

# Package ‘mar1s’

August 18, 2018

**Type** Package

**Title** Multiplicative AR(1) with Seasonal Processes

**Version** 2.1.1

**Date** 2018-08-17

**Author** Andrey Paramonov

**Maintainer** Andrey Paramonov <paramon@acd1labs.ru>

**Depends** cmrutils, fda, zoo

**Description** Multiplicative AR(1) with Seasonal is a stochastic process model built on top of AR(1). The package provides the following procedures for MAR(1)S processes: fit, compose, decompose, advanced simulate and predict.

**License** GPL (>= 3)

**URL** <https://github.com/aparamon/mar1s>

**NeedsCompilation** no

**Repository** CRAN

**Date/Publication** 2018-08-18 15:30:03 UTC

## R topics documented:

compose.ar1 . . . . .	2
compose.mar1s . . . . .	3
fit.mar1s . . . . .	5
forest.fire . . . . .	7
nesterov.index . . . . .	7
seasonal.ave . . . . .	8
seasonal.smooth . . . . .	9
sim.mar1s . . . . .	11

<b>Index</b>	<b>13</b>
--------------	-----------

compose.ar1

*Compose and Decompose AR(1) Process***Description**

compose.ar1 composes AR(1) process realization by given vector(s) of innovations.

decompose.ar1 extracts AR(1) process residuals from time series.

**Usage**

```
compose.ar1(arcoef, innov, init = 0, xregcoef = 0, xreg = NULL,
            init.xreg = rep(0, length(xregcoef)))
```

```
decompose.ar1(arcoef, data, init = NA, xregcoef = 0, xreg = NULL,
              init.xreg = rep(NA, length(xregcoef)))
```

**Arguments**

arcoef	A number specifying autoregression coefficient.
innov	A univariate or multivariate time series containing the innovations.
data	A univariate or multivariate time series containing the process realization(s).
init	A number specifying the value of the process just prior to the start value in innov/data.
xregcoef	A vector specifying coefficients for the external regressors.
xreg	A matrix-like object of the same row count as innov/data, specifying the values of external regressors. The default NULL means zeroes.
init.xreg	A vector specifying the values of external regressors just prior to the start values in xreg. The default NULL means zeroes.

**Details**

Here *AR(1) process with external regressors* is a linear regression with AR(1) model for the error term:

$$y_t = b_1 x_{t,1} + \dots + b_k x_{t,k} + z_t$$

$$z_t = a z_{t-1} + e_t$$

Use xreg = NULL for the regular AR(1) process.

**Value**

An object of the same type and dimensions as innov/data (typically time series).

**See Also**

[arima](#) for more general  $ARMA(p, q)$  processes.

**Examples**

```
## Simple
e <- ts(c(0, 1, 0, 1, 0), freq = 12)
compose.ar1(0.1, e)
compose.ar1(0.1, e, 1)

x <- ts(c(0, 1, 0, 1, 0), freq = 12)
decompose.ar1(0.1, x)
decompose.ar1(0.1, x, 1)

## Multiseries
compose.ar1(0.1, ts(cbind(0, 1)))
compose.ar1(0.1, ts(cbind(c(0, 1, 0), c(1, 0, 1))))

decompose.ar1(0.1, ts(cbind(0, 1)))
decompose.ar1(0.1, ts(cbind(c(0, 1, 0), c(1, 0, 1))))

## External regressors
xreg1 <- rep(2, 5)
xreg2 <- matrix(rep(c(2, 1), each = 5), 5, 2)
e <- ts(c(0, 1, 0, 1, 0), freq = 12)
compose.ar1(0.1, e, xregcoef = 0.5, xreg = xreg1)
compose.ar1(0.1, e, xregcoef = 0.5, init = 0, xreg = xreg1, init.xreg = -2)
compose.ar1(0.1, e, xregcoef = c(1, -1), xreg = xreg2)

x <- ts(c(0, 1, 0, 1, 0), freq = 12)
decompose.ar1(0.1, x, xregcoef = 0.5, xreg = xreg1)
decompose.ar1(0.1, x, xregcoef = 0.5, init = 0, xreg = xreg1, init.xreg = -2)
decompose.ar1(0.1, x, xregcoef = c(1, -1), xreg = xreg2)

## Back-test
a <- 0.5
innov <- ts(rnorm(10), frequency = 12)
init <- 1
xrcoef <- seq(-0.1, 0.1, length.out = 3)
xreg <- matrix(1:30, 10, 3)
init.xreg <- 1:3
x <- compose.ar1(a, innov, init, xrcoef, xreg, init.xreg)
r <- decompose.ar1(a, x, init, xrcoef, xreg, init.xreg)
stopifnot(all.equal(innov, r))
```

