

Package ‘scoringRules’

October 5, 2020

Type Package

Title Scoring Rules for Parametric and Simulated Distribution
Forecasts

Version 1.0.1

Date 2020-10-03

Author Alexander Jordan, Fabian Krueger, Sebastian Lerch

Maintainer Fabian Krueger <Fabian.Krueger83@gmail.com>

Description Dictionary-like reference for computing scoring rules in a wide range of situations. Covers both parametric forecast distributions (such as mixtures of Gaussians) and distributions generated via simulation.

URL <https://github.com/FK83/scoringRules>

License GPL (>= 2)

Imports Rcpp (>= 0.12.0), methods, MASS, knitr

Depends R (>= 3.00)

Suggests gsl (>= 1.8-3), hypergeo(>= 1.0), rmarkdown, testthat, crch

LinkingTo Rcpp, RcppArmadillo

RoxygenNote 7.1.1

VignetteBuilder knitr

Encoding UTF-8

NeedsCompilation yes

Repository CRAN

Date/Publication 2020-10-05 10:10:02 UTC

R topics documented:

ar_ms	2
crps.numeric	5
GDP data	8
logs.numeric	9

plot.casestudy	12
plot.mcstudy	13
print.casestudy	14
print.mcstudy	14
run_casestudy	15
run_mcstudy	16
scores	17
scores_2pexp	18
scores_2pnorm	19
scores_beta	19
scores_binom	20
scores_exp	20
scores_gamma	21
scores_gev	22
scores_gpd	22
scores_hyper	23
scores_lapl	24
scores_llapl	24
scores_llogis	25
scores_lnorm	25
scores_logis	26
scores_mixnorm	27
scores_moments	28
scores_nbinom	29
scores_norm	30
scores_pois	31
scores_sample_multiv	31
scores_sample_univ	33
scores_t	35
scores_unif	36
summary.casestudy	37
summary.mcstudy	37
Supplementary distributions: Positive real line	38
Supplementary distributions: Real line	39
Supplementary distributions: Variable support	40
Index	43

ar_ms

Bayesian analysis of a Markov Switching autoregressive model

Description

Bayesian analysis of a Markov Switching autoregressive model

Usage

```

ar_ms(
  y,
  nlag = 1,
  beta_switch = FALSE,
  variance_switch = TRUE,
  identification_constraint = "variance",
  n_burn = 5000,
  n_rep = 20000,
  forecast_periods = 5,
  printout = FALSE,
  Hm1_delta = 25,
  mu_delta = 0,
  s_ = 0.3,
  nu_ = 3,
  R = matrix(c(8, 2, 2, 8), nrow = 2)
)

```

Arguments

y numeric vector (time series to be analyzed).

nlag integer, number of autoregressive lags (defaults to one).

beta_switch, variance_switch logicals, indicating whether there should be Markovian state dependence in regression parameters and residual variance, respectively. Defaults to `beta_switch = FALSE, variance_switch = TRUE`.

identification_constraint character, indicating how to identify latent states. Possible values: "variance", "mean" and "persistence". Defaults to "variance".

n_burn, n_rep integers, number of MCMC iterations for burn-in and main analysis.

forecast_periods number of future periods for which forecasts are computed.

printout logical, whether to print progress report during MCMC (defaults to FALSE).

Hm1_delta, mu_delta, s_, nu_, R prior parameters as described in KLTG (2020, Appendix E and Table 4).

Details

The default parameters are as set by KLTG (2020, Section 5). The output matrices `fcMeans` and `fcSds` can be used to construct the mixture-of-parameters estimator analyzed by KLTG. While many of the model features can be changed as described above, the number of Markov regimes is always fixed at two.

`ar_ms` is an R/C++ implementation of Matlab code kindly shared by Gianni Amisano via his website (<https://sites.google.com/site/gianniamisanowebiste/>). See Amisano and Giacomini (2007) who analyze a similar model.

Value

List containing parameter estimates and forecasts, with the following elements:

- pars, matrix of posterior draws for parameters (rows are MCMC iterations, columns are parameters)
- fcMeans and fcSds, matrices of forecast means and standard deviations (rows are MCMC iterations, columns are forecast horizons)
- probs, matrix of filtered probabilities for first latent state (rows are MCMC iterations, columns are time periods, excluding the first nlag values for initialization).
- count, integer, counter for the number of states that were relabeled based on identification_constraint.

Author(s)

Fabian Krueger, based on Matlab code by Gianni Amisano (see details section)

References

Amisano, G. and R. Giacomini (2007), ‘Comparing density forecasts via weighted likelihood ratio tests’, *Journal of Business and Economic Statistics* 25, 177-190. doi: [10.1198/073500106000000332](https://doi.org/10.1198/073500106000000332)

Krueger, F., Lerch, S., Thorarinsdottir, T.L. and T. Gneiting (2020): ‘Predictive inference based on Markov chain Monte Carlo output’, *International Statistical Review*, forthcoming. doi: [10.1111/insr.12405](https://doi.org/10.1111/insr.12405)

See Also

[run_casestudy](#) uses [ar_ms](#) to replicate the results of KLTG (2020, Section 5).

Examples

```
## Not run:
# Use GDP data from 2014Q4 edition
data(gdp)
dat <- subset(gdp, vint == "2014Q4")
y <- dat$val[order(dat$dt)]

# Fit model, using the default settings
set.seed(816)
fit <- ar_ms(y)

# Histograms of parameter draws
par(mfrow = c(2, 2))
hist(fit$pars[,1], main = "Intercept (state-invariant)", xlab = "")
hist(fit$pars[,2], main = "AR(1) term (state-invariant)", xlab = "")
hist(1/fit$pars[,3], main = "Residual variance in 1st state", xlab = "")
hist(1/fit$pars[,4], main = "Residual variance in 2nd state", xlab = "")

# By construction, the residual variance is smaller in the 1st than in the 2nd state:
print(mean(1/fit$pars[,3] < 1/fit$pars[,4]))

## End(Not run)
```

crps.numeric	<i>Continuous Ranked Probability Score for Parametric Forecast Distributions</i>
--------------	--

Description

Calculate the Continuous Ranked Probability Score (CRPS) given observations and parameters of a family of distributions.

Usage

```
## S3 method for class 'numeric'
crps(y, family, ...)
```

Arguments

y	vector of realized values.
family	string which specifies the parametric family; current options: "2pexp", "2pnorm", "beta", "binom", "cl
...	vectors of parameter values; expected input depends on the chosen family. See details below.

Details

Mathematical details are available in Appendix A of the vignette *Evaluating probabilistic forecasts with scoringRules* that accompanies the package.

The parameters supplied to each of the functions are numeric vectors:

1. Distributions defined on the real line:
 - "laplace" or "lapl": location (real-valued location parameter), scale (positive scale parameter); see [crps_lapl](#)
 - "logistic" or "logis": location (real-valued location parameter), scale (positive scale parameter); see [crps_logis](#)
 - "normal" or "norm": mean, sd (mean and standard deviation); see [crps_norm](#)
 - "normal-mixture" or "mixture-normal" or "mixnorm": m (mean parameters), s (standard deviations), w (weights); see [crps_mixnorm](#); note: matrix-input for parameters
 - "t": df (degrees of freedom), location (real-valued location parameter), scale (positive scale parameter); see [crps_t](#)
 - "two-piece-exponential" or "2pexp": location (real-valued location parameter), scale1, scale2 (positive scale parameters); see [crps_2pexp](#)
 - "two-piece-normal" or "2pnorm": location (real-valued location parameter), scale1, scale2 (positive scale parameters); see [crps_2pnorm](#)
2. Distributions for non-negative random variables:
 - "exponential" or "exp": rate (positive rate parameter); see [crps_exp](#)
 - "gamma": shape (positive shape parameter), rate (positive rate parameter), scale (alternative to rate); see [crps_gamma](#)

