

# Package ‘WR’

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**Type** Package

**Title** Win Ratio Analysis of Composite Time-to-Event Outcomes

**Version** 1.0

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**Description** Implements various win ratio methodologies for composite endpoints of death and non-fatal events, including the (stratified) proportional win-fractions (PW) regression models (Mao and Wang, 2020 <[doi:10.1111/biom.13382](https://doi.org/10.1111/biom.13382)>), (stratified) two-sample tests with possibly recurrent nonfatal event, and sample size calculation for standard win ratio test (Mao et al., 2021 <[doi:10.1111/biom.13501](https://doi.org/10.1111/biom.13501)>).

**License** GPL (>= 2)

**Encoding** UTF-8

**LazyData** true

**Depends** R (>= 3.5.0)

**RoxygenNote** 7.1.2

**Imports** survival, cubature, gumbel

**Suggests** knitr, rmarkdown

**VignetteBuilder** knitr

**NeedsCompilation** no

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base	<i>Compute the baseline parameters needed for sample size calculation for standard win ratio test</i>
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### Description

Compute the baseline parameters  $\zeta_0^2$  and  $\delta_0$  needed for sample size calculation for standard win ratio test (see [WRSS](#)). The calculation is based on a Gumbel–Hougaard copula model for survival time  $D^{(a)}$  and nonfatal event time  $T^{(a)}$  for group  $a$  (1: treatment; 0: control):

$$P(D^{(a)} > s, T^{(a)} > t) = \exp\left(-[\{\exp(a\xi_1)\lambda_D s\}^\kappa + \{\exp(a\xi_2)\lambda_H t\}^\kappa]^{1/\kappa}\right),$$

where  $\xi_1$  and  $\xi_2$  are the component-wise log-hazard ratios to be used as effect size in [WRSS](#). We also assume that patients are recruited uniformly over the period  $[0, \tau_b]$  and followed until time  $\tau$  ( $\tau \geq \tau_b$ ), with an exponential loss-to-follow-up hazard  $\lambda_L$ .

### Usage

```
base(lambda_D, lambda_H, kappa, tau_b, tau, lambda_L, N = 1000, seed = 12345)
```

### Arguments

lambda_D	Baseline hazard $\lambda_D$ for death.
lambda_H	Baseline hazard $\lambda_H$ for nonfatal event.
kappa	Gumbel–Hougaard copula correlation parameter $\kappa$ .
tau_b	Length of the initial (uniform) accrual period $\tau_b$ .
tau	Total length of follow-up $\tau$ .
lambda_L	Exponential hazard rate $\lambda_L$ for random loss to follow-up.
N	Simulated sample size for monte-carlo integration.
seed	Seed for monte-carlo simulation.

### Value

A list containing real number `zeta2` for  $\zeta_0^2$  and bivariate vector `delta` for  $\delta_0$ .

## References

Mao, L., Kim, K. and Miao, X. (2021). Sample size formula for general win ratio analysis. *Biometrics*, <https://doi.org/10.1111/biom.13501>.

## See Also

[gumbel.est](#), WRSS

## Examples

```
# see the example for WRSS
```

---

gbc	<i>A subset of the German Breast Cancer study data</i>
-----	--

---

## Description

These are a subset of the German Breast Cancer study data.

## Usage

```
gbc
```

## Format

A data frame with 985 rows and 12 variables:

**id** subject IDs

**time** event times (months)

**status** event status; 0:censoring, 1:death, 2:cancer recurrence

**hormone** treatment indicator: 1=Hormone therapy; 2=standard therapy

**age** age at diagnosis (years)

**menopause** menopausal Status; 1=No; 2=Yes

**size** tumor size

**grade** tumor grade, 1-3

**nodes** number of nodes involved

**prog\_recp** number of progesterone receptors

**estrg\_recp** number of estrogen receptors

## References

Sauerbrei, W., Royston, P., Bojar, H., Schmoor, C. and Schumacher, M. (1999). Modelling the effects of standard prognostic factors in node-positive breast cancer. German Breast Cancer Study Group (GBSG). *British Journal of Cancer*, 79, 1752–1760.