**Description**

compose.mar1s composes MAR(1)S process realization by given vector of log-innovations.  
 decompose.mar1s extracts MAR(1)S process components from time series.

**Usage**

```
compose.mar1s(object, loginnov, start.time = head(time(loginnov), 1),
              xreg.absdata = NULL, init.absdata = NULL)
```

```
decompose.mar1s(object, absdata, start.time = head(time(absdata), 1),
                 init.absdata = rep(NA, NCOL(absdata)))
```

**Arguments**

object	An object of class "mar1s" specifying the model parameters.
loginnov	A univariate time series containing the log-innovations.
absdata	A univariate or multivariate time series containing the process realization.
start.time	The sampling time for the first simulation step.
xreg.absdata	A matrix-like object with row count = n.ahead, specifying the values for the external regressors. If NULL, default values are used.
init.absdata	A vector specifying the initial values of the process. If NULL, default values are used.

**Details**

*Multiplicative AR(1) with Seasonal (MAR(1)S) process* is defined as

$$x_t = \exp(s_t + y_t)$$

$$y_{t,1} = b_1 y_{t,2} + \dots + b_k y_{t,k+1} + z_t$$

$$z_t = a z_{t-1} + e_t$$

where

$s_t$  is the log-seasonal component,

$y_t$  is the AR(1) (log-stochastic) component,

$e_t$  is the log-residuals (random component).

**Value**

absdata	Realization of the process (a univariate or multivariate time series object).
logdata	Logarithm of absdata (a univariate or multivariate time series object).
logstoch	Log-stochastic component (a univariate or multivariate time series object).
logresid	Random component (a univariate time series object).

**Note**

decompose.mar1s and fit.mar1s compute the random component in different ways: decompose.mar1s uses filter while fit.mar1s saves the residuals returned by arima. The results may be different in:

**the first value:** decompose.mar1s uses specified init.absdata while arima always assumes zero initial values for the fitted process;

**non-finite values:** decompose.mar1s handles non-finite values more accurately.

**See Also**

[compose.ar1](#) for the AR(1) with external regressors processes, [fit.mar1s](#) for fitting MAR(1)S process to data, [sim.mar1s](#) for MAR(1)S process simulation and prediction.

**Examples**

```
data(forest.fire, package = "mar1s")
data(nesterov.index, package = "mar1s")

## Simple
mar1s <- fit.mar1s(window(forest.fire, 1969, 1989))

x <- ts(rnorm(365, sd = mar1s$logresid.sd), start = c(1989, 1))
plot(compose.mar1s(mar1s, x)$absdata)

decomp <- decompose.mar1s(mar1s, mar1s$decomposed$absdata)
delta <- abs(nan2na(mar1s$decomposed$logresid) -
             nan2na(decomp$logresid))
stopifnot(all(na.exclude(tail(delta, -1)) < 1E-6))

## External regressors
mar1s <- fit.mar1s(window(forest.fire, 1969, 1989),
                  window(nesterov.index[, "mean"], 1969, 1989))

x <- rnorm(365, sd = mar1s$logresid.sd)
xreg <- window(nesterov.index[, "mean"], 1989.001, 1990)
plot(compose.mar1s(mar1s, x, c(1989, 1), xreg)$absdata)

decomp <- decompose.mar1s(mar1s, mar1s$decomposed$absdata)
delta <- abs(mar1s$decomposed$logstoch - decomp$logstoch)
stopifnot(all(na.exclude(delta) < 1E-6))
delta <- abs(nan2na(mar1s$decomposed$logresid) -
             nan2na(decomp$logresid))
stopifnot(all(na.exclude(tail(delta, -1)) < 1E-6))
```

**Description**

Fits Multiplicative AR(1) with Seasonal process model to time series.

