

Package ‘fractional’

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Type Package

Title Vulgar Fractions in R

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Description The main function of this package allows numerical vector objects to be displayed with their values in vulgar fractional form. This is convenient if patterns can then be more easily detected. In some cases replacing the components of a numeric vector by a rational approximation can also be expected to remove some component of round-off error. The main functions form a re-implementation of the functions 'fractions' and 'rational' of the MASS package, but using a radically improved programming strategy.

License GPL (>= 2)

Suggests stats, MASS, knitr, rmarkdown, ggplot2, dplyr

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fractional	<i>Representation of a numeric vector in vulgar fractional form</i>
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Description

The object is flagged so that if it is coerced to character, or printed, the numerical quantities are represented by a rational approximation. In other respects the numerical object behaves as normally.

Usage

```
fractional(x, eps = 1e-06, maxConv = 20, sync = FALSE)
```

```
## S3 method for class 'fractional'
as.character(x, eps = attr(x, "eps"), maxConv = attr(x,
  "maxConv"), ...)
```

```
## S3 method for class 'charFrac'
print(x, ...)
```

```
## S3 method for class 'fractional'
print(x, ...)
```

Arguments

x	A numeric object
eps	An absolute error tolerance
maxConv	An upper limit on the number of convergents to use in the continued fractions.
sync	A logical value. Should the numerical value be changed to match the rational approximation, as closely as possible with floating point, (TRUE)? Or, should it be left and used in its original state (FALSE)?
...	Currently ignored.

Value

A numeric object of class "fractional".

Methods (by generic)

- `as.character`: S3 method for coercion to character, producing an object inheriting from class "charFrac"
- `print`: Print method for class "charFrac" objects, unquoted.
- `print`: Print method for "fractional" objects

See Also

[fractions](#) for a similar functionality.

Examples

```
(M <- solve(cbind(1, contr.helmert(5))))
(Mf <- fractional(M))    ## print method right justifies
(Mc <- as.character(Mf)) ## print method left justifies
(Mn <- numerical(Mc))
set.seed(123)
u <- matrix(runif(10), 2, 5)
(uf <- fractional(u))
(us <- fractional(u, sync = TRUE)) ## may look different!
unfractional(uf) - unfractional(us) ## rational approximation errors
```

Math.fractional	<i>Method for the group generic function for the elementary mathematical functions</i>
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Description

Allows graceful operations with mathematical functions.

Usage

```
## S3 method for class 'fractional'
Math(x, ...)
```

Arguments

x	A numerical object flagged as fractional
...	Passed on to further methods (but usually not required)

Value

A numeric object with the results of the computations, but NOT flagged as of class "fractional".

Examples

```
(M <- fractional(solve(cbind(1, contr.helmert(5))))
(M0 <- abs(M)*sign(M)) ## fractional flag lost
```

numerators

Extract the parts of a fractional object

Description

Generic function for extracting numerators with methods for "fractional" or "charFrac" objects

Generic function for extracting denominators with methods for "fractional" or "charFrac" objects

Usage

```
numerators(x)

## S3 method for class 'charFrac'
numerators(x)

## S3 method for class 'fractional'
numerators(x)

## Default S3 method:
numerators(x)

denominators(x)

## S3 method for class 'charFrac'
denominators(x)

## S3 method for class 'fractional'
denominators(x)

## Default S3 method:
denominators(x)
```

Arguments

x An object of class "fractional" or "charFrac"

Value

An integer vector of numerators

An integer vector of denominators

Methods (by class)

- charFrac: numerators method function for "charFrac" objects
- fractional: numerators method function for "fractional" objects

- default: Default numerators method for numeric objects
- charFrac: denominators method function for "charFrac" objects
- fractional: denominators method function for "fractional" objects
- default: Default denominators method for numeric objects

Examples

```
(pi_approx <- vfractional(base::pi, eps = 0, maxConv = 1:10))
numerators(pi_approx)
denominators(pi_approx)
```

numerical

Convert a fractional object to the equivalent numeric object

Description

Convert an object of class "fractional" or "charFrac" to a purely numeric object. This is effectively a method function for the .Primitive generic function as.numeric but written as a separate function for purely technical reasons.