Hosmer, D.W. and Lemeshow, S. and May, S. (2008) *Applied Survival Analysis: Regression Modeling of Time to Event Data: Second Edition*, John Wiley and Sons Inc., New York, NY

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gumbel.est	<i>Estimate baseline parameters in the Gumbel–Hougaard model for sample size calculation using pilot data</i>
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## Description

Estimate baseline parameters in the Gumbel–Hougaard model described in [base](#) for sample size calculation using pilot study data.

## Usage

```
gumbel.est(id, time, status)
```

## Arguments

id	A vector of unique patient identifiers.
time	A numeric vector of event times.
status	A vector of event type variable; 2 = nonfatal event, 1 = death, and 0 = censoring.

## Value

A list containing lambda\_D for  $\lambda_D$ , lambda\_H for  $\lambda_H$ , and kappa for  $\kappa$  in the Gumbel–Hougaard model.

## References

Mao, L., Kim, K. and Miao, X. (2021). Sample size formula for general win ratio analysis. *Biometrics*, <https://doi.org/10.1111/biom.13501>.

## See Also

[base](#), [WRSS](#)

## Examples

```
# see the example for WRSS
```

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hfaction_cpx9	<i>A subset of the HF-ACTION study data on high-risk non-ischemic heart failure patients</i>
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**Description**

These are data on a subgroup of 426 high-risk non-ischemic patients in the HF-ACTION study.

**Usage**

hfaction\_cpx9

**Format**

A data frame with 1,448 rows and 5 variables:

**patid** patient ID

**time** event times (months)

**status** event status; 0:censoring, 1:death, 2:hospitalization

**trt\_ab** treatment indicator: 1: exercise training, 0: usual care

**age60** 1: 60 years or older, 0: less than 60 years old

**References**

O'Connor, C. M., Whellan, D. J., Lee, K. L., Keteyian, S. J., Cooper, L. S., Ellis, S. J., Leifer, E. S., Kraus, W. E., Kitzman, D. W., Blumenthal, J. A. et al. (2009). Efficacy and safety of exercise training in patients with chronic heart failure: HF-ACTION randomized controlled trial. *Journal of the American Medical Association*, 301, 1439–1450.

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non_ischemic	<i>A subset of the HF-ACTION study data on non-ischemic heart failure patients with full covariate measurement.</i>
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**Description**

These are a subset of the data on 451 non-ischemic patients in the HF-ACTION study will complete baseline covariates.

**Usage**

non\_ischemic

**Format**

A data frame with 751 rows and 16 variables:

**ID** subject IDs

**time** event times (days)

**status** event status; 0:censoring, 1:death, 2:hospitalization

**trt\_ab** treatment indicator: 1=exercise training; 0=usual care

**age** patient age in years

**sex** 1=female; 2=male

**Black.vs.White** 1=black; 0=otherwise

**Other.vs.White** 1=race other than black or white; 0=otherwise

**bmi** body mass index

**bipllvf** (biplane) left-ventricular ejection fraction

**hyperten** indicator for history of hypertension

**COPD** indicator for history of COPD

**diabetes** indicator for history of diabetes

**acei** indicator for current use of ACE inhibitors

**betab** indicator for current use of beta blockers

**smokecurr** indicator for current smoker

**References**

O'Connor, C. M., Whellan, D. J., Lee, K. L., Keteyian, S. J., Cooper, L. S., Ellis, S. J., Leifer, E. S., Kraus, W. E., Kitzman, D. W., Blumenthal, J. A. et al. (2009). Efficacy and safety of exercise training in patients with chronic heart failure: HF-ACTION randomized controlled trial. *Journal of the American Medical Association*, 301, 1439–1450.

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plot.pwreg.score

*Plot the standardized score processes*

---

**Description**

Plot the standardized score processes.