**Usage**

```
fit.mar1s(x, xreg = NULL, seasonal.fun = seasonal.smooth, ...)
```

**Arguments**

x	A univariate time series.
xreg	A univariate or multivariate time series of external regressors, or NULL.
seasonal.fun	A function which takes a univariate time series as its first argument and returns the estimated seasonal component.
...	Additional arguments passed to seasonal.fun.

**Value**

An object of class "mar1s" with the following components:

logseasonal	Estimated log-seasonal figure (a univariate or multivariate time series object).
logstoch.ar1	AR(1) with external regressors model fitted for the log-stochastic component (an object of class "Arima").
logresid.sd	Standard deviation of the residuals.
decomposed	An object of class "mar1s.ts" containing decomposed time series (see <a href="#">compose.mar1s</a> ).

**See Also**

[compose.mar1s](#) for MAR(1)S process formal definition and composition/decomposition functions, [seasonal.ave](#), [seasonal.smooth](#) for seasonal component extraction functions, [sim.mar1s](#) for MAR(1)S process simulation and prediction.

**Examples**

```
data(forest.fire, package = "mar1s")
data(nesterov.index, package = "mar1s")

## Simple
mar1s <- fit.mar1s(forest.fire)
plot(mar1s$logseasonal)
confint(mar1s$logstoch.ar1)
mar1s$logresid.sd
resid <- nan2na(mar1s$decomposed$logresid)
qqnorm(resid)
qqline(resid)

## External regressors
mar1s <- fit.mar1s(forest.fire, nesterov.index[, "mean"])
plot(cbind(mar1s$logseasonal, mar1s$logseasonal.r))
confint(mar1s$logstoch.ar1)
```

```
resid <- nan2na(mar1s$decomposed$logresid)
qqnorm(resid)
qqline(resid)
```

---

forest.fire

*Forest fire in Irkutsk region, USSR: historical data*

---

### Description

Number of forest fire seats in Irkutsk region, USSR. Daily from April 01 to October 31, 1969–1991 (total 4708 observations).

### Usage

```
data(forest.fire)
```

### Format

A univariate time series.

### Source

AviaLesoOkhrana (<http://www.nffc.aviales.ru/engl/main.sht>).

### Examples

```
data(forest.fire)
colnames(forest.fire)
plot(forest.fire)
```

---

nesterov.index

*Nesterov index in Irkutsk region, USSR: historical data*

---

### Description

Values of Nesterov index in 6 distincts of Irkutsk region, USSR + region averaged. Daily from April 01 to October 31, 1969–1991 (total 4708 observations).

### Usage

```
data(nesterov.index)
```

### Format

A multivariate time series.

### Details

The Nesterov index is the official Russian fire-danger rating specified by standard GOST R 22.1.09–99. It is calculated using the ignition index, the temperature, the dew-point temperature and the number of days since last significant ( $\geq 3mm$ ) precipitation.

The dataset consists of daily values 1969–1991.

### Source

Russian Institute of Hydrometeorological Information–World Data Center (<http://meteo.ru/english/>).

### Examples

```
data(nesterov.index)
colnames(nesterov.index)
plot(nesterov.index)
```

---

seasonal.ave

*Averaged Seasonal Component of Time Series*

---

### Description

Extracts seasonal component of time series by averaging observations on the same position in the cycle.

### Usage

```
seasonal.ave(x, ave.FUN = mean, ...)
```

### Arguments

x	A univariate time series.
ave.FUN	Averaging function.
...	Additional arguments passed to ave.FUN.

### Value

A time series object with times from 0 to 1 and the same frequency as x.