- "log-laplace" or "llapl": locationlog (real-valued location parameter), scalelog (positive scale parameter); see [crps_llapl](#)
 - "log-logistic" or "llogis": locationlog (real-valued location parameter), scalelog (positive scale parameter); see [crps_llogis](#)
 - "log-normal" or "lnorm": locationlog (real-valued location parameter), scalelog (positive scale parameter); see [crps_lnorm](#)
3. Distributions with flexible support and/or point masses:
- "beta": shape1, shape2 (positive shape parameters), lower, upper (lower and upper limits); see [crps_beta](#)
 - "uniform" or "unif": min, max (lower and upper limits), lmass, umass (point mass in lower or upper limit); see [crps_unif](#)
 - "expM": location (real-valued location parameter), scale (positive scale parameter), mass (point mass in location); see [crps_expM](#)
 - "gev": location (real-valued location parameter), scale (positive scale parameter), shape (real-valued shape parameter); see [crps_gev](#)
 - "gpd": location (real-valued location parameter), scale (positive scale parameter), shape (real-valued shape parameter), mass (point mass in location); see [crps_gpd](#)
 - "tlogis": location (location parameter), scale (scale parameter), lower, upper (lower and upper limits); see [crps_tlogis](#)
 - "clogis": location (location parameter), scale (scale parameter), lower, upper (lower and upper limits); see [crps_clogis](#)
 - "gtclogis": location (location parameter), scale (scale parameter), lower, upper (lower and upper limits); lmass, umass (point mass in lower or upper limit); see [crps_gtclogis](#)
 - "tnorm": location (location parameter), scale (scale parameter), lower, upper (lower and upper limits); see [crps_tnorm](#)
 - "cnorm": location (location parameter), scale (scale parameter), lower, upper (lower and upper limits); see [crps_cnorm](#)
 - "gtcnorm": location (location parameter), scale (scale parameter), lower, upper (lower and upper limits); lmass, umass (point mass in lower or upper limit); see [crps_gtcnorm](#)
 - "tt": df (degrees of freedom), location (location parameter), scale (scale parameter), lower, upper (lower and upper limits); see [crps_tt](#)
 - "ct": df (degrees of freedom), location (location parameter), scale (scale parameter), lower, upper (lower and upper limits); see [crps_ct](#)
 - "gtct": df (degrees of freedom), location (location parameter), scale (scale parameter), lower, upper (lower and upper limits); lmass, umass (point mass in lower or upper limit); see [crps_gtct](#)
4. Distributions of discrete variables:
- "binom": size (number of trials (zero or more)), prob (probability of success on each trial); see [crps_binom](#)
 - "hyper": m (the number of white balls in the urn), n (the number of black balls in the urn), k (the number of balls drawn from the urn); see [crps_hyper](#)
 - "negative-binomial" or "nbinom": size (positive dispersion parameter), prob (success probability), mu (mean, alternative to prob); see [crps_nbinom](#)
 - "poisson" or "pois": lambda (positive mean); see [crps_pois](#)

All numerical arguments should be of the same length. An exception are scalars of length 1, which will be recycled.

Value

Vector of score values. *A lower score indicates a better forecast.*

Author(s)

Alexander Jordan, Fabian Krueger, Sebastian Lerch

References

Closed form expressions of the CRPS for specific distributions:

Baran, S. and S. Lerch (2015): ‘Log-normal distribution based Ensemble Model Output Statistics models for probabilistic wind-speed forecasting’, Quarterly Journal of the Royal Meteorological Society 141, 2289-2299. doi: [10.1002/qj.2521](https://doi.org/10.1002/qj.2521) (*Log-normal*)

Friederichs, P. and T.L. Thorarinsdottir (2012): ‘Forecast verification for extreme value distributions with an application to probabilistic peak wind prediction’, Environmetrics 23, 579-594. doi: [10.1002/env.2176](https://doi.org/10.1002/env.2176) (*Generalized Extreme Value, Generalized Pareto*)

Gneiting, T., Larson, K., Westvelt III, A.H. and T. Goldman (2005): ‘Calibrated probabilistic forecasting using ensemble model output statistics and minimum CRPS estimation’, Monthly Weather Review 133, 1098-1118. doi: [10.1175/mwr2904.1](https://doi.org/10.1175/mwr2904.1) (*Normal*)

Gneiting, T., Larson, K., Westrick, K., Genton, M.G. and E. Aldrich (2006): ‘Calibrated probabilistic forecasting at the stateline wind energy center: The regime-switching space-time method’, Journal of the American Statistical Association 101, 968-979. doi: [10.1198/016214506000000456](https://doi.org/10.1198/016214506000000456) (*Censored normal*)

Gneiting, T. and T.L. Thorarinsdottir (2010): ‘Predicting inflation: Professional experts versus no-change forecasts’, arXiv preprint arXiv:1010.2318. (*Two-piece normal*)

Grimm, E.P., Gneiting, T., Berrocal, V.J. and N.A. Johnson (2006): ‘The continuous ranked probability score for circular variables and its application to mesoscale forecast ensemble verification’, Quarterly Journal of the Royal Meteorological Society 132, 2925-2942. doi: [10.1256/qj.05.235](https://doi.org/10.1256/qj.05.235) (*Mixture of normals*)

Scheuerer, M. and D. Moeller (2015): ‘Probabilistic wind speed forecasting on a grid based on ensemble model output statistics’, Annals of Applied Statistics 9, 1328-1349. doi: [10.1214/15-aos843](https://doi.org/10.1214/15-aos843) (*Gamma*)

Thorarinsdottir, T.L. and T. Gneiting (2010): ‘Probabilistic forecasts of wind speed: ensemble model output statistics by using heteroscedastic censored regression’, Journal of the Royal Statistical Society (Series A) 173, 371-388. doi: [10.1111/j.1467985x.2009.00616.x](https://doi.org/10.1111/j.1467985x.2009.00616.x) (*Truncated normal*)

Wei, W. and L. Held (2014): ‘Calibration tests for count data’, TEST 23, 787-205. doi: [10.1007/s1174901403808](https://doi.org/10.1007/s1174901403808) (*Poisson, Negative Binomial*)

Independent listing of closed-form solutions for the CRPS:

Taillardat, M., Mestre, O., Zamo, M. and P. Naveau (2016): ‘Calibrated ensemble forecasts using quantile regression forests and ensemble model output statistics’, Monthly Weather Review 144, 2375-2393. doi: [10.1175/mwr150260.1](https://doi.org/10.1175/mwr150260.1)

See Also

[logs.numeric](#)

Examples

```
crps(y = 1, family = "normal", mean = 0, sd = 2)
crps(y = rnorm(20), family = "normal", mean = 1:20, sd = sqrt(1:20))

## Arguments can have different lengths:
crps(y = rnorm(20), family = "normal", mean = 0, sd = 2)
crps(y = 1, family = "normal", mean = 1:20, sd = sqrt(1:20))

## Mixture of normal distributions requires matrix input for parameters:
mval <- matrix(rnorm(20*50), nrow = 20)
sdval <- matrix(runif(20*50, min = 0, max = 2), nrow = 20)
weights <- matrix(rep(1/50, 20*50), nrow = 20)
crps(y = rnorm(20), family = "mixnorm", m = mval, s = sdval, w = weights)
```

GDP data

Data and forecasts for US GDP growth

Description

Historical data and forecast distributions for the growth rate of US gross domestic product (GDP). The forecasts are generated from a Bayesian Markov Switching model as described in Section 5 of Krueger et al (2020).

Format

`gdp` is a data frame which contains the real-time data set used in Section 5 of KLTG (2020), with the following columns:

- `dt` - date in question (e.g., "2013Q2" for the second quarter of 2013)
- `vint` - data vintage (i.e., the date at which the realization was recorded); same format as `dt`
- `val` - value of the GDP growth rate

`gdp_mcmc` is a list, whereby each element is a data frame. `gdp_mcmc$forecasts` contains the simulated forecast distributions. There are 20 columns (corresponding to quarters 2008:Q1 to 2012:Q4) and 5.000 rows (corresponding to simulation draws). `gdp_mcmc$actuals` contains the actual observations. There are 20 columns (again corresponding to quarterly dates) and a single row.

Details

The realizations in `gdp_mcmc$actuals` are also contained in `gdp`, based on the second available vintage for each date. For example, `gdp_mcmc$actuals$X2008Q1` is the entry in `gdp` for which `dt == "2008Q1"` and `vint == "2008Q3"`.

Source

The GDP growth rate is computed from real-time data provided by the Federal Reserve Bank of Philadelphia, <https://www.phil.frb.org/research-and-data/real-time-center/> (series code “ROUTPUT”, second-vintage data). The same data also enters the model which is used to generate the forecast distribution. *Disclaimer: The provider of the raw data takes no responsibility for the accuracy of the data posted here. Furthermore, the raw data may be revised over time, and the website linked above should be consulted for the official, most recent version.*

The model from which the forecast draws are generated is described in Section 5 of KLTG (2020). Forecasts are one quarter ahead (that is, they are based on data until the previous quarter).

References

Krueger, F., Lerch, S., Thorarinsdottir, T.L. and T. Gneiting (2020): ‘Predictive inference based on Markov chain Monte Carlo output’, *International Statistical Review*, forthcoming. doi: [10.1111/insr.12405](https://doi.org/10.1111/insr.12405)

Examples

```
## Not run:

# Load data
data(gdp_mcmc)

# Histogram of forecast draws for 2012Q4
fc_draws <- gdp_mcmc$forecasts[, "X2012Q4"]
hist(fc_draws, main = "Forecast draws for 2012:Q4", xlab = "Value")

# Add vertical line at realizing value
rlz <- gdp_mcmc$actuals[, "X2012Q4"]
abline(v = rlz, lwd = 3)

# Compute CRPS for this forecast case
crps_sample(y = rlz, dat = fc_draws)

## End(Not run)
```

logs.numeric

Logarithmic Score for Parametric Forecast Distributions

Description

Calculate the logarithmic score (LogS) given observations and parameters of a family of distributions.