**Usage**

```
## S3 method for class 'pwreg.score'
plot(
  x,
  k,
  xlab = "Time",
  ylab = "Standardized score",
```

```
    lty = 1,  
    frame.plot = TRUE,  
    add = FALSE,  
    ylim = c(-3, 3),  
    xlim = NULL,  
    lwd = 1,  
    ...  
  )
```

### Arguments

<code>x</code>	an object of class <code>pwreg.score</code> .
<code>k</code>	A positive integer indicating the order of covariate to be plotted. For example, <code>k=3</code> requests the standardized score process for the third covariate in the covariate matrix <code>Z</code> .
<code>xlab</code>	a title for the x axis.
<code>ylab</code>	a title for the y axis.
<code>lty</code>	the line type. Default is 1.
<code>frame.plot</code>	a logical variable indicating if a frame should be drawn in the 1D case.
<code>add</code>	a logical variable indicating whether add to current plot?
<code>ylim</code>	a vector indicating the range of y-axis. Default is (-3,3).
<code>xlim</code>	a vector indicating the range of x-axis. Default is NULL.
<code>lwd</code>	the line width, a positive number. Default is 1.
<code>...</code>	further arguments passed to or from other methods

### Value

A plot of the standardized score process for object `pwreg.score`.

### See Also

[score.proc](#)

### Examples

```
# see the example for score.proc
```

print.pwreg                    *Print the results of the proportional win-fractions regression model*

---

**Description**

Print the results of the proportional win-fractions regression model.

**Usage**

```
## S3 method for class 'pwreg'  
print(x, ...)
```

**Arguments**

x                    an object of class pwreg.  
...                    further arguments passed to or from other methods

**Value**

Print the results of pwreg object

**See Also**

[pwreg](#)

**Examples**

```
# see the example for pwreg
```

---

print.pwreg.score            *Print information on the content of the pwreg.score object*

---

**Description**

Print information on the content of the pwreg.score object

**Usage**

```
## S3 method for class 'pwreg.score'  
print(x, ...)
```

**Arguments**

x                    A object of class pwreg.score.  
...                    further arguments passed to or from other methods.



**Value**

Print the results of `pwreg.score` object.

**See Also**

[score.proc](#)

**Examples**

```
# see the example for score.proc
```

---

<code>print.WRrec</code>	<i>Print the results of the two-sample recurrent-event win ratio analysis</i>
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---

**Description**

Print the results of the two-sample recurrent-event win ratio analysis.

**Usage**

```
## S3 method for class 'WRrec'  
print(x, ...)
```

**Arguments**

<code>x</code>	an object of class <code>WRrec</code> .
<code>...</code>	further arguments passed to or from other methods.

**Value**

Print the results of `WRrec` object.

**See Also**

[WRrec](#)

**Examples**

```
# see the example for WRrec
```

pwreg

*Fit a standard proportional win-fractions (PW) regression model***Description**

Fit a standard proportional win-fractions (PW) regression model.

**Usage**

```
pwreg(
  ID,
  time,
  status,
  Z,
  rho = 0,
  strata = NULL,
  fixedL = TRUE,
  eps = 1e-04,
  maxiter = 50
)
```

**Arguments**

ID	a vector of unique subject-level identifiers.
time	a vector of event times.
status	a vector of event type labels. 0: censoring, 1:death and 2: non-fatal event.
Z	a matrix or a vector of covariates.
rho	a non-negative number as the power of the survival function used in the weight. Default (rho=0) is recommended. If there is a 'strata' argument, then 'rho' is ignored.
strata	a vector of stratifying variable if a stratified model is desired.
fixedL	logical variable indicating which variance estimator to be used. If 'TRUE', the type I variance estimator (for a small number strata) is used; otherwise the type II variance estimator (for a large number strata) is used.
eps	precision for the convergence of Newton-Raphson algorithm.
maxiter	maximum number of iterations allow for the Newton-Raphson algorithm.

**Value**

An object of class pwreg with the following components. beta:a vector of estimated regression coefficients. Var:estimated covariance matrix for beta. conv: boolean variable indicating whether the algorithm converged within the maximum number of iterations.

