

Package ‘dppmix’

January 14, 2020

Type Package

Title Determinantal Point Process Mixture Models

Version 0.1.1

Date 2019-12-20

Author Yanxun Xu [aut], Peter Mueller [aut], Donatello Telesca [aut], David J. H. Shih [aut, cre]

Maintainer David J. H. Shih <djh.shih@gmail.com>

Description Multivariate Gaussian mixture model with a determinant point process prior to promote the discovery of parsimonious components from observed data. See Xu, Mueller, Telesca (2016) <doi:10.1111/biom.12482>.

URL <https://bitbucket.org/djhshih/dppmix>

BugReports <https://bitbucket.org/djhshih/dppmix/issues>

Imports stats, mvtnorm

License GPL (>= 3)

RoxygenNote 7.0.2

NeedsCompilation no

Repository CRAN

Date/Publication 2020-01-14 10:00:07 UTC

R topics documented:

dgammapois	2
dppmix_mvnorm	2
estimate	4
rbern	5
rbvec	5
rdirichlet	6
rmvnorm_clusters	6

Index	7
--------------	----------

dgammapois	<i>Density function for Gamma-Poisson distribution.</i>
------------	---

Description

Data follow the Poisson distribution parameterized by a mean parameter that follows a gamma distribution.

Usage

```
dgammapois(x, a, b = 1, log = FALSE)
```

Arguments

x	vector of x values
a	shape parameter for gamma distribution on mean parameter
b	rate parameter for gamma distribution on mean parameter
log	whether to return the density in log scale

Value

density values

dppmix_mvnorm	<i>Fit a determinantal point process multivariate normal mixture model.</i>
---------------	---

Description

Discover clusters in multidimensional data using a multivariate normal mixture model with a determinantal point process prior.

Usage

```
dppmix_mvnorm(  
  X,  
  hparams = NULL,  
  store = NULL,  
  control = NULL,  
  fixed = NULL,  
  verbose = TRUE  
)
```

Arguments

<code>X</code>	<code>N x J</code> data matrix of <code>N</code> observations and <code>J</code> features
<code>hparams</code>	a list of hyperparameter values: <code>delta</code> , <code>a0</code> , <code>b0</code> , <code>theta</code> , <code>sigma_prop_mu</code>
<code>store</code>	a vector of character strings specifying additional vars of interest; a value of <code>NA</code> indicates that samples of all parameters in the model will be stored
<code>control</code>	a list of control parameters: <code>niter</code> , <code>burnin</code> , <code>thin</code>
<code>fixed</code>	a list of fixed parameter values
<code>verbose</code>	whether to emit verbose message

Details

A determinantal point process (DPP) prior is a repulsive prior. Compare to mixture models using independent priors, a DPP mixture model will often discover a parsimonious set of mixture components (clusters).

Model fitting is done by sampling parameters from the posterior distribution using a reversible jump Markov chain Monte Carlo sampling approach.

Given $X = [x_i]$, where each x_i is a D -dimensional real vector, we seek the posterior distribution the latent variable $z = [z_i]$, where each z_i is an integer representing cluster membership.

$$x_i | z_i \sim Normal(\mu_k, \Sigma_k)$$

$$z_i \sim Categorical(w)$$

$$w \sim Dirichlet([\delta \dots \delta])$$

$$\mu_k \sim DPP(C)$$

where C is the covariance function that evaluates the distances among the data points:

$$C(x_1, x_2) = \exp\left(-\sum_d \frac{(x_1 - x_2)^2}{\theta^2}\right)$$

We also define $\Sigma_k = E_k \Lambda_k E_k^T$, where E_k is an orthonormal matrix whose column represents eigenvectors. We further assume that $E_k = E$ is fixed across all cluster components so that E can be estimated as the eigenvectors of the covariance matrix of the data matrix X . Finally, we put a prior on the entries of the Λ_k diagonal matrix:

$$\lambda_{kd}^{-1} \sim Gamma(a_0, b_0)$$

Hence, the hyperparameters of the model include: `delta`, `a0`, `b0`, `theta`, as well as sampling hyperparameter `sigma_pro_mu`, which controls the spread of the Gaussian proposal distribution for the random-walk Metropolis-Hastings update of the μ parameter.

The parameters (and their dimensions) in the model include: K , z ($N \times 1$), w ($K \times 1$), λ ($K \times J$), μ ($K \times J$), Σ ($J \times J \times K$). If any parameter is fixed, then K must be fixed as well.

Value

a `dppmix_mcmc` object containing posterior samples of the parameters

References

Yanxun Xu, Peter Mueller, Donatello Telesca. Bayesian Inference for Latent Biologic Structure with Determinantal Point Processes. *Biometrics*. 2016;72(3):955-64.

Examples

```
set.seed(1)
ns <- c(3, 3)
means <- list(c(-6, -3), c(0, 4))
d <- rmvnorm_clusters(ns, means)

mcmc <- dppmix_mvnorm(d$X, verbose=FALSE)
res <- estimate(mcmc)
table(d$c1, res$z)
```

estimate

Estimate parameter.

Description

Estimate parameter from fitted model.

Usage

```
estimate(object, pars, ...)
```

Arguments

<code>object</code>	fitted model
<code>pars</code>	names of parameters to estimate
<code>...</code>	other parameters to pass

rbern	<i>Random generator for the Bernoulli distribution.</i>
-------	---

Description

Random generator for the Bernoulli distribution.

Usage

```
rbern(n, prob)
```

Arguments

n	number of samples to generate
prob	event probability

Value

an integer vector of 0 (non-event) and 1 (event)

rbvec	<i>Generate a random binary vector.</i>
-------	---

Description

Generate a random binary vector.

Usage

```
rbvec(n, prob, e.min = 0)
```

Arguments

n	size of binary vector
prob	event probability (not accounting for minimum event constraint)
e.min	minimum number of events

Value

an integer vector of 0 and 1

rdirichlet	<i>Random generator for the Dirichlet distribution.</i>
------------	---

Description

Random generator for the Dirichlet distribution.

Usage

```
rdirichlet(n, alpha)
```

Arguments

n	number of vectors to generate
alpha	vector of parameters of the Dirichlet distribution

Value

a matrix in which each row vector is Dirichlet distributed

rmvnorm_clusters	<i>Generate random multivariate clusters</i>
------------------	--

Description

Generate random multivariate clusters

Usage

```
rmvnorm_clusters(ns, means)
```

Arguments

ns	number of data points in each cluster
means	centers of each cluster

Value

list containing matrix X and labels cl

Examples

```
ns <- c(5, 8, 7)
means <- list(c(-6, 1), c(-1, -1), c(0, 4))
d <- rmvnorm_clusters(ns, means)
```

Index

`dgamma`, 2

`dppmix_mvnorm`, 2

`estimate`, 4

`rbern`, 5

`rbvec`, 5

`rdirichlet`, 6

`rmvnorm_clusters`, 6