Usage

```
## S3 method for class 'numeric'
logs(y, family, ...)
```

Arguments

y	Vector of realized values.
family	String which specifies the parametric family; current options: "2pexp", "2pnorm", "beta", "binom", "ex
...	Vectors of parameter values; expected input depends on the chosen family. See details below.

Details

The parameters supplied to each of the functions are numeric vectors:

1. Distributions defined on the real line:
 - "laplace" or "lapl": location (real-valued location parameter), scale (positive scale parameter); see [logs_lapl](#)
 - "logistic" or "logis": location (real-valued location parameter), scale (positive scale parameter); see [logs_logis](#)
 - "normal" or "norm": mean, sd (mean and standard deviation); see [logs_norm](#)
 - "normal-mixture" or "mixture-normal" or "mixnorm": m (mean parameters), s (standard deviations), w (weights); see [logs_mixnorm](#); note: matrix-input for parameters
 - "t": df (degrees of freedom), location (real-valued location parameter), scale (positive scale parameter); see [logs_t](#)
 - "two-piece-exponential" or "2pexp": location (real-valued location parameter), scale1, scale2 (positive scale parameters); see [logs_2pexp](#)
 - "two-piece-normal" or "2pnorm": location (real-valued location parameter), scale1, scale2 (positive scale parameters); see [logs_2pnorm](#)
2. Distributions for non-negative random variables:
 - "exponential" or "exp": rate (positive rate parameter); see [logs_exp](#)
 - "gamma": shape (positive shape parameter), rate (positive rate parameter), scale (alternative to rate); see [logs_gamma](#)
 - "log-laplace" or "llapl": locationlog (real-valued location parameter), scalelog (positive scale parameter); see [logs_llapl](#)
 - "log-logistic" or "llogis": locationlog (real-valued location parameter), scalelog (positive scale parameter); see [logs_llogis](#)
 - "log-normal" or "lnorm": locationlog (real-valued location parameter), scalelog (positive scale parameter); see [logs_lnorm](#)
3. Distributions with flexible support and/or point masses:
 - "beta": shape1, shape2 (positive shape parameters), lower, upper (lower and upper limits); see [logs_beta](#)
 - "uniform" or "unif": min, max (lower and upper limits); see [logs_unif](#)
 - "exp2": location (real-valued location parameter), scale (positive scale parameter); see [logs_exp2](#)
 - "gev": location (real-valued location parameter), scale (positive scale parameter), shape (real-valued shape parameter); see [logs_gev](#)
 - "gpd": location (real-valued location parameter), scale (positive scale parameter), shape (real-valued shape parameter); see [logs_gpd](#)

- "tlogis": location (location parameter), scale (scale parameter), lower, upper (lower and upper limits); see [logs_tlogis](#)
 - "tnorm": location (location parameter), scale (scale parameter), lower, upper (lower and upper limits); see [logs_tnorm](#)
 - "tt": df (degrees of freedom), location (location parameter), scale (scale parameter), lower, upper (lower and upper limits); see [logs_tt](#)
4. Distributions of discrete variables:
- "binom": size (number of trials (zero or more)), prob (probability of success on each trial); see [crps_binom](#)
 - "hyper": m (the number of white balls in the urn), n (the number of black balls in the urn), k (the number of balls drawn from the urn); see [crps_hyper](#)
 - "negative-binomial" or "nbinom": size (positive dispersion parameter), prob (success probability), mu (mean, alternative to prob); see [logs_nbinom](#)
 - "poisson" or "pois": lambda (positive mean); see [logs_pois](#)

All numerical arguments should be of the same length. An exception are scalars of length 1, which will be recycled.

Value

Vector of score values. *A lower score indicates a better forecast.*

Author(s)

Alexander Jordan, Fabian Krueger, Sebastian Lerch

See Also

[crps.numeric](#)

Examples

```
logs(y = 1, family = "normal", mean = 0, sd = 2)
logs(y = rnorm(20), family = "normal", mean = 1:20, sd = sqrt(1:20))

## Arguments can have different lengths:
logs(y = rnorm(20), family = "normal", mean = 0, sd = 2)
logs(y = 1, family = "normal", mean = 1:20, sd = sqrt(1:20))

## Mixture of normal distributions requires matrix input for parameters:
mval <- matrix(rnorm(20*50), nrow = 20)
sdval <- matrix(runif(20*50, min = 0, max = 2), nrow = 20)
weights <- matrix(rep(1/50, 20*50), nrow = 20)
logs(y = rnorm(20), family = "mixnorm", m = mval, s = sdval, w = weights)
```

plot.casestudy *Plot the output of run_casestudy*

Description

Plot the output of run_casestudy

Usage

```
## S3 method for class 'casestudy'  
plot(x, ...)
```

Arguments

x object of class casestudy, generated by [run_casestudy](#)
... additional parameters, see details below.

Details

The plot is in the same format as Figure 3 in KLTG (2020). Its content (nr of MCMC chains, maximal sample size, etc) depends on the parameters used to generate [run_casestudy](#). In terms of additional inputs (...), the following are currently implemented:

- `scoring_rule`, the scoring rule for which results are to be plotted, either "crps" or "logs". Defaults to "crps".
- `add_main_title`, logical, whether to add main title to plot. Defaults to TRUE.

Value

none, used for the effect of drawing a plot.

Author(s)

Fabian Krueger

References

Krueger, F., Lerch, S., Thorarinsdottir, T.L. and T. Gneiting (2020): 'Predictive inference based on Markov chain Monte Carlo output', *International Statistical Review*, forthcoming. doi: [10.1111/insr.12405](https://doi.org/10.1111/insr.12405)

See Also

[run_casestudy](#) produces the forecast results summarized by [plot.casestudy](#)

plot.mcstudy	<i>Plot the output of run_mcstudy</i>
--------------	---------------------------------------

Description

Plot the output of run_mcstudy

Usage

```
## S3 method for class 'mcstudy'  
plot(x, ...)
```

Arguments

x	object of class mcstudy, generated by run_mcstudy
...	additional parameters, see details below.

Details

The plot is in the same format as Figure 1 or 2 in KLTG (2020), depending on the parameters set when running [run_mcstudy](#). These parameters also determine the plot content (nr of MCMC chains, maximal sample size, etc). In terms of additional inputs (. . .), the following are currently implemented:

- scoring_rule, the scoring rule for which results are to be plotted, either "crps" or "logs". Defaults to "crps".
- add_main_title, logical, whether to add main title to plot. Defaults to TRUE.

Value

none, used for the effect of drawing a plot.

Author(s)

Fabian Krueger

References

Krueger, F., Lerch, S., Thorarinsdottir, T.L. and T. Gneiting (2020): 'Predictive inference based on Markov chain Monte Carlo output', *International Statistical Review*, forthcoming. doi: [10.1111/insr.12405](https://doi.org/10.1111/insr.12405)

See Also

[run_mcstudy](#) produces the simulation results summarized by [plot.mcstudy](#)

print.casestudy *Simple print method for object of class casestudy*

Description

Simple print method for object of class casestudy

Usage

```
## S3 method for class 'casestudy'  
print(x, ...)
```

Arguments

x Object of class casestudy, generated via [run_casestudy](#)
... Additional specifications (presently not in use)

print.mcstudy *Simple print function for object of class mcstudy*

Description

Simple print function for object of class mcstudy

Usage

```
## S3 method for class 'mcstudy'  
print(x, ...)
```

Arguments

x Object of class mcstudy, generated via [run_mcstudy](#)
... Additional specifications (presently not in use)

run_casestudy	<i>Run the case study in KLTG (2020), or a smaller version thereof</i>
---------------	--

Description

Run the case study in KLTG (2020), or a smaller version thereof

Usage

```
run_casestudy(
  data_df,
  burnin_size = 5000,
  max_mcmc_sample_size = 5000,
  nr_of_chains = 3,
  first_vint = "1996Q2",
  last_vint = "2014Q3",
  forecast_horizon = 1,
  random_seed = 816
)
```

Arguments

data_df	data frame in the same format as the gdp data set in this package.
burnin_size	length of the burn-in period used for each forecast.
max_mcmc_sample_size	maximal number of MCMC draws to consider (integer, must equal either 1000, 5000, 10000, 20000 or 40000). Defaults to 5000.
nr_of_chains	number of parallel MCMC for each forecast date (integer, defaults to 3).
first_vint, last_vint	first and last data vintage (= time point at which forecasts are made). Default to "1996Q2" and "2014Q3", respectively.
forecast_horizon	forecast horizon to be analyzed (integer, defaults to 1).
random_seed	seed for random numbers used during the MCMC sampling process. Defaults to 816.