Usage

```
numerical(vulgar)

## S3 method for class 'fractional'
numerical(vulgar)

## S3 method for class 'charFrac'
numerical(vulgar)

## Default S3 method:
numerical(vulgar)
```

Arguments

vulgar character string form of a class 'fractional' object.

Value

A numeric object as represented by its (usually fractional) display.

Methods (by class)

- fractional: Method for "fractional" objects
- charFrac: Method for "charFrac" objects
- default: Default method for numerical generic

Examples

```

suppressPackageStartupMessages(library(dplyr))
m <- 2*diag(5)
m[abs(row(m) - col(m)) == 1] <- -1
m ## How much roundoff error does inverting entail?
(mi <- solve(m) %>% fractional) ## patterned inverse
mi * max(denominators(mi)) ## clearer pattern
m1 <- solve(mi)
range(m1 - m) ## roundoff still present
m2 <- m1 %>% numerical ## remove roundoff error - hopefully!
identical(m2, m) ## no roundoff

```

Ops.fractional

Method for the group generic function for the arithmetic operators

Description

Provides arithmetic operations for numeric objects or of class "fractional".

Usage

```

## S3 method for class 'fractional'
Ops(e1, e2)

```

Arguments

e1 A numeric object, possibly of class "fractional"
e2 A numeric object, possibly of class "fractional"

Value

The result of the arithmetic operation, flagged as class "fractional"

Examples

```

(M <- fractional(1:10/7))
M + 1
1 + M + M^2

```

rat *Calculate Rational Approximation Using Continued Fraction Methods*

Description

This is a behind-the-scenes function not likely to be used other than internally within the package. It computes the rational approximations for each value in the principal argument.

Usage

```
rat(x, eps = 1e-06, maxConv = 20L)
```

```
.ratr(x, eps = 1e-06, maxConv = 20)
```

```
ratr(x, eps = 1e-06, maxConv = 20)
```

Arguments

x	A numeric vector for which rational approximations are required.
eps	An absolute error tolerance on the approximation
maxConv	An upper limit on the number of convergents that the continued fraction expansion may employ. The fraction is terminated once the desired accuracy is met (or the upper limit is about to be exceeded).

Value

A 3 column matrix giving, respectively, the numerators, denominators and number of convergents needed to achieve the error tolerance, in the columns

Functions

- `rat`: C++ version of the same function used for speed
- `.ratr`: Workhorse function for a single value

See Also

[rat](#) which has the same functionality, but is coded in C++.

Examples

```
fractional(base::pi)
ratr(base::pi)

set.seed(123)
(u <- matrix(runif(10), 2, 5))
(ru <- ratr(u, eps = 1.0e-3, maxConv = 6))
(abs_error <- matrix(abs(u - ru[, 1]/ru[, 2]), 2, 5))
```

unfractional	<i>Demote a fractional object back to a numeric one</i>
--------------	---

Description

Given an object of class "fractional" this simple function removes the attributes that signal that it is to be treated as a fractional object, thus returning it to its original numeric status alone

Usage

```
unfractional(x)
```

Arguments

x A "fractional" object

Value

A simple numeric object like x

Examples

```
(tst <- fractional(matrix(0:9/10, 2, 5)))
(tst <- unfractional(tst))
```

vfractional	<i>Vectorized form for fractional</i>
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Description

A function which allows any or all of the first three arguments of fractional to be vectors, with short vectors recycled in the usual way. Note that the return value is a *character string* vector and may not be used in arithmetic operations

Usage

```
vfractional(x, eps = 1e-06, maxConv = 20)
```

Arguments

x as for fractional
eps as for fractional, but may be a vector
maxConv as for fractional but may be a vector

Value

A character string vector of class "charFrac"

Examples

```
oldOpt <- options(scipen = 15)
pi_approx <- vfractional(base::pi, eps = 0, maxConv = 1:10)
within(data.frame(pi_approx, stringsAsFactors = FALSE), {
  value = numerical(pi_approx)
  error = signif(base::pi - value, 3)
  n = seq_along(value) - 1
})[, c("n", "pi_approx", "value", "error")]
options(oldOpt)
```

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