# Package 'ismev'

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Description Functions to support the computations carried out in  `An Introduction to Statistical Modeling of Extreme Values' by  Stuart Coles. The functions may be divided into the following  groups; maxima/minima, order statistics, peaks over thresholds and point processes.
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dowjones

Index

Daily Closing Prices of The Dow Jones Index

**32** 

# Description

The dowjones data frame has 1304 rows and 2 columns. The second column contains daily closing prices of the Dow Jones Index over the period 1996 to 2000. The first column contains a POSIXct object giving the dates of each observation.

# Usage

data(dowjones)

## **Format**

This data frame contains the following columns:

Date A POSIXct object containing dates.

Index A numeric vector containing daily closing prices of the Dow Jones Index.

# Source

Coles, S. G. (2001) An Introduction to Statistical Modelling of Extreme Values. London: Springer.

engine 3

engine

Engine Failure Time Data

# Description

The engine data frame has 32 rows and 2 columns. The first column contains the corrosion level, the second column gives the engine failure time.

# Usage

data(engine)

## **Format**

This data frame contains the following columns:

Time A numeric vector of corrosion levels.

**Corrosion** A numeric vector of failure times.

#### **Source**

Unknown.

euroex

UK/Euro Exchange Rates

# Description

A numeric vector of daily exchange rates between the Euro and UK sterling.

## Usage

data(euroex)

## **Format**

A vector containing 975 observations.

## Source

Unknown.

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exchange

UK/US and UK/Canada Exchange Rates

#### **Description**

The exchange data frame has 975 rows and 2 columns. The columns contain daily exchange rates; UK sterling against the US dollar (first column) and UK sterling against the Canadian dollar (second column). The rownames contain the corresponding dates in a character string with the format "2000/05/26". This can be converted into a POSIXct or POSIXlt object using as.POSIXct or as.POSIXlt.

## Usage

data(exchange)

#### **Format**

This data frame contains the following columns:

USD.GBP US against UK exchange rate.

CAD.GBP Canada against UK exchange rate.

#### **Source**

Coles, S. G. (2001) An Introduction to Statistical Modelling of Extreme Values. London: Springer.

fremantle

Annual Maximum Sea Levels at Fremantle, Western Australia

## **Description**

The fremantle data frame has 86 rows and 3 columns. The second column gives 86 annual maximimum sea levels recorded at Fremantle, Western Australia, within the period 1897 to 1989. The first column gives the corresponding years. The third column gives annual mean values of the Southern Oscillation Index (SOI), which is a proxy for meteorological volitility.

# Usage

data(fremantle)

## **Format**

This data frame contains the following columns:

**Year** A numeric vector of years.

**SeaLevel** A numeric vector of annual sea level maxima.

SOI A numeric vector of annual mean values of the Southern Oscillation Index.

## Source

Coles, S. G. (2001) An Introduction to Statistical Modelling of Extreme Values. London: Springer.

gamGPDfitboot	Smooth Parameter Estimation and Bootstrapping of Generalized
gamer 21 Tesour	Pareto Distributions with Penalized Maximum Likelihood Estimation

## **Description**

gamGPDfit() fits the parameters of a generalized Pareto distribution (GPD) depending on covariates in a non- or semiparametric way.

gamGPDboot() fits and bootstraps the parameters of a GPD distribution depending on covariates in a non- or semiparametric way. Applies the post-blackend bootstrap of Chavez-Demoulin and Davison (2005).

## Usage

#### Arguments

epsnu

Ę	guments		
	х	data.frame containing the losses (in some component; can be specified with the argument datvar; the other components contain the covariates).	
	В	number of bootstrap replications.	
	threshold	threshold of the peaks-over-threshold (POT) method.	
	nexc	number of excesses. This can be used to determine	
	datvar	name of the data column in x which contains the the data to be modeled.	
	xiFrhs	right-hand side of the formula for $\xi$ in the gam() call for fitting $\xi$ .	
	nuFrhs	right-hand side of the formula for $\nu$ in the gam() call for fitting $\nu$ .	
	init	bivariate vector containing initial values for $(\xi, \beta)$ .	
	niter	maximal number of iterations in the backfitting algorithm.	
include.updates			
		logical indicating whether updates for xi and nu are returned as well (note: this might lead to objects of large size).	
	epsxi	epsilon for stop criterion for $\xi$ .	

epsilon for stop criterion for  $\nu$ .

boot.progress logical indicating whether progress information about gamGPDboot() is displayed.

progress logical indicating whether progress information about gamGPDfit() is displayed. For gamGPDboot(), progress is only passed to gamGPDfit() in the case that boot.progress==TRUE.

verbose logical indicating whether additional information (in case of undesired behavior) is printed. For gamGPDboot(), progress is only passed to gamGPDfit() if boot.progress==TRUE.

debug logical indicating whether initial fit (before the bootstrap is initiated) is saved.

additional arguments passed to gam() (which is called internally; see the source code of gamGPDfitUp()).