Details

The full results in Section 5 of KLTG (2020) are based on the following setup: `burnin_size = 10000`, `max_mcmc_sample_size = 50000`, `nr_of_chains = 16`, `data_df = gdp`, `first_vint = "1996Q2"`, `last_vint = "2014Q3"`, and `forecast_horizon = 1`. Since running this full configuration is very time consuming, the default setup offers the possibility to run a small-scale study which reproduces the qualitative outcomes of the analysis. Running the small-scale study implied by the defaults of `run_study` as well as the GDP data (`data_df = gdp`) takes about 40 minutes on an Intel i7 processor.

Value

Object of class "casestudy", containing the results of the analysis. This object can be passed to `plot` for plotting, see the documentation for [plot.casestudy](#).

Author(s)

Fabian Krueger

References

Krueger, F., Lerch, S., Thorarinsdottir, T.L. and T. Gneiting (2020): ‘Predictive inference based on Markov chain Monte Carlo output’, *International Statistical Review*, forthcoming. doi: [10.1111/insr.12405](https://doi.org/10.1111/insr.12405)

See Also

[plot.casestudy](#) produces a summary plot of the results generated by `run_casestudy` `run_casestudy` uses `ar_ms` to fit a Bayesian Markov Switching model, recursively for several time periods.

Examples

```
## Not run:
data(gdp)
cs <- run_casestudy(data_df = gdp, last_vint = "1999Q4")
plot(cs)

## End(Not run)
```

run_mcstudy

Run the Monte Carlo study by KLTG (2020), or a smaller version thereof

Description

Run the Monte Carlo study by KLTG (2020), or a smaller version thereof

Usage

```
run_mcstudy(
  s = 2,
  a = 0.5,
  n = 12,
  nr_iterations = 50,
  zoom = FALSE,
  random_seed = 816
)
```


Arguments

<code>s, a, n</code>	parameters characterizing the process from which data are simulated (see Section 4 and Table 4 of KLTG, 2019). Defaults to the values reported in the main text of the paper.
<code>nr_iterations</code>	number of Monte Carlo iterations (defaults to 50).
<code>zoom</code>	set to TRUE to produce results for a fine grid of small (MCMC) sample sizes, as in Figure 2 of KLTG (2020).
<code>random_seed</code>	seed used for running the simulation experiment. Defaults to 816.

Details

The full results in Section 4 of KLTG (2020) are based on $s = 2$, $a = 0.5$, $n = 12$ and `nr_iterations = 1000`. Producing these results takes about 140 minutes on an Intel i7 processor.

Value

Object of class "mstudy", containing the results of the analysis. This object can be passed to `plot` for plotting, see the documentation for [plot.mstudy](#).

Author(s)

Fabian Krueger

References

Krueger, F., Lerch, S., Thorarinsdottir, T.L. and T. Gneiting (2020): 'Predictive inference based on Markov chain Monte Carlo output', *International Statistical Review*, forthcoming. doi: [10.1111/insr.12405](https://doi.org/10.1111/insr.12405)

See Also

[plot.mstudy](#) produces a summary plot of the results generated by [run_mstudy](#)

scores

Generic Scoring Rule Calculation

Description

Generic functions for calculating the Continuous Ranked Probability Score and the Logarithmic Score of R objects.

`scoringRules` provides default methods ([crps.numeric](#), [logs.numeric](#)) to calculate scores of forecasts that are members of families of parametric distributions.

Usage

```
crps(y, ...)
```

```
logs(y, ...)
```

Arguments

`y` an object for which the score is to be calculated
`...` further arguments passed to or from other methods

Details

The mean logarithmic score corresponds to the negative of the log-likelihood [logLik](#).

Value

Returns a vector of scores. One for each forecast-observation pair.

References

General background and further references on scoring rules:

Gneiting, T. and A.E. Raftery (2007): ‘Strictly proper scoring rules, prediction and estimation’, *Journal of the American Statistical Association* 102, 359-378. doi: [10.1198/016214506000001437](#)

Gneiting, T. and M. Katzfuss (2014): ‘Probabilistic forecasting’, *Annual Review of Statistics and Its Application* 1, 125-151. doi: [10.1146/annurevstatistics062713085831](#)

See Also

[crps.numeric](#), [logs.numeric](#)

scores_2pexp

Calculating scores for the two-piece-exponential distribution

Description

Calculating scores for the two-piece-exponential distribution

Usage

```
crps_2pexp(y, scale1, scale2, location = 0)
```

```
logs_2pexp(y, scale1, scale2, location = 0)
```

Arguments

`y` vector of observations.
`scale1, scale2` vectors of positive scale parameters.
`location` vector of location parameters.

Value

A vector of score values.

scores_2pnorm	<i>Calculating scores for the two-piece-normal distribution</i>
---------------	---

Description

Calculating scores for the two-piece-normal distribution

Usage

```
crps_2pnorm(y, scale1, scale2, location = 0)
```

```
logs_2pnorm(y, scale1, scale2, location = 0)
```

Arguments

y vector of observations.
 scale1, scale2 vectors of positive scale parameters.
 location vector of location parameters.

Value

A vector of score values.

scores_beta	<i>Calculating scores for the beta distribution</i>
-------------	---

Description

Calculating scores for the beta distribution

Usage

```
crps_beta(y, shape1, shape2, lower = 0, upper = 1)
```

```
logs_beta(y, shape1, shape2, lower = 0, upper = 1)
```

```
dss_beta(y, shape1, shape2, lower = 0, upper = 1)
```

Arguments

y vector of observations.
 shape1, shape2 vectors of positive shape parameters.
 lower, upper vectors of lower and upper limits of the distribution. Must be finite.

Value

A vector of score values.

scores_binom	<i>Calculating scores for the binomial distribution</i>
--------------	---

Description

Calculating scores for the binomial distribution

Usage

```
crps_binom(y, size, prob)
```

```
logs_binom(y, size, prob)
```

Arguments

y	vector of observations.
size	number of trials (zero or more).
prob	probability of success on each trial.

Value

A vector of score values.

scores_exp	<i>Calculating scores for the exponential distribution</i>
------------	--

Description

Calculating scores (CRPS, LogS, DSS) for the exponential distribution, and the exponential distribution with location-scale transformation and point mass in location.

Usage

```
crps_exp(y, rate = 1)
```

```
crps_expM(y, location = 0, scale = 1, mass = 0)
```

```
logs_exp(y, rate = 1)
```

```
logs_exp2(y, location = 0, scale = 1)
```

```
dss_exp(y, rate = 1)
```

Arguments

y	vector of observations.
rate	vector of rates.
location	vector of location parameters.
scale	vector of positive scale parameters.
mass	vector of point masses in location.

Value

A vector of score values.

scores_gamma	<i>Calculating scores for the gamma distribution</i>
--------------	--

Description

Calculating scores for the gamma distribution

Usage

```
crps_gamma(y, shape, rate = 1, scale = 1/rate)
```

```
logs_gamma(y, shape, rate = 1, scale = 1/rate)
```

```
dss_gamma(y, shape, rate = 1, scale = 1/rate)
```

Arguments

y	vector of observations.
shape	vector of positive shape parameters.
rate	an alternative way to specify the scale.
scale	vector of positive scale parameters.

Value

A vector of score values.

`scores_gev`*Calculating scores for the generalized extreme value distribution*

Description

Calculating scores for the generalized extreme value distribution

Usage

```
crps_gev(y, shape, location = 0, scale = 1)
```

```
logs_gev(y, shape, location = 0, scale = 1)
```

```
dss_gev(y, shape, location = 0, scale = 1)
```

Arguments

<code>y</code>	vector of observations.
<code>shape</code>	vector of positive shape parameters.
<code>location</code>	vector of location parameters.
<code>scale</code>	vector of positive scale parameters.

Value

A vector of score values.

`scores_gpd`*Calculating scores for the generalized Pareto distribution*

Description

Calculating scores for the generalized Pareto distribution

Usage

```
crps_gpd(y, shape, location = 0, scale = 1, mass = 0)
```

```
logs_gpd(y, shape, location = 0, scale = 1)
```

```
dss_gpd(y, shape, location = 0, scale = 1)
```

Arguments

y	vector of observations.
shape	vector of positive shape parameters.
location	vector of location parameters.
scale	vector of positive scale parameters.
mass	vector of point masses in location.

Value

A vector of score values.

scores_hyper	<i>Calculating scores for the hypergeometric distribution</i>
--------------	---

Description

Calculating scores for the hypergeometric distribution

Usage

```
crps_hyper(y, m, n, k)
```

```
logs_hyper(y, m, n, k)
```

Arguments

y	vector of observations / numbers of white balls drawn without replacement from an urn which contains both black and white balls.
m	the number of white balls in the urn.
n	the number of black balls in the urn.
k	the number of balls drawn from the urn, hence must be in $0, 1, \dots, m + n$.

Value

A vector of score values.

scores_lapl *Calculating scores for the Laplace distribution*

Description

Calculating scores for the Laplace distribution

Usage

```
crps_lapl(y, location = 0, scale = 1)
```

```
logs_lapl(y, location = 0, scale = 1)
```

```
dss_lapl(y, location = 0, scale = 1)
```

Arguments

y vector of observations.
location vector of location parameters.
scale vector of positive scale parameters.