### See Also

[ave](#), [seasonal.smooth](#) for alternative seasonal extraction method.



## Examples

```

set.seed(19860306)

## Artificial example
x <- ts(sin(2*pi*(3:97)/10) + 0.5*rnorm(length(3:97)),
start = c(0, 3), frequency = 10)

plot.default(time(x)%%1, x, xlab = "Phase")
lines(seasonal.ave(x), col = "blue")
lines(seasonal.ave(x, median), col = "green")
legend("bottomleft",
      legend = c("Mean averaging",
"Median averaging"),
      col = c("blue", "green"),
      lty = "solid")

## Realistic example
data(nesterov.index, package = "mar1s")
x <- log(nesterov.index[, "mean"])
x[x < -10] <- -Inf

plot.default(time(x)%%1, x, xlab = "Phase", pch = ".")
lines(seasonal.ave(x), col = "blue")
lines(seasonal.ave(x, median), col = "green")
legend("topleft",
      legend = c("Mean averaging",
"Median averaging"),
      col = c("blue", "green"),
      lty = "solid")

```

---

seasonal.smooth

*Smooth Seasonal Component of Time Series*


---

## Description

Extracts seasonal component of time series by fitting the data with a linear combination of smooth periodic functions.

## Usage

```
seasonal.smooth(x, basis = create.fourier.basis(nbasis = 3), lambda = 0, ...)
```

## Arguments

x	A univariate time series.
basis	A functional basis object (see <a href="#">basisfd</a> ). By default, use a linear combination of $\text{const}$ , $\sin((2\pi)*t)$ and $\cos((2\pi)*t)$ .
lambda	A nonnegative number specifying the amount of smoothing. By default, apply no additional smoothing.
...	Not currently used.

## Details

Although it is possible to specify arbitrary functional basis object, the function will only work properly if the basis is periodical on the unit interval. It is recommended to use a Fourier basis with default period ([create.fourier.basis](#)).

Positive values of lambda imply a restriction on roughness of the result. The more the value, the more smooth result is; see [smooth.basis](#) for more detailed description.

## Value

A time series object with times from 0 to 1 and the same frequency as x. The smoothing functional data object is stored in attribute fd.

## See Also

[smooth.basisPar](#), [fd](#) for functional data objects, [seasonal.ave](#) for alternative seasonal extraction method.

## Examples

```
set.seed(19860306)

## Artificial example
x <- ts(sin(2*pi*(3:97)/10) + 0.5*rnorm(length(3:97)),
start = c(0, 3), frequency = 10)

fourier3 <- seasonal.smooth(x)
fourier9 <- seasonal.smooth(x, create.fourier.basis(nbasis = 9))
fourier9s<- seasonal.smooth(x, create.fourier.basis(nbasis = 9), 1E-6)

plot.default(time(x)%%1, x, xlab = "Phase")
points(fourier3, pch = 20, col = "blue")
lines(attr(fourier3, "fd"), col = "blue")
points(fourier9, pch = 20, col = "green")
lines(attr(fourier9, "fd"), col = "green")
points(fourier9s, pch = 20, col = "red")
lines(attr(fourier9s, "fd"), col = "red")
legend("bottomleft",
      legend = c("Fourier-3 basis",
"Fourier-9 basis",
"Fourier-9 basis, smooth"),
      col = c("blue", "green", "red"),
      lty = "solid")

## Realistic example
data(nesterov.index, package = "mar1s")
x <- log(nesterov.index[, "mean"])
x[x < -10] <- -Inf

fourier3 <- seasonal.smooth(x)
fourier9 <- seasonal.smooth(x, create.fourier.basis(nbasis = 9))
fourier9s<- seasonal.smooth(x, create.fourier.basis(nbasis = 9), 2E-5)
```

```

plot.default(time(x)%%1, x, xlab = "Phase", pch = ".")
lines(attr(fourier3, "fd"), col = "blue")
lines(attr(fourier9, "fd"), col = "green")
lines(attr(fourier9s, "fd"), col = "red")
legend("topleft",
      legend = c("Fourier-3 basis",
                 "Fourier-9 basis",
                 "Fourier-9 basis, smooth"),
      col = c("blue", "green", "red"),
      lty = "solid")

```

---

sim.mar1s

*Simulate from MAR(1)S Process*


---

### Description

sim.mar1s simulates from MAR(1)S process.

predict.mar1s is a wrapper around sim.mar1s which estimates confidence intervals for the future values of the MAR(1)S process.