#### **Details**

gamGPDfit() fits the parameters  $\xi$  and  $\beta$  of the generalized Pareto distribution  $GPD(\xi, \beta)$  depending on covariates in a non- or semiparametric way. The distribution function is given by

$$G_{\xi,\beta}(x) = 1 - (1 + \xi x/\beta)^{-1/\xi}, \quad x \ge 0,$$

for  $\xi > 0$  (which is what we assume) and  $\beta > 0$ . Note that  $\beta$  is also denoted by  $\sigma$  in this package. Estimation of  $\xi$  and  $\beta$  by gamGPDfit() is done via penalized maximum likelihood estimation, where the estimators are computed with a backfitting algorithm. In order to guarantee convergence of this algorithm, a reparameterization of  $\beta$  in terms of the parameter  $\nu$  is done via

$$\beta = \exp(\nu)/(1+\xi).$$

The parameters  $\xi$  and  $\nu$  (and thus  $\beta$ ) are allowed to depend on covariates (including time) in a non-or semiparametric way, for example:

$$\xi = \xi(\boldsymbol{x}, t) = \boldsymbol{x}^{\top} \boldsymbol{\alpha}_{\xi} + h_{\xi}(t),$$

$$\nu = \nu(\boldsymbol{x}, t) = \boldsymbol{x}^{\top} \boldsymbol{\alpha}_{\nu} + h_{\nu}(t),$$

where x denotes the vector of covariates,  $\alpha_{\xi}$ ,  $\alpha_{\nu}$  are parameter vectors and  $h_{\xi}$ ,  $h_{\nu}$  are regression splines. For more details, see the references and the source code.

gamGPDboot() first fits the GPD parameters via gamGPDfit(). It then conducts the post-blackend bootstrap of Chavez-Demoulin and Davison (2005). To this end, it computes the residuals, resamples them (B times), reconstructs the corresponding excesses, and refits the GPD parameters via gamGPDfit() again.

#### Value

gamGPDfit() returns a list with the components

xi: estimated parameters  $\xi$ ;

beta: estimated parameters  $\beta$ ;

nu: estimated parameters  $\nu$ ;

se.xi: standard error for  $\xi$  ((possibly adjusted) second-order derivative of the reparameterized log-likelihood with respect to  $\xi$ ) multiplied by -1;

```
se.nu: standard error for \nu ((possibly adjusted) second-order derivative of the reparameterized
     log-likelihood with respect to \nu) multiplied by -1;
xi.covar: (unique) covariates for \xi;
nu.covar: (unique) covariates for \nu;
covar: available covariate combinations used for fitting \beta(\xi, \nu);
y: vector of excesses (exceedances minus threshold);
res: residuals:
MRD: mean relative distances between for all iterations, calculated between old parameters (\xi, \nu)
     (from the last iteration) and new parameters (currently estimated ones);
logL: log-likelihood at the estimated parameters;
xiObj: R object of type gamObject for estimated \xi (returned by mgcv::gam());
nu0bj: R object of type gam0bject for estimated \nu (returned by mgcv::gam());
xiUpdates: if include updates is TRUE, updates for \xi for each iteration. This is a list of R objects
     of type gamObject which contains xiObj as last element;
nuUpdates: if include updates is TRUE, updates for \nu for each iteration. This is a list of R objects
     of type gamObject which contains nuObj as last element;
```

gamGPDboot() returns a list of length B+1 where the first component contains the results of the initial fit via gamGPDfit() and the other B components contain the results for each replication of the post-blackend bootstrap.

#### Author(s)

Marius Hofert, Valerie Chavez-Demoulin.

#### References

Chavez-Demoulin, V., and Davison, A. C. (2005), Generalized additive models for sample extremes, *Applied Statistics* **54**(1), 207–222.

Chavez-Demoulin, V., and Hofert, M. (to be submitted), Smooth extremal models fitted by penalized maximum likelihood estimation.

## **Examples**

```
function(y) u + rGPD(n, xi=xi.true.A[y], beta=1)))
xi.true.B <- xi.true.A^2 # true xi for group "B"
## generate losses for group "B"
lossB <- unlist(lapply(1:nyears,</pre>
                        function(y) u + rGPD(n, xi=xi.true.B[y], beta=1)))
## build data frame
time <- rep(rep(years, each=n), 2) # "2" stands for the two groups
covar <- rep(c("A","B"), each=n*nyears)</pre>
value <- c(lossA, lossB)</pre>
x <- data.frame(covar=covar, time=time, value=value)</pre>
eps <- 1e-3 # to decrease the run time for this example
fit <- gamGPDfit(x, threshold=u, datvar="value", xiFrhs=~covar+s(time)-1,</pre>
                 nuFrhs=~covar+s(time)-1, epsxi=eps, epsnu=eps)
## note: choosing s(..., bs="cr") will fit cubic splines
## grab the fitted values per group and year
xi.fit <- fitted(fit$xi0bj)</pre>
xi.fit. <- xi.fit[1+(0:(2*nyears-1))*n] # pick fit for each group and year
xi.fit.A <- xi.fit.[1:nyears] # fit for "A" and each year
xi.fit.B <- xi.fit.[(nyears+1):(2*nyears)] # fit for "B" and each year
## plot the fitted values of xi and the true ones we simulated from
par(mfrow=c(1,2))
plot(years, xi.true.A, type="l", ylim=range(xi.true.A, xi.fit.A),
     main="Group A", xlab="Year", ylab=expression(xi))
points(years, xi.fit.A, type="l", col="red")
legend("topleft", inset=0.04, lty=1, col=c("black", "red"),
       legend=c("true", "fitted"), bty="n")
plot(years, xi.true.B, type="1", ylim=range(xi.true.B, xi.fit.B),
     main="Group B", xlab="Year", ylab=expression(xi))
points(years, xi.fit.B, type="l", col="blue")
legend("topleft", inset=0.04, lty=1, col=c("black", "blue"),
       legend=c("true", "fitted"), bty="n")
## Not run:
### Example 2: Comparison of (the more general) gamGPDfit() with gpd.fit() ########
set.seed(17) # setting seed
xi.true.A <- rep(0.4, length=nyears)</pre>
xi.true.B <- rep(0.8, length=nyears)</pre>
## generate losses for group "A"
lossA <- unlist(lapply(1:nyears,</pre>
                        function(y) u + rGPD(n, xi=xi.true.A[y], beta=1)))
## generate losses for group "B"
lossB <- unlist(lapply(1:nyears,</pre>
                        function(y) u + rGPD(n, xi=xi.true.B[y], beta=1)))
## build data frame
x <- data.frame(covar=covar, time=time, value=c(lossA, lossB))</pre>
## fit with gpd.fit
fit.coles <- gpd.fit(x$value, threshold=u, shl=1, sigl=1, ydat=x)</pre>
```

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gev.diag

Diagnostic Plots for GEV Models

## **Description**

Produces diagnostic plots for GEV models using the output of the function gev.fit.