Value

A vector of score values.

scores_llapl *Calculating scores for the log-Laplace distribution*

Description

Calculating scores for the log-Laplace distribution

Usage

```
crps_llapl(y, locationlog, scalelog)
```

```
logs_llapl(y, locationlog, scalelog)
```

```
dss_llapl(y, locationlog, scalelog)
```

Arguments

y vector of observations.
locationlog vector of location parameters on the log scale.
scalelog vector of positive scale parameters on the log scale.

Value

A vector of score values.

scores_llogis	<i>Calculating scores for the log-logistic distribution</i>
---------------	---

Description

Calculating scores for the log-logistic distribution

Usage

```
crps_llogis(y, locationlog, scalelog)
```

```
logs_llogis(y, locationlog, scalelog)
```

```
dss_llogis(y, locationlog, scalelog)
```

Arguments

y vector of observations.
locationlog vector of location parameters on the log scale.
scalelog vector of positive scale parameters on the log scale.

Value

A vector of score values.

scores_lnorm	<i>Calculating scores for the log-normal distribution</i>
--------------	---

Description

Calculating scores for the log-normal distribution

Usage

```
crps_lnorm(y, meanlog = 0, sdlog = 1, locationlog = meanlog, scalelog = sdlog)
```

```
logs_lnorm(y, meanlog = 0, sdlog = 1, locationlog = meanlog, scalelog = sdlog)
```

```
dss_lnorm(y, meanlog = 0, sdlog = 1, locationlog = meanlog, scalelog = sdlog)
```

Arguments

y	vector of observations.
meanlog	an alternative way to specify locationlog.
sdlog	an alternative way to specify scalelog.
locationlog	vector of location parameters on the log scale.
scalelog	vector of positive scale parameters on the log scale.

Value

A vector of score values.

scores_logis	<i>Calculating scores for the logistic distribution</i>
--------------	---

Description

These functions calculate scores (CRPS, logarithmic score) and its gradient and Hessian with respect to the parameters of a location-scale transformed logistic distribution. Furthermore, the censoring transformation and the truncation transformation may be introduced on top of the location-scale transformed logistic distribution.

Usage

```
## score functions
crps_logis(y, location = 0, scale = 1)
crps_clogis(y, location = 0, scale = 1, lower = -Inf, upper = Inf)
crps_tlogis(y, location = 0, scale = 1, lower = -Inf, upper = Inf)
crps_gtclogis(y, location = 0, scale = 1, lower = -Inf, upper = Inf, lmass = 0, umass = 0)
logs_logis(y, location = 0, scale = 1)
logs_tlogis(y, location = 0, scale = 1, lower = -Inf, upper = Inf)
dss_logis(y, location = 0, scale = 1)

## gradient (location, scale) functions
gradcrps_logis(y, location = 0, scale = 1)
gradcrps_clogis(y, location = 0, scale = 1, lower = -Inf, upper = Inf)
gradcrps_tlogis(y, location = 0, scale = 1, lower = -Inf, upper = Inf)

## Hessian (location, scale) functions
hesscrps_logis(y, location = 0, scale = 1)
hesscrps_clogis(y, location = 0, scale = 1, lower = -Inf, upper = Inf)
hesscrps_tlogis(y, location = 0, scale = 1, lower = -Inf, upper = Inf)
```

Arguments

y	vector of observations.
location	vector of location parameters.
scale	vector of scale parameters.
lower, upper	lower and upper truncation/censoring bounds.
lmass, umass	vectors of point masses in lower and upper respectively.

Value

For the score functions: a vector of score values.

For the gradient and Hessian functions: a matrix with column names corresponding to the respective partial derivatives.

scores_mixnorm	<i>Calculating scores for a mixture of normal distributions.</i>
----------------	--

Description

Calculating scores for a mixture of normal distributions.

Usage

```
crps_mixnorm(y, m, s, w = NULL)
crps_mixnorm_int(y, m, s, w = NULL, rel_tol = 1e-06)
logs_mixnorm(y, m, s, w = NULL)
dss_mixnorm(y, m, s, w = NULL)
```

Arguments

y	vector of observations.
m	matrix of mean parameters; rows represent observations, columns represent mixture components.
s	matrix of scale parameters; same structure as m.
w	optional; matrix of non-negative weights; same structure as m.
rel_tol	relative accuracy for numerical integration.

Details

logs_mixnorm and crps_mixnorm calculate scores via analytical formulas. crps_mixnorm_int uses numerical integration for the CRPS; this can be faster if there are many mixture components (i.e., if m, s and w have many columns). See examples below.

Value

A vector of score values.

Examples

```
# Example 1: 100 observations, 15 mixture components
mval <- matrix(rnorm(100*15), nrow = 100)
sdval <- matrix(rgamma(100*15, shape = 2), nrow = 100)
weights <- matrix(rep(1/15, 100*15), nrow = 100)
y <- rnorm(100)
crps1 <- crps_mixnorm(y = y, m = mval, s = sdval, w = weights)
crps2 <- crps_mixnorm_int(y = y, m = mval, s = sdval, w = weights)

## Not run:
# Example 2: 2 observations, 10000 mixture components
mval <- matrix(rnorm(2*10000), nrow = 2)
sdval <- matrix(rgamma(2*10000, shape = 2), nrow = 2)
weights <- matrix(rep(1/10000, 2*10000), nrow = 2)
y <- rnorm(2)
# With many mixture components, numerical integration is much faster
system.time(crps1 <- crps_mixnorm(y = y, m = mval, s = sdval, w = weights))
system.time(crps2 <- crps_mixnorm_int(y = y, m = mval, s = sdval, w = weights))

## End(Not run)
```

scores_moments

Scoring Rules for a Vector of Moments

Description

Calculate scores (DSS, ESS) given observations and moments of the predictive distributions.

Usage

```
dss_moments(y, mean = 0, var = 1)
```

```
ess_moments(y, mean = 0, var = 1, skew = 0)
```

Arguments

y	vector of realized values.
mean	vector of mean values.
var	vector of variance values.
skew	vector of skewness values.

Details

The skewness of a random variable X is the third standardized moment

$$E\left[\left(\frac{X - \text{mean}}{\sqrt{\text{var}}}\right)^3\right].$$

Value

Value of the score. *A lower score indicates a better forecast.*

Author(s)

Alexander Jordan, Sebastian Lerch

References

Dawid-Sebastiani score:

Dawid, A.P. and P. Sebastiani (1999): 'Coherent dispersion criteria for optimal experimental design' *The Annals of Statistics*, 27, 65-81. doi: [10.1214/aos/1018031101](https://doi.org/10.1214/aos/1018031101)

Error-spread score:

Christensen, H.M., I.M. Moroz, and T.N. Palmer (2015): 'Evaluation of ensemble forecast uncertainty using a new proper score: Application to medium-range and seasonal forecasts', *Quarterly Journal of the Royal Meteorological Society*, 141, 538-549. doi: [10.1002/qj.2375](https://doi.org/10.1002/qj.2375)

scores_nbinom

Calculating scores for the negative binomial distribution

Description

Calculating scores for the negative binomial distribution

Usage

crps_nbinom(y, size, prob, mu)

logs_nbinom(y, size, prob, mu)

dss_nbinom(y, size, prob, mu)

Arguments

y	vector of observations.
size	target for number of successful trials, or dispersion parameter (the shape parameter of the gamma mixing distribution). Must be strictly positive, need not be integer.
prob	probability of success in each trial. $0 < \text{prob} \leq 1$.
mu	alternative parametrization via mean: see 'Details'.

Details

The mean of the negative binomial distribution is given by $\mu = \text{size} \cdot (1 - \text{prob}) / \text{prob}$.

Value

A vector of score values.

scores_norm

Calculating scores for the normal distribution

Description

These functions calculate scores (CRPS, LogS, DSS) and their gradient and Hessian with respect to the parameters of a location-scale transformed normal distribution. Furthermore, the censoring transformation and the truncation transformation may be introduced on top of the location-scale transformed normal distribution.

Usage

```
## score functions
crps_norm(y, mean = 0, sd = 1, location = mean, scale = sd)
crps_cnorm(y, location = 0, scale = 1, lower = -Inf, upper = Inf)
crps_tnorm(y, location = 0, scale = 1, lower = -Inf, upper = Inf)
crps_gtcnorm(y, location = 0, scale = 1, lower = -Inf, upper = Inf, lmass = 0, umass = 0)
logs_norm(y, mean = 0, sd = 1, location = mean, scale = sd)
logs_tnorm(y, location = 0, scale = 1, lower = -Inf, upper = Inf)
dss_norm(y, mean = 0, sd = 1, location = mean, scale = sd)

## gradient (location, scale) functions
gradcrps_norm(y, location = 0, scale = 1)
gradcrps_cnorm(y, location = 0, scale = 1, lower = -Inf, upper = Inf)
gradcrps_tnorm(y, location = 0, scale = 1, lower = -Inf, upper = Inf)

## Hessian (location, scale) functions
hesscrps_norm(y, location = 0, scale = 1)
hesscrps_cnorm(y, location = 0, scale = 1, lower = -Inf, upper = Inf)
hesscrps_tnorm(y, location = 0, scale = 1, lower = -Inf, upper = Inf)
```

Arguments

y	vector of observations.
mean	an alternative way to specify location.
sd	an alternative way to specify scale.
location	vector of location parameters.
scale	vector of scale parameters.
lower, upper	lower and upper truncation/censoring bounds.
lmass, umass	vectors of point masses in lower and upper respectively.