### Usage

```

sim.mar1s(object, n.ahead = 1, n.sim = 1, start.time = 0,
          xreg.absdata = NULL, init.absdata = NULL)

```

```

## S3 method for class 'mar1s'
predict(object, n.ahead = 1, start.time = 0,
        xreg.absdata = NULL, init.absdata = NULL,
        probs = c(0.05, 0.5, 0.95), n.sim = 1000, ...)

```

### Arguments

object	An object of class "mar1s" specifying the model parameters.
n.ahead	Number of steps ahead at which to simulate/predict.
n.sim	Number of simulations.
start.time	The sampling time for the first simulation step.
xreg.absdata	A matrix-like object with row count = n.ahead, specifying the values for the external regressors. If NULL, default values are used.
init.absdata	A vector specifying the initial values of the process. If NULL, default values are used.
probs	A vector of probabilities.
...	Arguments from previous methods.

**Value**

For `sim.mar1s`, a vector of simulated values.

For `predict.mar1s`, a vector of estimated quantiles.

**See Also**

[compose.mar1s](#) for MAR(1)S process formal definition and composition/decomposition functions,  
[fit.mar1s](#) for fitting MAR(1)S process to data.

**Examples**

```
data(forest.fire, package = "mar1s")
data(nesterov.index, package = "mar1s")

## Univariate
mar1s <- fit.mar1s(forest.fire)

sim.mar1s(mar1s)
sim.mar1s(mar1s, n.sim = 6)
sim.mar1s(mar1s, n.ahead = 3)

predict(mar1s)
predict(mar1s, n.ahead = 10)
predict(mar1s, init.absdata = 100)

t <- seq(1/12, 11/12, 1/6)
p <- mapply(predict, start.time = t,
            MoreArgs = list(object = mar1s, probs = c(0.05, 0.95)))
plot(exp(mar1s$logseasonal), ylim = c(0, max(p)),
     ylab = "Forest fire")
arrows(t, p[1, ], t, p[2, ],
       code = 3, angle = 90, length = 0.05)

## External regressors
mar1s <- fit.mar1s(forest.fire, nesterov.index[, "mean"])

sim.mar1s(mar1s)
sim.mar1s(mar1s, n.sim = 6)

predict(mar1s)
predict(mar1s, xreg.absdata = 10000)
predict(mar1s, init.absdata = c(100, 1000))
```

# Index

## \*Topic **datasets**

forest.fire, 7  
nesterov.index, 7

## \*Topic **models**

compose.ar1, 2  
compose.mar1s, 3  
fit.mar1s, 5  
sim.mar1s, 11

## \*Topic **multivariate**

compose.ar1, 2  
compose.mar1s, 3  
fit.mar1s, 5  
sim.mar1s, 11

## \*Topic **ts**

compose.ar1, 2  
compose.mar1s, 3  
fit.mar1s, 5  
seasonal.ave, 8  
seasonal.smooth, 9  
sim.mar1s, 11

arima, 3

ave, 8

basisfd, 9

compose.ar1, 2, 5

compose.mar1s, 3, 6, 12

create.fourier.basis, 10

decompose.ar1 (compose.ar1), 2

decompose.mar1s (compose.mar1s), 3

fd, 10

fit.mar1s, 5, 5, 12

forest.fire, 7

nesterov.index, 7

predict.mar1s (sim.mar1s), 11

seasonal.ave, 6, 8, 10

seasonal.smooth, 6, 8, 9

sim.mar1s, 5, 6, 11

smooth.basis, 10

smooth.basisPar, 10