## Usage

```
gev.diag(z)
```

## **Arguments**

z

An object returned by gev.fit.

## Value

For stationary models four plots are produced; a probability plot, a quantile plot, a return level plot and a histogram of data with fitted density.

For non-stationary models two plots are produced; a residual probability plot and a residual quantile plot.

#### See Also

```
gev.fit, gev.prof
```

## **Examples**

```
data(portpirie)
ppfit <- gev.fit(portpirie[,2])
gev.diag(ppfit)</pre>
```

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gev.fit

Maximum-likelihood Fitting of the GEV Distribution

#### **Description**

Maximum-likelihood fitting for the generalized extreme value distribution, including generalized linear modelling of each parameter.

## Usage

```
gev.fit(xdat, ydat = NULL, mul = NULL, sigl = NULL, shl = NULL,
   mulink = identity, siglink = identity, shlink = identity,
   muinit = NULL, siginit = NULL, shinit = NULL,
   show = TRUE, method = "Nelder-Mead", maxit = 10000, ...)
```

## **Arguments**

xdat A numeric vector of data to be fitted.

ydat A matrix of covariates for generalized linear modelling of the parameters (or

NULL (the default) for stationary fitting). The number of rows should be the

same as the length of xdat.

mul, sigl, shl Numeric vectors of integers, giving the columns of ydat that contain covari-

ates for generalized linear modelling of the location, scale and shape parameters repectively (or NULL (the default) if the corresponding parameter is stationary).

mulink, siglink, shlink

Inverse link functions for generalized linear modelling of the location, scale and

shape parameters repectively.

muinit, siginit, shinit

numeric of length equal to total number of parameters used to model the location, scale or shape parameter(s), resp. See Details section for default (NULL)

initial values.

show Logical; if TRUE (the default), print details of the fit.

method The optimization method (see optim for details).

maxit The maximum number of iterations.

... Other control parameters for the optimization. These are passed to components

of the control argument of optim.

# Details

The form of the GEV used is that of Coles (2001) Eq (3.2). Specifically, positive values of the shape parameter imply a heavy tail, and negative values imply a bounded upper tail.

For non-stationary fitting it is recommended that the covariates within the generalized linear models are (at least approximately) centered and scaled (i.e.\ the columns of ydat should be approximately centered and scaled).

gev.fit

Let m=mean(xdat) and s=sqrt(6\*var(xdat))/pi. Then, initial values assigend when 'muinit' is NULL are m - 0.57722 \* s (stationary case). When 'siginit' is NULL, the initial value is taken to be s, and when 'shinit' is NULL, the initial value is taken to be 0.1. When covariates are introduced (non-stationary case), these same initial values are used by default for the constant term, and zeros for all other terms. For example, if a GEV( mu(t)=mu0+mu1\*t, sigma, xi) is being fitted, then the initial value for mu0 is m - 0.57722 \* s, and 0 for mu1.

## Value

A list containing the following components. A subset of these components are printed after the fit. If show is TRUE, then assuming that successful convergence is indicated, the components nllh, mle and se are always printed.

nllh	single numeric giving the negative log-likelihood value.
mle	numeric vector giving the MLE's for the location, scale and shape parameters, resp.
se	numeric vector giving the standard errors for the MLE's for the location, scale and shape parameters, resp.
trans	An logical indicator for a non-stationary fit.
model	A list with components mul, sigl and shl.
link	A character vector giving inverse link functions.
conv	The convergence code, taken from the list returned by optim. A zero indicates successful convergence.
nllh	The negative logarithm of the likelihood evaluated at the maximum likelihood estimates.
data	The data that has been fitted. For non-stationary models, the data is standardized.
mle	A vector containing the maximum likelihood estimates.
cov	The covariance matrix.
se	A vector containing the standard errors.
vals	A matrix with three columns containing the maximum likelihood estimates of the location, scale and shape parameters at each data point.

## References

Coles, S., 2001. An Introduction to Statistical Modeling of Extreme Values. Springer-Verlag, London, U.K., 208pp.

## See Also

```
gev.diag, optim, gev.prof
```

# **Examples**

```
data(portpirie)
gev.fit(portpirie[,2])
```

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gev.	prof
500.	PI OI

Profile Log-likelihoods for Stationary GEV Models

# Description

Produce profile log-likelihoods for shape parameters and m year/block return levels for stationary GEV models using the output of the function gev.fit.

## Usage

```
gev.prof(z, m, xlow, xup, conf = 0.95, nint = 100)
gev.profxi(z, xlow, xup, conf = 0.95, nint = 100)
```

## **Arguments**

Z	An object returned by gev. fit. The object should represent a stationary model.
m	The return level (i.e.\ the profile likelihood is for the value that is exceeded with probability $1/m$ ).
xlow, xup	The least and greatest value at which to evaluate the profile likelihood.
conf	The confidence coefficient of the plotted profile confidence interval.
nint	The number of points at which the profile likelihood is evaluated.