Value

For the score functions: a vector of score values.

For the gradient and Hessian functions: a matrix with column names corresponding to the respective partial derivatives.

scores_pois	<i>Calculating scores for the Poisson distribution</i>
-------------	--

Description

Calculating scores for the Poisson distribution

Usage

```
crps_pois(y, lambda)
```

```
logs_pois(y, lambda)
```

```
dss_pois(y, lambda)
```

Arguments

`y` vector of observations.

`lambda` vector of (non-negative) means.

Value

A vector of score values.

scores_sample_multiv	<i>Multivariate Scoring Rules for Simulated Forecast Distributions</i>
----------------------	--

Description

Compute multivariate scores of the form $S(y, dat)$, where S is a proper scoring rule, y is a d -dimensional realization vector and dat is a simulated sample of multivariate forecasts. Available are the energy score and the variogram score of order p .

Usage

```
es_sample(y, dat)
```

```
vs_sample(y, dat, w = NULL, p = 0.5)
```

Arguments

y	realized values (numeric vector of length d).
dat	numeric matrix of data (columns are simulation draws from multivariate forecast distribution).
w	numeric matrix of weights for dat used in the variogram score. If no weights are specified, constant weights with $w = 1$ are used.
p	order of variogram score. Standard choices include $p = 1$ and $p = 0.5$.

Details

In the input matrix `dat` each column is expected to represent a sample from the multivariate forecast distribution, the number of rows of `dat` thus has to match the length of the observation vector `y`, and the number of columns of `dat` is the number of simulated samples.

In [vs_sample](#) it is possible to specify a matrix `w` of non-negative weights that allow to emphasize or downweight pairs of component combinations based on subjective expert decisions. `w` is a square matrix with dimensions equal to the length of the input vector `y`, and the entry in the i -th row and j -th column of `w` corresponds to the weight assigned to the combination of the corresponding i -th and j -th component. For details and examples, see Scheuerer and Hamill (2015).

Value

Value of the score. *A lower score indicates a better forecast.*

Author(s)

Maximiliane Graeter, Sebastian Lerch, Fabian Krueger

References*Energy score*

Gneiting, T., Stanberry, L.I., Grimit, E.P., Held, L. and N.A. Johnson (2008): ‘Assessing probabilistic forecasts of multivariate quantities, with an application to ensemble predictions of surface winds’, *TEST*, 17, 211-235. doi: [10.1007/s117490080114x](https://doi.org/10.1007/s117490080114x)

Variogram-based proper scoring rules

Scheuerer, M. and T.M. Hamill (2015): ‘Variogram-based proper scoring rules for probabilistic forecasts of multivariate quantities’, *Monthly Weather Review*, 143, 1321-1334. doi: [10.1175/mwr-d1400269.1](https://doi.org/10.1175/mwr-d1400269.1)

Examples

```
d <- 10 # number of dimensions
m <- 50 # number of samples from multivariate forecast distribution

mu0 <- rep(0, d)
mu <- rep(1, d)
S0 <- S <- diag(d)
S[S==0] <- 0.1
```



```

S0[S0==0] <- 0.2

# generate samples from multivariate normal distributions
obs <- drop(mu0 + rnorm(d) %*% chol(S0))
fc_sample <- replicate(m, drop(mu + rnorm(d) %*% chol(S)))

es_sample(y = obs, dat = fc_sample)

# weighting matrix for variogram score
w_vs <- matrix(NA, nrow = d, ncol = d)
for(d1 in 1:d){for(d2 in 1:d){w_vs[d1,d2] <- 0.5^abs(d1-d2)}}

vs_sample(y = obs, dat = fc_sample)
vs_sample(y = obs, dat = fc_sample, w = w_vs)
vs_sample(y = obs, dat = fc_sample, w = w_vs, p = 1)

```

scores_sample_univ *Scoring Rules for Simulated Forecast Distributions*

Description

Calculate scores (CRPS, LogS, DSS) given observations and draws from the predictive distributions.

Usage

```

crps_sample(
  y,
  dat,
  method = "edf",
  w = NULL,
  bw = NULL,
  num_int = FALSE,
  show_messages = TRUE
)

logs_sample(y, dat, bw = NULL, show_messages = FALSE)

dss_sample(y, dat, w = NULL)

```

Arguments

y	vector of realized values.
dat	vector or matrix (depending on y; see details) of simulation draws from forecast distribution.
method	string; approximation method. Options: "edf" (empirical distribution function) and "kde" (kernel density estimation).

w	optional; vector or matrix (matching dat) of weights for method "edf".
bw	optional; vector (matching y) of bandwidths for kernel density estimation; see details.
num_int	logical; if TRUE numerical integration is used for method "kde".
show_messages	logical; display of messages (does not affect warnings and errors).

Details

For a vector y of length n , `dat` should be given as a matrix with n rows. If y has length 1, then `dat` may be a vector.

`crps_sample` employs an empirical version of the quantile decomposition of the CRPS (Laio and Tamea, 2007) when using `method = "edf"`. For `method = "kde"`, it uses kernel density estimation using a Gaussian kernel. The logarithmic score always uses kernel density estimation.

The bandwidth (`bw`) for kernel density estimation can be specified manually, in which case it must be a positive number. If `bw == NULL`, the bandwidth is selected using the core function `bw.nrd`. Numerical integration may speed up computation for `crps_sample` in case of large samples `dat`.

Value

Value of the score. *A lower score indicates a better forecast.*

Author(s)

Alexander Jordan, Fabian Krueger, Sebastian Lerch

References

Evaluating simulation based forecast distributions:

Krueger, F., Lerch, S., Thorarinsdottir, T.L. and T. Gneiting (2020): ‘Predictive inference based on Markov chain Monte Carlo output’, *International Statistical Review*, forthcoming. doi: [10.1111/insr.12405](https://doi.org/10.1111/insr.12405)

Empirical quantile decomposition of the CRPS:

Laio, F. and S. Tamea (2007): ‘Verification tools for probabilistic forecasts of continuous hydrological variables’, *Hydrology and Earth System Sciences*, 11, 1267-1277. doi: [10.5194/hess111267-2007](https://doi.org/10.5194/hess111267-2007)

Examples

```
## Not run:

# y has length greater than 1
y <- 1:2
sample <- matrix(rnorm(20), nrow = 2)
crps_sample(y = y, dat = sample)
logs_sample(y = y, dat = sample)

y <- 1:2
sample <- rnorm(10)
```

```

crps_sample(y = y, dat = sample) # error

# y has length 1
y <- 1
sample <- rnorm(10)
crps_sample(y = y, dat = sample)

sample <- matrix(rnorm(10), nrow = 1)
crps_sample(y = y, dat = sample)

sample <- matrix(rnorm(20), nrow = 2)
crps_sample(y = y, dat = sample) # error

## End(Not run)

```

scores_t

Calculating scores for Student's t-distribution

Description

These functions calculate scores (CRPS, logarithmic score) and their gradient and Hessian with respect to the parameters of a location-scale transformed Student's t -distribution. Furthermore, the censoring transformation and the truncation transformation may be introduced on top of the location-scale transformed normal distribution.

Usage

```

## score functions
crps_t(y, df, location = 0, scale = 1)
crps_ct(y, df, location = 0, scale = 1, lower = -Inf, upper = Inf)
crps_tt(y, df, location = 0, scale = 1, lower = -Inf, upper = Inf)
crps_gtct(y, df, location = 0, scale = 1, lower = -Inf, upper = Inf, lmass = 0, umass = 0)
logs_t(y, df, location = 0, scale = 1)
logs_tt(y, df, location = 0, scale = 1, lower = -Inf, upper = Inf)
dss_t(y, df, location = 0, scale = 1)

## gradient (location, scale) functions
gradcrps_t(y, df, location = 0, scale = 1)
gradcrps_ct(y, df, location = 0, scale = 1, lower = -Inf, upper = Inf)
gradcrps_tt(y, df, location = 0, scale = 1, lower = -Inf, upper = Inf)

## Hessian (location, scale) functions
hesscrps_t(y, df, location = 0, scale = 1)
hesscrps_ct(y, df, location = 0, scale = 1, lower = -Inf, upper = Inf)
hesscrps_tt(y, df, location = 0, scale = 1, lower = -Inf, upper = Inf)

```

Arguments

y	vector of observations.
df	vector of degrees of freedom.
location	vector of location parameters.
scale	vector of scale paramters.
lower, upper	lower and upper truncation/censoring bounds.
lmass, umass	vectors of point masses in lower and upper respectively.