**References**

- Mao, L. and Wang, T. (2020). A class of proportional win-fractions regression models for composite outcomes. *Biometrics*, 10.1111/biom.13382
- Wang, T. and Mao, L. (2021+). Stratified Proportional Win-fractions Regression Analysis.

**See Also**

[score.proc](#), [print.pwreg](#)

**Examples**

```
library(WR)
head(non_ischemic)
id_unique <- unique(non_ischemic$ID)

# Randomly sample 200 subjects from non_ischemic data
set.seed(2019)
id_sample <- sample(id_unique, 200)
non_ischemic_reduce <- non_ischemic[non_ischemic$ID %in% id_sample, ]

# Use the reduced non_ischemic data for analysis
nr <- nrow(non_ischemic_reduce)
p <- ncol(non_ischemic_reduce)-3
ID <- non_ischemic_reduce[, "ID"]
time <- non_ischemic_reduce[, "time"]
status <- non_ischemic_reduce[, "status"]
Z <- as.matrix(non_ischemic_reduce[, 4:(3+p)], nr, p)
## unstratified analysis
pwreg.obj <- pwreg(time=time, status=status, Z=Z, ID=ID)
print(pwreg.obj)
## Not run:
## stratified PW by sex
sex <- Z[, 3]
## take out sex from the covariate matrix
Z1 <- Z[, -3]
pwreg.obj1 <- pwreg(time=time, status=status, Z=Z1, ID=ID, strata=sex)
print(pwreg.obj1)

## End(Not run)
```

---

score.proc

*Computes the standardized score processes*

---

**Description**

Computes the standardized score processes for the covariates.

**Usage**

```
score.proc(obj, t = NULL)
```

**Arguments**

<code>obj</code>	an object of class <code>pwreg</code> .
<code>t</code>	a vector containing times. If not specified, the function will use all unique event times from the data.

**Value**

An object of class `pwreg.score` consisting of `t`: a vector of times; and `score`: a matrix whose rows are the standardized score processes as a function of `t`.

**References**

Mao, L. and Wang, T. (2020). A class of proportional win-fractions regression models for composite outcomes. *Biometrics*, 10.1111/biom.13382

**See Also**

[pwreg](#), [print.pwreg](#)

**Examples**

```
library(WR)
head(non_ischemic)

# Randomly sample 200 subjects from non_ischemic data
id_unique <- unique(non_ischemic$ID)
set.seed(2019)
id_sample <- sample(id_unique, 200)
non_ischemic_reduce <- non_ischemic[non_ischemic$ID %in% id_sample, ]

# Use the reduced non_ischemic data for analysis
nr <- nrow(non_ischemic_reduce)
p <- ncol(non_ischemic_reduce)-3
ID <- non_ischemic_reduce[, "ID"]
time <- non_ischemic_reduce[, "time"]
status <- non_ischemic_reduce[, "status"]
Z <- as.matrix(non_ischemic_reduce[, 4:(3+p)], nr, p)
pwreg.obj <- pwreg(time=time, status=status, Z=Z, ID=ID)
score.obj <- score.proc(pwreg.obj)
#plot the standardized score process for the first covariate
plot(score.obj, k = 1)
```

**Description**

Perform stratified two-sample test of possibly recurrent nonfatal event and death using the recommended last-event assisted win ratio (LWR), and/or naive win ratio (NWR) and first-event assisted win ratio (FWR) (Mao et al., 2022). The LWR and FWR reduce to the standard win ratio of Pocock et al. (2012).

**Usage**

```
WRrec(ID, time, status, trt, strata = NULL, naive = FALSE)
```

**Arguments**

ID	A vector of unique patient identifiers.
time	A numeric vector of event times.
status	A vector of event type variable; 2 = recurrent event, 1 = death, and 0 = censoring.
trt	A vector of binary treatment indicators.
strata	A vector of categorical variable for strata; Default is NULL, which leads to unstratified analysis.
naive	If TRUE, results for NWR and FWR will be provided in addition to LWR; Default is FALSE, which gives LWR only.