## Value

A plot of the profile likelihood is produced, with a horizontal line representing a profile confidence interval with confidence coefficient conf.

## See Also

```
gev.fit, gev.diag
```

# **Examples**

```
data(portpirie)
ppfit <- gev.fit(portpirie[,2])
## Not run: gev.prof(ppfit, m = 10, 4.1, 5)
## Not run: gev.profxi(ppfit, -0.3, 0.3)</pre>
```

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glass

Breaking Strengths of Glass Fibres

## **Description**

A numeric vector containing breaking strengths of 63 glass fibres of length 1.5 centimetres, recorded under experimental conditions.

# Usage

```
data(glass)
```

#### **Format**

A vector containing 63 observations.

#### **Source**

Smith, R. L. and Naylor, J. C. (1987) A comparison of maximum likelihood and Bayesian estimators for the three-parameter Weibull distribution. *Applied Statistics* **36**, 358–396.

## References

Coles, S. G. (2001) An Introduction to Statistical Modelling of Extreme Values. London: Springer.

gpd.diag

Diagnostic Plots for GPD Models

# Description

Produces diagnostic plots for GPD models using the output of the function gpd.fit.

## Usage

```
gpd.diag(z)
```

# **Arguments**

z

An object returned by gpd.fit.

## Value

For stationary models four plots are produced; a probability plot, a quantile plot, a return level plot and a histogram of data with fitted density.

For non-stationary models two plots are produced; a residual probability plot and a residual quantile plot.

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## See Also

```
gpd.fit, gpd.prof, pp.fit
```

## **Examples**

```
data(rain)
rnfit <- gpd.fit(rain, 10)
gpd.diag(rnfit)</pre>
```

gpd.fit

Maximum-likelihood Fitting for the GPD Model

## **Description**

Maximum-likelihood fitting for the GPD model, including generalized linear modelling of each parameter.

#### Usage

```
gpd.fit(xdat, threshold, npy = 365, ydat = NULL, sigl = NULL,
    shl = NULL, siglink = identity, shlink = identity, siginit = NULL,
    shinit = NULL, show = TRUE,
    method = "Nelder-Mead", maxit = 10000, ...)
```

#### **Arguments**

xdat A numeric vector of data to be fitted.

threshold The threshold; a single number or a numeric vector of the same length as xdat.

npy The number of observations per year/block.

ydat A matrix of covariates for generalized linear modelling of the parameters (or

NULL (the default) for stationary fitting). The number of rows should be the

same as the length of xdat.

sigl, shl Numeric vectors of integers, giving the columns of ydat that contain covariates

for generalized linear modelling of the scale and shape parameters repectively

(or NULL (the default) if the corresponding parameter is stationary).

siglink, shlink

Inverse link functions for generalized linear modelling of the scale and shape

parameters repectively.

siginit, shinit

numeric giving initial value(s) for parameter estimates. If NULL, default is sqrt(6 \* var(xdat))/pi and 0.1 for the scale and shape parameters, resp. If using parameter covariates, then these values are used for the constant term, and zeros

for all other terms.

method The optimization method (see optim for details).

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maxit The maximum number of iterations.

Other control parameters for the optimization. These are passed to components

of the control argument of optim.

#### **Details**

For non-stationary fitting it is recommended that the covariates within the generalized linear models are (at least approximately) centered and scaled (i.e.\ the columns of ydat should be approximately centered and scaled).

The form of the GP model used follows Coles (2001) Eq (4.7). In particular, the shape parameter is defined so that positive values imply a heavy tail and negative values imply a bounded upper value.

#### Value

npy

xdata

A list containing the following components. A subset of these components are printed after the fit. If show is TRUE, then assuming that successful convergence is indicated, the components nexc, nllh, mle, rate and se are always printed.

nexc single numeric giving the number of threshold exceedances. nllh nsingle umeric giving the negative log-likelihood value. mle numeric vector giving the MLE's for the scale and shape parameters, resp. single numeric giving the estimated probability of exceeding the threshold. rate se numeric vector giving the standard error estiamtes for the scale and shape parameter estimates, resp. trans An logical indicator for a non-stationary fit. mode1 A list with components sigl and shl. link A character vector giving inverse link functions. threshold The threshold, or vector of thresholds. The number of data points above the threshold. nexc The data that lie above the threshold. For non-stationary models, the data is data standardized. The convergence code, taken from the list returned by optim. A zero indicates conv successful convergence. nllh The negative logarithm of the likelihood evaluated at the maximum likelihood estimates. vals A matrix with three columns containing the maximum likelihood estimates of the scale and shape parameters, and the threshold, at each data point. mle A vector containing the maximum likelihood estimates. The proportion of data points that lie above the threshold. rate The covariance matrix. cov A vector containing the standard errors. se The number of data points (i.e.\ the length of xdat). n The number of observations per year/block.

The data that has been fitted.

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## References

Coles, S., 2001. An Introduction to Statistical Modeling of Extreme Values. Springer-Verlag, London, U.K., 208pp.

#### See Also

```
gpd.diag, optim, gpd.prof, gpd.fitrange, mrl.plot, pp.fit
```

# **Examples**

```
data(rain)
gpd.fit(rain, 10)
```

gpd.fitrange

Fitting the GPD Model Over a Range of Thresholds

#### **Description**

Maximum-likelihood fitting for a stationary GPD model, over a range of thresholds. Graphs of parameter estimates which aid the selection of a threshold are produced.