Value

For the CRPS functions: a vector of score values.

For the gradient and Hessian functions: a matrix with column names corresponding to the respective partial derivatives.

scores_unif	<i>Calculating scores for the uniform distribution</i>
-------------	--

Description

Calculating scores for the uniform distribution

Usage

```
crps_unif(y, min = 0, max = 1, lmass = 0, umass = 0)
```

```
logs_unif(y, min = 0, max = 1)
```

```
dss_unif(y, min = 0, max = 1)
```

Arguments

y	vector of observations.
min, max	lower and upper limits of the distribution. Must be finite.
lmass, umass	vectors of point masses in min and max respectively.

Value

A vector of score values.

summary.casestudy	<i>Summary method for class casestudy</i>
-------------------	---

Description

Summary method for class casestudy

Usage

```
## S3 method for class 'casestudy'  
summary(object, ...)
```

Arguments

object	Object of class casestudy, generated via run_casestudy
...	Additional specifications (presently not in use)

summary.mcstudy	<i>Simple summary method for class mcstudy</i>
-----------------	--

Description

Simple summary method for class mcstudy

Usage

```
## S3 method for class 'mcstudy'  
summary(object, ...)
```

Arguments

object	Object of class mcstudy, generated via run_mcstudy
...	Additional specifications (presently not in use)

Supplementary distributions: Positive real line

Supplementary distributions (not in base R) supported on the positive real line.

Description

We include the probability density functions of some distributions which are part of `scoringRules`, but are not part of base R. The parametrizations used here are identical to the ones used when calling `crps` and `logs`.

Here we document distributions on the positive real line: `fllapl` - log-Laplace distribution; `fllogis` - log-logistic distribution.

Usage

```
fllapl(x, locationlog, scalelog)
fllogis(x, locationlog, scalelog)
```

Arguments

<code>x</code>	vector of quantiles
<code>locationlog</code>	vector of location parameters on the log scale
<code>scalelog</code>	vector of scale parameters on the log scale

Details

To be added.

Value

Probability density function of the relevant distribution, evaluated at `x`.

Author(s)

Alexander Jordan

See Also

The documentation for [crps.numeric](#) contains the full list of distributions supported by `scoringRules` (includes the ones documented here, as well as many others).

Supplementary distributions: Real line

Supplementary distributions (not in base R) supported on the real line.

Description

We include the probability density functions of some distributions which are part of `scoringRules`, but are not part of base R. The parametrizations used here are identical to the ones used when calling `crps` and `logs`.

Here we document distributions with support on the real line: `f1apl` - Laplace distribution; `f2pexp` - two-piece exponential distribution; `fmixnorm` - mixture of normal distributions; `f2pnorm` - two-piece normal distribution.

Usage

```
f1apl(x, location, scale)

f2pexp(x, location, scale1, scale2)
f2pnorm(x, location, scale1, scale2)

fmixnorm(x, m, s, w)
```

Arguments

<code>x</code>	vector of quantiles
<code>location</code>	vector of location parameters
<code>scale, scale1, scale2</code>	vector of scale parameters
<code>m</code>	matrix of means (rows correspond to observations, columns correspond to mixture components)
<code>s</code>	matrix of standard deviations (same structure as <code>m</code>)
<code>w</code>	matrix of weights (same structure as <code>m</code>)

Details

The Laplace distribution (`f1apl`) is described on https://en.wikipedia.org/wiki/Laplace_distribution. It is a special case of the two-piece exponential distribution (`f2pexp`), which allows for different scale parameters to the left and right of `location`.

The density function of a mixture of normal distributions (`fmixnorm`) is given by the weighted sum over the mixture components,

$$f(x) = \sum w_i/s_i \phi((x - m_i)/s_i),$$

where ϕ is the pdf of the standard normal distribution.

For details on the two-piece normal distribution (`f2pnorm`), see Box A of Wallis (2004, "An Assessment of Bank of England and National Institute Inflation Forecast Uncertainties", National Institute Economic Review).

Value

Probability density function of the relevant distribution, evaluated at x .

Author(s)

Alexander Jordan

See Also

The documentation for [crps.numeric](#) contains the full list of distributions supported by `scoringRules` (includes the ones documented here, as well as many others).

[fnorm](#), [flogis](#), [ft](#)

Examples

```
# Plot PDF of Laplace distribution
ff <- function(x) flapl(x, location = 0, scale = 2)
curve(ff, from = -8, to = 8, bty = "n", xlab = "Value",
      ylab = "PDF",
      main = "Laplace distribution with location 0 and scale 2")
```

Supplementary distributions: Variable support

Supplementary distributions (not in base R) with variable support.

Description

We include the probability density functions of some distributions which are part of `scoringRules`, but are not part of base R. The parametrizations used here are identical to the ones used when calling `crps` and `logs`.

Here we document distributions with variable support: `fexp` - location-scale exponential distribution with a point mass on the lower boundary; `fgdp` - generalized Pareto distribution with a point mass on the lower boundary; `fgev` - generalized extreme value distribution; `fnorm`, `flogis`, `ft` - (normal/logistic/Student's t)-distribution with flexible domain and point masses on the boundaries.

Usage

```
fexp(x, location, scale, mass = 0, log = FALSE)
fgpd(x, location, scale, shape, mass = 0, log = FALSE)

fgev(x, location, scale, shape)

fnorm(x, location, scale, lower = -Inf, upper = Inf, lmass = 0, umass = 0, log = FALSE)
ft(x, df, location, scale, lower = -Inf, upper = Inf, lmass = 0, umass = 0, log = FALSE)
flogis(x, location, scale, lower = -Inf, upper = Inf, lmass = 0, umass = 0, log = FALSE)
```


Arguments

<code>x</code>	vector of quantiles
<code>df</code>	vector of degrees of freedom parameters
<code>location</code>	vector of location parameters
<code>scale</code>	vector of scale parameters (positive)
<code>shape</code>	vector of shape parameters
<code>mass</code>	vector of point masses in <code>location</code>
<code>lower</code>	vector of lower bounds
<code>upper</code>	vector of upper bounds
<code>lmass</code>	vector of point masses in <code>lower</code> , or strings "trunc" / "cens"
<code>umass</code>	vector of point masses in <code>upper</code> , or strings "trunc" / "cens"
<code>log</code>	logical; if TRUE, the log of the density is returned

Details

For details on generalized extreme value and generalized Pareto distributions, see Friederichs, F. and T.L. Thorarinsdottir (2012, "Forecast verification for extreme value distributions with an application to probabilistic peak wind prediction", *Environmetrics* 23, 579-594). Note that the support of both distributions depends on the input parameters; see https://en.wikipedia.org/wiki/Generalized_extreme_value_distribution and https://en.wikipedia.org/wiki/Generalized_Pareto_distribution.

Sometimes truncated or censored versions of the normal distribution are used to model variables with a restricted domain (e.g. precipitation). We allow the flexible specification of lower and upper boundaries and point masses in those boundaries. The truncated normal distribution assumes no point masses (i.e. redistributes the cut-off) and can be specified using the string "trunc" instead of a numerical probability. In contrast, the censored distribution introduces a point mass at the bound in the amount of the cut-off. Here, the string "cens" may be used for `lmass` or `umass`. The most common use in practice lies in the context of non-negative quantities. For example, a truncated standard normal distribution (left truncation at zero) has pdf $f(x) = \phi(x)/(1 - \Phi(0))$, for $x \geq 0$ and 0 otherwise. A censored standard normal distribution (left censoring at zero) has point mass $\Phi(0)$ at zero, and density $\phi(x)$ for $x > 0$.

The location-scale family based on Student's t-distribution (`ft`) has mean `location` for $df > 1$ and variance $df/(df - 2) * scale^2$ for $df > 2$. Note that the `crps` exists only for $df > 1$. For details, see https://en.wikipedia.org/wiki/Student's_t-distribution#Non-standardized_Student.27s_t-distribution.

Value

Density function of the relevant distribution, evaluated at `x`. NOTE: For distributions involving a point mass (e.g., when `lmass = "cens"` in `fnorm`), the density functions do not integrate to one.

Author(s)

Alexander Jordan

See Also

The documentation for [crps.numeric](#) contains the full list of distributions supported by `scoringRules` (includes the ones documented here, as well as many others).

