(\theta) - A(\phi)}$$

where W_{-1} denotes the negative branch of the Lambert W function. $A(\theta) = \sum_{n=1}^{\infty} a_n\theta^n$ is given by specific power series distribution. Note that $x > 0, \lambda > 0$ for all members in Lindley Power Series distribution. $0 < \theta < 1$ for Lindley-Geometric distribution, Lindley-logarithmic distribution, Lindley-Negative Binomial distribution. $\theta > 0$ for Lindley-Poisson distribution, Lindley-Binomial distribution.

Value

plindleynb gives the cumulative distribution function

dlindleynb gives the probability density function

hlindleynb gives the hazard rate function

qlindleynb gives the quantile function

rlindleynb gives the random number generated by distribution

Invalid arguments will return an error message.

Author(s)

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References

- Si, Y. & Nadarajah, S., (2018). Lindley Power Series Distributions. *Sankhya A*, **9**, pp1-15.
- Ghitany, M. E., Atieh, B., Nadarajah, S., (2008). Lindley distribution and its application. *Mathematics and Computers in Simulation*, **78**, (4), 49-506.
- Jodra, P., (2010). Computer generation of random variables with Lindley or Poisson-Lindley distribution via the Lambert W function. *Mathematics and Computers in Simulation*, **81**, (4), 851-859.
- Lindley, D. V., (1958). Fiducial distributions and Bayes' theorem. *Journal of the Royal Statistical Society. Series B. Methodological*, **20**, 102-107.
- Lindley, D. V., (1965). *Introduction to Probability and Statistics from a Bayesian View-point, Part II: Inference*. Cambridge University Press, New York.

Examples

```
set.seed(1)
lambda = 1
theta = 0.5
n = 10
m = 10
x <- seq(from = 0.1, to = 6, by = 0.5)
p <- seq(from = 0.1, to = 1, by = 0.1)
plindleynb(x, lambda, theta, m, log.p = FALSE)
dlindleynb(x, lambda, theta, m)
```

```

hlindleynb(x, lambda, theta, m)
qlindleynb(p, lambda, theta, m)
rlindleynb(n, lambda, theta, m)

```

```

plindleypoisson      LindleyPoisson

```

Description

distribution function, density function, hazard rate function, quantile function, random number generation

Usage

```

plindleypoisson(x, lambda, theta, log.p = FALSE)

dlindleypoisson(x, lambda, theta)

hlindleypoisson(x, lambda, theta)

qlindleypoisson(p, lambda, theta)

rlindleypoisson(n, lambda, theta)

```

Arguments

x	vector of positive quantiles.
lambda	positive parameter
theta	positive parameter.
log.p	logical; If TRUE, probabilities p are given as $\log(p)$.
p	vector of probabilities.
n	number of observations.

Details

Probability density function

$$f(x) = \frac{\theta \lambda^2}{(\lambda + 1)A(\theta)} (1 + x) \exp(-\lambda x) A'(\phi)$$

Cumulative distribution function

$$F(x) = \frac{A(\phi)}{A(\theta)}$$

Quantile function

$$F^{-1}(p) = -1 - \frac{1}{\lambda} - \frac{1}{\lambda} W_{-1} \left\{ \frac{\lambda + 1}{\exp(\lambda + 1)} \left[\frac{1}{\theta} A^{-1}\{pA(\theta)\} - 1 \right] \right\}$$

Hazard rate function

$$h(x) = \frac{\theta\lambda^2}{1+\lambda}(1+x)\exp(-\lambda x)\frac{A'(\phi)}{A(\theta) - A(\phi)}$$

where W_{-1} denotes the negative branch of the Lambert W function. $A(\theta) = \sum_{n=1}^{\infty} a_n\theta^n$ is given by specific power series distribution. Note that $x > 0, \lambda > 0$ for all members in Lindley Power Series distribution. $0 < \theta < 1$ for Lindley-Geometric distribution, Lindley-logarithmic distribution, Lindley-Negative Binomial distribution. $\theta > 0$ for Lindley-Poisson distribution, Lindley-Binomial distribution.

Value

plindleypoisson gives the culmulative distribution function

dlindleypoisson gives the probability density function

hlindleypoisson gives the hazard rate function

qlindleypoisson gives the quantile function

rlindleypoisson gives the random number generatedy by distribution

Invalid arguments will return an error message.

Author(s)

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References

- Si, Y. & Nadarajah, S., (2018). Lindley Power Series Distributions. *Sankhya A*, **9**, pp1-15.
- Ghitany, M. E., Atieh, B., Nadarajah, S., (2008). Lindley distribution and its application. *Mathematics and Computers in Simulation*, **78**, (4), 49-506.
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- Lindley, D. V., (1965). *Introduction to Probability and Statistics from a Bayesian View-point, Part II: Inference*. Cambridge University Press, New York.

Examples

```
set.seed(1)
lambda = 1
theta = 0.5
n = 10
x <- seq(from = 0.1, to = 6, by = 0.5)
p <- seq(from = 0.1, to = 1, by = 0.1)
plindleypoisson(x, lambda, theta, log.p = FALSE)
dlindleypoisson(x, lambda, theta)
hlindleypoisson(x, lambda, theta)
```

```
qlindleypoisson(p, lambda, theta)  
rlindleypoisson(n, lambda, theta)
```

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