## Usage

```
gpd.fitrange(data, umin, umax, nint = 10, show = FALSE, ...)
```

## **Arguments**

data A numeric vector of data to be fitted.

umin, umax The minimum and maximum thresholds at which the model is fitted.

nint The number of fitted models.

show Logical; if TRUE, print details of each fit.

... Optional arguments to gpd. fit.

## Value

Two graphs showing maximum likelihood estimates and confidence intervals of the shape and modified scale parameters over a range of thresholds are produced. A list object is returned invisibly with components: 'threshold' numeric vector of length 'nint' giving the thresholds used, 'mle' an 'nint X 3' matrix giving the maximum likelihood parameter estimates (columns are location, scale and shape respectively), 'se' an 'nint X 3' matrix giving the estimated standard errors for the parameter estimates (columns are location, scale and shape, resp.), 'ci.low', 'ci.up' 'nint X 3' matrices giving the lower and upper 95 intervals, resp. (columns same as for 'mle' and 'se').

#### See Also

```
gpd.fit, mrl.plot, pp.fit, pp.fitrange
```

gpd.prof

# **Examples**

```
## Not run: data(rain)
## Not run: gpd.fitrange(rain, 10, 40)
```

gpd.prof

Profile Log-likelihoods for Stationary GPD Models

# **Description**

Produce profile log-likelihoods for shape parameters and m year/block return levels for stationary GPD models using the output of the function gpd.fit.

# Usage

```
gpd.prof(z, m, xlow, xup, npy = 365, conf = 0.95, nint = 100)
gpd.profxi(z, xlow, xup, conf = 0.95, nint = 100)
```

# Arguments

Z	An object returned by gpd. fit. The object should represent a stationary model.
m	The return level (i.e.\ the profile likelihood is for the value that is exceeded with probability $1/m$ ).
xlow, xup	The least and greatest value at which to evaluate the profile likelihood.
npy	The number of observations per year.
conf	The confidence coefficient of the plotted profile confidence interval.
nint	The number of points at which the profile likelihood is evaluated.

## Value

A plot of the profile likelihood is produced, with a horizontal line representing a profile confidence interval with confidence coefficient conf.

# See Also

```
gpd.fit, gpd.diag
```

# Examples

```
data(rain)
rnfit <- gpd.fit(rain, 10)
## Not run: gpd.prof(rnfit, m = 10, 55, 75)
## Not run: gpd.profxi(rnfit, -0.02, 0.15)</pre>
```

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gum.diag

Diagnostic Plots for Gumbel Models

## **Description**

Produces diagnostic plots for Gumbel models using the output of the function gum. fit.

## Usage

```
gum.diag(z)
```

## **Arguments**

z

An object returned by gum. fit.

#### Value

For stationary models four plots are produced; a probability plot, a quantile plot, a return level plot and a histogram of data with fitted density.

For non-stationary models two plots are produced; a residual probability plot and a residual quantile plot.

## See Also

```
gev.fit, gum.fit
```

## **Examples**

```
data(portpirie)
ppfit <- gum.fit(portpirie[,2])
gum.diag(ppfit)</pre>
```

gum.fit

Maximum-likelihood Fitting of the Gumbel Distribution

## **Description**

Maximum-likelihood fitting for the gumbel distribution, including generalized linear modelling of each parameter.

# Usage

```
gum.fit(xdat, ydat = NULL, mul = NULL, sigl = NULL, mulink = identity,
    siglink = identity, muinit = NULL, siginit = NULL, show = TRUE,
    method = "Nelder-Mead", maxit = 10000, ...)
```

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## Arguments

xdat A numeric vector of data to be fitted.

ydat A matrix of covariates for generalized linear modelling of the parameters (or

NULL (the default) for stationary fitting). The number of rows should be the

same as the length of xdat.

mul, sigl Numeric vectors of integers, giving the columns of ydat that contain covariates

for generalized linear modelling of the location and scale parameters repectively

(or NULL (the default) if the corresponding parameter is stationary).

mulink, siglink

Inverse link functions for generalized linear modelling of the location and scale

parameters repectively.

muinit, siginit

numeric giving initial parameter estimates. See Details section for information

about default values (NULL).

show Logical; if TRUE (the default), print details of the fit.

method The optimization method (see optim for details).

maxit The maximum number of iterations.

... Other control parameters for the optimization. These are passed to components

of the control argument of optim.

#### **Details**

For non-stationary fitting it is recommended that the covariates within the generalized linear models are (at least approximately) centered and scaled (i.e.\ the columns of ydat should be approximately centered and scaled).

Let m=mean(xdat) and s=sqrt(6\*var(xdat))/pi. Then, initial values assigned when 'muinit' is NULL are m - 0.57722 \* s (stationary case). When 'siginit' is NULL, the initial value is taken to be s, and when 'shinit' is NULL. When covariates are introduced (non-stationary case), these same initial values are used by default for the constant term, and zeros for all other terms. For example, if a Gumbel( mu(t)=mu0+mu1\*t, sigma) is being fitted, then the initial value for mu0 is m - 0.57722 \* s, and 0 for mu1.

## Value

A list containing the following components. A subset of these components are printed after the fit. If show is TRUE, then assuming that successful convergence is indicated, the components nllh, mle and se are always printed.

trans An logical indicator for a non-stationary fit.

model A list with components mul and sigl.

link A character vector giving inverse link functions.

conv The convergence code, taken from the list returned by optim. A zero indicates

successful convergence.

nllh The negative logarithm of the likelihood evaluated at the maximum likelihood

estimates.