Index

- * **datasets**
 - GDP data, 8
- * **distributions**
 - Supplementary distributions:
 - Positive real line, 38
 - Supplementary distributions: Real line, 39
 - Supplementary distributions:
 - Variable support, 40
- * **replication**
 - plot.casestudy, 12
 - plot.mcstudy, 13
 - run_casestudy, 15
 - run_mcstudy, 16
- ar_ms, 2, 3, 4, 16
- bw.nrd, 34
- crps, 41
- crps (scores), 17
- crps.numeric, 5, 11, 17, 18, 38, 40, 42
- crps_2pexp, 5
- crps_2pexp (scores_2pexp), 18
- crps_2pnorm, 5
- crps_2pnorm (scores_2pnorm), 19
- crps_beta, 6
- crps_beta (scores_beta), 19
- crps_binom, 6, 11
- crps_binom (scores_binom), 20
- crps_clogis, 6
- crps_clogis (scores_logis), 26
- crps_cnorm, 6
- crps_cnorm (scores_norm), 30
- crps_ct, 6
- crps_ct (scores_t), 35
- crps_exp, 5
- crps_exp (scores_exp), 20
- crps_expM, 6
- crps_expM (scores_exp), 20
- crps_gamma, 5
- crps_gamma (scores_gamma), 21
- crps_gev, 6
- crps_gev (scores_gev), 22
- crps_gpd, 6
- crps_gpd (scores_gpd), 22
- crps_gtclogis, 6
- crps_gtclogis (scores_logis), 26
- crps_gtcnorm, 6
- crps_gtcnorm (scores_norm), 30
- crps_gtct, 6
- crps_gtct (scores_t), 35
- crps_hyper, 6, 11
- crps_hyper (scores_hyper), 23
- crps_lapl, 5
- crps_lapl (scores_lapl), 24
- crps_llapl, 6
- crps_llapl (scores_llapl), 24
- crps_llogis, 6
- crps_llogis (scores_llogis), 25
- crps_lnorm, 6
- crps_lnorm (scores_lnorm), 25
- crps_logis, 5
- crps_logis (scores_logis), 26
- crps_mixnorm, 5
- crps_mixnorm (scores_mixnorm), 27
- crps_mixnorm_int (scores_mixnorm), 27
- crps_nbinom, 6
- crps_nbinom (scores_nbinom), 29
- crps_norm, 5
- crps_norm (scores_norm), 30
- crps_pois, 6
- crps_pois (scores_pois), 31
- crps_sample, 34
- crps_sample (scores_sample_univ), 33
- crps_t, 5
- crps_t (scores_t), 35
- crps_tlogis, 6
- crps_tlogis (scores_logis), 26

- crps_tnorm, [6](#)
- crps_tnorm(scores_norm), [30](#)
- crps_tt, [6](#)
- crps_tt(scores_t), [35](#)
- crps_unif, [6](#)
- crps_unif(scores_unif), [36](#)

- dss_beta(scores_beta), [19](#)
- dss_exp(scores_exp), [20](#)
- dss_gamma(scores_gamma), [21](#)
- dss_gev(scores_gev), [22](#)
- dss_gpd(scores_gpd), [22](#)
- dss_lapl(scores_lapl), [24](#)
- dss_llapl(scores_llapl), [24](#)
- dss_llogis(scores_llogis), [25](#)
- dss_lnorm(scores_lnorm), [25](#)
- dss_logis(scores_logis), [26](#)
- dss_mixnorm(scores_mixnorm), [27](#)
- dss_moments(scores_moments), [28](#)
- dss_nbinom(scores_nbinom), [29](#)
- dss_norm(scores_norm), [30](#)
- dss_pois(scores_pois), [31](#)
- dss_sample(scores_sample_univ), [33](#)
- dss_t(scores_t), [35](#)
- dss_unif(scores_unif), [36](#)

- es_sample(scores_sample_multiv), [31](#)
- ess_moments(scores_moments), [28](#)

- f2pexp(Supplementary distributions:
Real line), [39](#)
- f2pnorm(Supplementary distributions:
Real line), [39](#)
- fexp(Supplementary distributions:
Variable support), [40](#)
- fgev(Supplementary distributions:
Variable support), [40](#)
- fspd(Supplementary distributions:
Variable support), [40](#)
- flapl(Supplementary distributions:
Real line), [39](#)
- llapl(Supplementary distributions:
Positive real line), [38](#)
- lllogis(Supplementary distributions:
Positive real line), [38](#)
- flogis, [40](#)
- flogis(Supplementary distributions:
Variable support), [40](#)

- fmixnorm(Supplementary distributions:
Real line), [39](#)
- fnorm, [40](#)
- fnorm(Supplementary distributions:
Variable support), [40](#)
- ft, [40](#)
- ft(Supplementary distributions:
Variable support), [40](#)

- gdp, [15](#)
- gdp(GDP data), [8](#)
- GDP data, [8](#)
- gdp_mcmc(GDP data), [8](#)
- gradcrps_clogis(scores_logis), [26](#)
- gradcrps_cnorm(scores_norm), [30](#)
- gradcrps_ct(scores_t), [35](#)
- gradcrps_logis(scores_logis), [26](#)
- gradcrps_norm(scores_norm), [30](#)
- gradcrps_t(scores_t), [35](#)
- gradcrps_tlogis(scores_logis), [26](#)
- gradcrps_tnorm(scores_norm), [30](#)
- gradcrps_tt(scores_t), [35](#)

- hesscrps_clogis(scores_logis), [26](#)
- hesscrps_cnorm(scores_norm), [30](#)
- hesscrps_ct(scores_t), [35](#)
- hesscrps_logis(scores_logis), [26](#)
- hesscrps_norm(scores_norm), [30](#)
- hesscrps_t(scores_t), [35](#)
- hesscrps_tlogis(scores_logis), [26](#)
- hesscrps_tnorm(scores_norm), [30](#)
- hesscrps_tt(scores_t), [35](#)

- logLik, [18](#)
- logs(scores), [17](#)
- logs.numeric, [7, 9, 17, 18](#)
- logs_2pexp, [10](#)
- logs_2pexp(scores_2pexp), [18](#)
- logs_2pnorm, [10](#)
- logs_2pnorm(scores_2pnorm), [19](#)
- logs_beta, [10](#)
- logs_beta(scores_beta), [19](#)
- logs_binom(scores_binom), [20](#)
- logs_exp, [10](#)
- logs_exp(scores_exp), [20](#)
- logs_exp2, [10](#)
- logs_exp2(scores_exp), [20](#)
- logs_gamma, [10](#)
- logs_gamma(scores_gamma), [21](#)

logs_gev, [10](#)
logs_gev (scores_gev), [22](#)
logs_gpd, [10](#)
logs_gpd (scores_gpd), [22](#)
logs_hyper (scores_hyper), [23](#)
logs_lapl, [10](#)
logs_lapl (scores_lapl), [24](#)
logs_llapl, [10](#)
logs_llapl (scores_llapl), [24](#)
logs_llogis, [10](#)
logs_llogis (scores_llogis), [25](#)
logs_lnorm, [10](#)
logs_lnorm (scores_lnorm), [25](#)
logs_logis, [10](#)
logs_logis (scores_logis), [26](#)
logs_mixnorm, [10](#)
logs_mixnorm (scores_mixnorm), [27](#)
logs_nbinom, [11](#)
logs_nbinom (scores_nbinom), [29](#)
logs_norm, [10](#)
logs_norm (scores_norm), [30](#)
logs_pois, [11](#)
logs_pois (scores_pois), [31](#)
logs_sample (scores_sample_univ), [33](#)
logs_t, [10](#)
logs_t (scores_t), [35](#)
logs_tlogis, [11](#)
logs_tlogis (scores_logis), [26](#)
logs_tnorm, [11](#)
logs_tnorm (scores_norm), [30](#)
logs_tt, [11](#)
logs_tt (scores_t), [35](#)
logs_unif, [10](#)
logs_unif (scores_unif), [36](#)

plot.casestudy, [12](#), [12](#), [16](#)
plot.mcstudy, [13](#), [13](#), [17](#)
print.casestudy, [14](#)
print.mcstudy, [14](#)

run_casestudy, [4](#), [12](#), [14](#), [15](#), [16](#), [37](#)
run_mcstudy, [13](#), [14](#), [16](#), [17](#), [37](#)

scores, [17](#)
scores_2pexp, [18](#)
scores_2pnorm, [19](#)
scores_beta, [19](#)
scores_binom, [20](#)
scores_exp, [20](#)
scores_gamma, [21](#)
scores_gev, [22](#)
scores_gpd, [22](#)
scores_hyper, [23](#)
scores_lapl, [24](#)
scores_llapl, [24](#)
scores_llogis, [25](#)
scores_lnorm, [25](#)
scores_logis, [26](#)
scores_mixnorm, [27](#)
scores_moments, [28](#)
scores_nbinom, [29](#)
scores_norm, [30](#)
scores_pois, [31](#)
scores_sample_multiv, [31](#)
scores_sample_univ, [33](#)
scores_t, [35](#)
scores_unif, [36](#)
summary.casestudy, [37](#)
summary.mcstudy, [37](#)
Supplementary distributions: Positive
real line, [38](#)
Supplementary distributions: Real
line, [39](#)
Supplementary distributions: Variable
support, [40](#)

vs_sample, [32](#)
vs_sample (scores_sample_multiv), [31](#)