**Value**

An object of class WRrec, which contains the following elements.

theta	A bivariate vector of win/loss fractions by LWR.
log.WR, se	Log-win ratio estimate and its standard error by LWR.
pval	$p$ -value by the LWR test.
theta.naive	A bivariate vector of win/loss fractions by NWR.
log.WR.naive, se.naive	Log-win ratio estimate and its standard error by NWR.
theta.FI	A bivariate vector of win/loss fractions by FWR.
log.WR.FI, se.FI	Log-win ratio estimate and its standard error by FWR.
...	

**References**

- Mao, L., Kim, K. and Li, Y. (2022). On recurrent-event win ratio. *Statistical Methods in Medical Research*, under review.
- Pocock, S., Ariti, C., Collier, T., and Wang, D. (2012). The win ratio: a new approach to the analysis of composite endpoints in clinical trials based on clinical priorities. *European Heart Journal*, 33, 176–182.

**See Also**

[print.WRrec.](#)

**Examples**

```
## load the HF-ACTION trial data
library(WR)
head(hfaction_cpx9)
dat<-hfaction_cpx9
## Comparing exercise training to usual care by LWR, FWR, and NWR
obj<-WRrec(ID=dat$patid,time=dat$time,status=dat$status,
           trt=dat$trt_ab,strata=dat$age60,naive=TRUE)
## print the results
obj
```

---

WRSS

---

*Compute the sample size for standard win ratio test*


---

**Description**

Compute the sample size for standard win ratio test.

**Usage**

```
WRSS(xi, bparam, q = 0.5, alpha = 0.05, side = 2, power = 0.8)
```

**Arguments**

xi	A bivariate vector of hypothesized component-wise (treatment-to-control) log-hazard ratios under the Gumbel–Hougaard copula model described in <a href="#">base</a> .
bparam	A list containing baseline parameters zeta2 for $\zeta_0^2$ and delta for $\delta_0$ ; Can directly use the output of <a href="#">base</a> .
q	Proportion of patients assigned to treatment.
alpha	Type I error rate.
side	2-sided or 1-sided test.
power	Target power.

**Value**

A list containing n, the computed sample size.

**References**

Mao, L., Kim, K. and Miao, X. (2021). Sample size formula for general win ratio analysis. *Biometrics*, <https://doi.org/10.1111/biom.13501>.

**See Also**

[gumbel.est, base](#)

**Examples**

```
# The following is not run in package checking to save time.
## Not run:
## load the package and pilot dataset
library(WR)
head(hfaction_cpx9)
dat<-hfaction_cpx9
## subset to control group
pilot<-dat[dat$trt_ab==0,]

## get the data ready for gumbel.est()
id<-pilot$patid
## convert time from month to year
time<-pilot$time/12
status<-pilot$status
## compute the baseline parameters for the Gumbel--Hougaard
## copula for death and hospitalization
gum<-gumbel.est(id, time, status)

## get the baseline parameters
lambda_D<-gum$lambda_D
lambda_H<-gum$lambda_H
kappa<-gum$kappa
## set up design parameters and use base()
## to calculate bparam for WRSS()
# max follow-up 4 years
tau<-4
# 3 years of initial accrual
tau_b<-3
# loss to follow-up rate
lambda_L=0.05
# compute the baseline parameters
bparam<-base(lambda_D,lambda_H,kappa,tau_b,tau,lambda_L)
bparam

## sample size with power=0.8 under hazard ratios
## 0.9 and 0.8 for death and hospitalization, respectively.
WRSS(xi=log(c(0.9,0.8)),bparam=bparam,q=0.5,alpha=0.05,
      power=0.8)$n
## sample size under the same set-up but with power 0.9
WRSS(xi=log(c(0.9,0.8)),bparam=bparam,q=0.5,alpha=0.05,
      power=0.9)$n

## End(Not run)
```

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