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data	The data that has been fitted. For non-stationary models, the data is standardized.
mle	A vector containing the maximum likelihood estimates.
cov	The covariance matrix.
se	A vector containing the standard errors.
vals	A matrix with two columns containing the maximum likelihood estimates of the location and scale parameters at each data point.

#### See Also

```
gum.diag, optim, gev.fit
```

# **Examples**

```
data(portpirie)
gum.fit(portpirie[,2])
```

ismev

ismev - an Introduction to Statistical Modeling of Extreme Values

## **Description**

**ismev** includes functions to support the computations carried out in Coles (2001). The functions may be divided into the following groups; maxima/minima, order statistics, peaks over thresholds and point processes. **ismev** is an R port of the S-Plus extreme value statistical routines believed to be originally written by Janet E. Heffernan.

Primary functions include:

```
gev.fit, gev.diag, gpd.fit, gpd.diag, pp.fit and pp.diag.
```

Original R port was carried out by Alec G. Stephenson, and the package is currently being maintained by Eric Gilleland.

Datasets from Coles (2001) included are:

dowjones euroex fremantle portpirie venice wind engine exchange glass rain wavesurge wooster

#### References

Coles, Stuart (2001) An Introduction to Statistical Modeling of Extreme Values, London, UK: Springer, ISBN: 1852334592, 208 pp.

mrl.plot 21

mrl.plot Mean Residual Life Plot

## **Description**

An empirical mean residual life plot, including confidence intervals, is produced. The mean residual life plot aids the selection of a threshold for the GPD or point process models.

## Usage

```
mrl.plot(data, umin = min(data), umax = max(data) - 0.1,
    conf = 0.95, nint = 100)
```

# Arguments

data	A numeric vector of data to be fitted.
umin, umax	The minimum and maximum thresholds at which the mean residual life function is calculated.
conf	The confidence coefficient for the confidence intervals depicted in the plot.
nint	The number of points at which the mean residual life function is calculated.

# See Also

```
gpd.fit, gpd.fitrange, pp.fit
```

# **Examples**

```
data(rain)
mrl.plot(rain)
```

portpirie	Annual Maximum Sea Levels at Port Pirie, South Australia
-----------	--

# Description

The portpirie data frame has 65 rows and 2 columns. The second column gives annual maximimum sea levels recorded at Port Pirie, South Australia, from 1923 to 1987. The first column gives the corresponding years.

## Usage

```
data(portpirie)
```

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## **Format**

This data frame contains the following columns:

Year A numeric vector of years.

SeaLevel A numeric vector of annual sea level maxima.

## **Source**

Coles, S. G. (2001) An Introduction to Statistical Modelling of Extreme Values. London: Springer.

pp.diag

Diagnostic Plots for Point Process Models

# Description

Produces diagnostic plots for point process models using the output of the function pp.fit.

## Usage

```
pp.diag(z)
```

## **Arguments**

Z

An object returned by pp.fit.

## Value

For stationary models two plots are produced; a probability plot and a quantile plot.

For non-stationary models two plots are produced; a residual probability plot and a residual quantile plot.

# See Also

```
pp.fit,gpd.fit
```

# **Examples**

```
data(rain)
rnfit <- pp.fit(rain, 10)
pp.diag(rnfit)</pre>
```

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pp.f	it
------	----

Maximum-likelihood Fitting for the Point Process Model

# **Description**

Maximum-likelihood fitting for the point process model, including generalized linear modelling of each parameter.

## Usage

```
pp.fit(xdat, threshold, npy = 365, ydat = NULL, mul = NULL, sigl =
   NULL, shl = NULL, mulink = identity, siglink = identity, shlink =
   identity, muinit = NULL, siginit = NULL, shinit = NULL, show = TRUE,
   method = "Nelder-Mead", maxit = 10000, ...)
```

## **Arguments**

xdat	A numeric vector of data to be fitted.		
threshold	The threshold; a single number or a numeric vector of the same length as xdat.		
npy	The number of observations per year/block.		
ydat	A matrix of covariates for generalized linear modelling of the parameters (or NULL (the default) for stationary fitting). The number of rows should be the same as the length of xdat.		
mul, sigl, shl	Numeric vectors of integers, giving the columns of ydat that contain covariates for generalized linear modelling of the location, scale and shape parameters repectively (or NULL (the default) if the corresponding parameter is stationary).		
mulink, siglink, shlink			
	Inverse link functions for generalized linear modelling of the location, scale and shape parameters repectively.		
muinit, siginit, shinit			
	numeric giving initial parameter estimates. See Details section for information on default (NULL) initial values.		
show	Logical; if TRUE (the default), print details of the fit.		
method	The optimization method (see optim for details).		
maxit	The maximum number of iterations.		
•••	Other control parameters for the optimization. These are passed to components of the control argument of optim.		

# **Details**

For non-stationary fitting it is recommended that the covariates within the generalized linear models are (at least approximately) centered and scaled (i.e.\ the columns of ydat should be approximately centered and scaled). Otherwise, the numerics may become unstable.

pp.fit

As of version 1.32, a more accurate estimate of the exceedance rate, in the face of covariates, is used (at the expense of computational efficiency). In particular, when including covariates, parameter estimates may differ from those in Coles (2001).

Let m=mean(xdat) and s=sqrt(6\*var(xdat))/pi. Then, initial values assigend when 'muinit' is NULL are m - 0.57722 \* s (stationary case). When 'siginit' is NULL, the initial value is taken to be s, and when 'shinit' is NULL, the initial value is taken to be 0.1. When covariates are introduced (non-stationary case), these same initial values are used by default for the constant term, and zeros for all other terms. For example, if a GEV( mu(t)=mu0+mu1\*t, sigma, xi) is being fitted, then the initial value for mu0 is m - 0.57722 \* s, and 0 for mu1.

#### Value

A list containing the following components. A subset of these components are printed after the fit. If show is TRUE, then assuming that successful convergence is indicated, the components nexc, nllh, mle and se are always printed.

An logical indicator for a non-stationary fit.
A list with components mul, sigl and shl.
A character vector giving inverse link functions.
The threshold, or vector of thresholds.
The number of observations per year/block.
The number of data points above the threshold.
The data that lie above the threshold. For non-stationary models, the data is standardized.
The convergence code, taken from the list returned by optim. A zero indicates successful convergence.
The negative logarithm of the likelihood evaluated at the maximum likelihood estimates.
A matrix with four columns containing the maximum likelihood estimates of the location, scale and shape parameters, and the threshold, at each data point.
A matrix with three rows containing the maximum likelihood estimates of corresponding GPD location, scale and shape parameters at each data point.
A vector containing the maximum likelihood estimates.
The covariance matrix.
A vector containing the standard errors.

#### Warning

Different optimization methods may result in wildly different parameter estimates.

#### Note

This code is adapted by Eric Gilleland from code originally written for S-Plus by Stuart Coles, and ported to R by Alec Stephenson. See details section above.

pp.fitrange 25

#### References

Beirlant J, Goegebeur Y, Segers J and Teugels J. (2004). Statistics of Extremes, Wiley, Chichester, England.

Coles, Stuart (2001). An Introduction to Statistical Modeling of Extreme Values. Springer-Verlag, London.

#### See Also

```
pp.diag, optim, pp.fitrange, mrl.plot, gpd.fit
```

# **Examples**

```
data(rain)
pp.fit(rain, 10)
```

pp.fitrange

Fitting the Point Process Model Over a Range of Thresholds

## **Description**

Maximum-likelihood fitting for a stationary point process model, over a range of thresholds. Graphs of parameter estimates which aid the selection of a threshold are produced.

## Usage

```
pp.fitrange(data, umin, umax, npy = 365, nint = 10, show = FALSE, ...)
```

#### **Arguments**

data A numeric vector of data to be fitted.

umin, umax The minimum and maximum thresholds at which the model is fitted.

npy The number of observations per year/block.

nint The number of fitted models.

show Logical; if TRUE, print details of each fit.

... Optional arguments to pp.fit.

## Value

Three graphs showing maximum likelihood estimates and confidence intervals of the location, scale and shape parameters over a range of thresholds are produced. A list object is returned invisibly with components: 'threshold' numeric vector of length 'nint' giving the thresholds used, 'mle' an 'nint X 3' matrix giving the maximum likelihood parameter estimates (columns are location, scale and shape respectively), 'se' an 'nint X 3' matrix giving the estimated standard errors for the parameter estimates (columns are location, scale and shape, resp.), 'ci.low', 'ci.up' 'nint X 3' matrices giving the lower and upper 95 intervals, resp. (columns same as for 'mle' and 'se').

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## See Also

```
pp.fit, mrl.plot, gpd.fit, gpd.fitrange
```

## **Examples**

```
## Not run: data(rain)
## Not run: pp.fitrange(rain, 10, 40)
```

rain

Daily Rainfall Accumulations in South-West England

# Description

A numeric vector containing daily rainfall accumulations at a location in south-west England over the period 1914 to 1962.

## Usage

data(rain)

#### **Format**

A vector containing 17531 observations.

#### **Source**

Coles, S. G. and Tawn, J. A. (1996) Modelling extremes of the areal rainfall process. *Journal of the Royal Statistical Society, B* **53**, 329–347.

## References

Coles, S. G. (2001) An Introduction to Statistical Modelling of Extreme Values. London: Springer.

rlarg.diag

Diagnostic Plots for Order Statistics Models

# **Description**

Produces diagnostic plots for order statistics models using the output of the function rlarg, fit.

## Usage

```
rlarg.diag(z, n = z r)
```

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## Arguments

- z An object returned by rlarg.fit.
- n Probability and quantile plots are produced for the largest n order statistics.

#### Value

For stationary models four plots are initially produced; a probability plot, a quantile plot, a return level plot and a histogram of data with fitted density. Then probability and quantile plots are produced for the largest n order statistics.

For non-stationary models residual probability plots and residual quantile plots are produced for the largest n order statistics.

## See Also

```
rlarg.fit
```

#### **Examples**

```
## Not run: data(venice)
## Not run: venfit <- rlarg.fit(venice[,-1])
## Not run: rlarg.diag(venfit)</pre>
```

rlarg.fit

Maximum-likelihood Fitting of Order Statistics Model

#### **Description**

Maximum-likelihood fitting for the order statistic model, including generalized linear modelling of each parameter.

## Usage

```
rlarg.fit(xdat, r = dim(xdat)[2], ydat = NULL, mul = NULL, sigl = NULL,
    shl = NULL, mulink = identity, siglink = identity, shlink = identity,
    muinit = NULL, siginit = NULL, shinit = NULL, show = TRUE,
    method = "Nelder-Mead", maxit = 10000, ...)
```

## **Arguments**

xdat

A numeric matrix of data to be fitted. Each row should be a vector of decreasing order, containing the largest order statistics for each year (or time period). The first column therefore contains annual (or period) maxima. Only the first r columns are used for the fitted model. By default, all columns are used. If one year (or time period) contains fewer order statistics than another, missing values can be appended to the end of the corresponding row.

r The largest r order statistics are used for the fitted model.

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ydat A matrix of covariates for generalized linear modelling of the parameters (or

NULL (the default) for stationary fitting). The number of rows should be the

same as the number of rows of xdat.

mul, sigl, shl Numeric vectors of integers, giving the columns of ydat that contain covariates for generalized linear modelling of the location, scale and shape parameters

repectively (or NULL (the default) if the corresponding parameter is stationary).

mulink, siglink, shlink

Inverse link functions for generalized linear modelling of the location, scale and

shape parameters repectively.

muinit, siginit, shinit

numeric of length equal to total number of parameters used to model the location, scale or shape parameter(s), resp. See Details section for default (NULL)

initial values.

show Logical; if TRUE (the default), print details of the fit.

method The optimization method (see optim for details).

maxit The maximum number of iterations.

.. Other control parameters for the optimization. These are passed to components

of the control argument of optim.

#### **Details**

For non-stationary fitting it is recommended that the covariates within the generalized linear models are (at least approximately) centered and scaled (i.e.\ the columns of ydat should be approximately centered and scaled).

Let m=mean(xdat) and s=sqrt(6\*var(xdat))/pi. Then, initial values assigned when 'muinit' is NULL are m - 0.57722 \* s (stationary case). When 'siginit' is NULL, the initial value is taken to be s, and when 'shinit' is NULL, the initial value is taken to be 0.1. When covariates are introduced (non-stationary case), these same initial values are used by default for the constant term, and zeros for all other terms. For example, if a GEV( mu(t)=mu0+mu1\*t, sigma, xi) is being fitted, then the initial value for mu0 is m - 0.57722 \* s, and 0 for mu1.

## Value

A list containing the following components. A subset of these components are printed after the fit. If show is TRUE, then assuming that successful convergence is indicated, the components nllh, mle and se are always printed.

trans	An logical indicator for a non-stationary fit.
model	A list with components mul, sigl and shl.
link	A character vector giving inverse link functions.
conv	The convergence code, taken from the list returned by optim. A zero indicates successful convergence.
nllh	The negative logarithm of the likelihood evaluated at the maximum likelihood estimates.
data	The data that has been fitted. For non-stationary models, the data is standardized.

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mle	A vector containing the maximum likelihood estimates.
cov	The covariance matrix.
se	A vector containing the standard errors.
vals	A matrix with three columns containing the maximum likelihood estimates of the location, scale and shape parameters at each data point.
r	The number of order statistics used.

## See Also

```
rlarg.diag, optim
```

## **Examples**

```
## Not run: data(venice)
## Not run: rlarg.fit(venice[,-1])
```

venice

Venice Sea Levels

## **Description**

The venice data frame has 51 rows and 11 columns. The final ten columns contain the 10 largest sea levels observed within the year given by the first column. The ten largest sea levels are given for every year in the period 1931 to 1981, excluding 1935 in which only the six largest measurements are available.

## Usage

```
data(venice)
```

## **Format**

This data frame contains the following columns:

Year A numeric vector of years.

- r1 Annual sea level maxima.
- r2 The second largest sea level.
- r3 The third largest sea level.
- r4 The forth largest sea level.
- **r5** The fifth largest sea level.
- **r6** The sixth largest sea level.
- r7 The seventh largest sea level.
- r8 The eigth largest sea level.
- r9 The ninth largest sea level.
- **r10** The tenth largest sea level.

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## **Source**

Smith, R. L. (1986) Extreme value theory based on the r largest annual events. *Journal of Hydrology* **86**, 27–43.

## References

Coles, S. G. (2001) An Introduction to Statistical Modelling of Extreme Values. London: Springer.

wavesurge

Wave and Surge Heights in South-West England

# Description

The wavesurge data frame has 2894 rows and 2 columns. The columns contain wave and surge heights (in metres) at a single location off south-west England.

## Usage

data(wavesurge)

#### **Format**

This data frame contains the following columns:

wave A numeric vector of wave heights.

surge A numeric vector of surge heights.

## Source

Coles, S. G. (2001) An Introduction to Statistical Modelling of Extreme Values. London: Springer.

wind

Annual Maximum Wind Speeds at Albany and Hartford

## **Description**

The wind data frame has 40 rows and 3 columns. The second and third columns contain annual maximum wind speeds at Albany, New York and Hartford, Connecticut respectively, over the period 1944 to 1983. The first column gives the corresponding years.

## Usage

data(wind)

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## **Format**

This data frame contains the following columns:

Year A numeric vector of years.

Hartford Annual maximum wind speeds at Hartford.

Albany Annual maximum wind speeds at Albany.

## **Source**

Coles, S. G. (2001) An Introduction to Statistical Modelling of Extreme Values. London: Springer.

wooster

Minimum Temperatures at Wooster, Ohio

## **Description**

A numeric vector containing daily minimum temperatures, in degrees Fahrenheit, at Wooster, Ohio, over the period 1983 to 1988.

## Usage

data(wooster)

#### **Format**

A vector containing 1826 observations.

# Source

Coles, S. G., Tawn, J. A. and Smith, R. L. (1994) A seasonal Markov model for extremely low temperatures. *Environmetrics* **5**, 221–239.

#### References

Coles, S. G. (2001) *An Introduction to Statistical Modelling of Extreme Values*. London: Springer. Smith, R. L., Tawn, J. A. and Coles, S. G. (1997) Markov chain models for threshold exceedences. *Biometrica* **84**, 249–268.

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