

recommenderlab: An R Framework for Developing and Testing Recommendation Algorithms

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Abstract

Algorithms that create recommendations based on observed data have significant commercial value for online retailers and many other industries. Recommender systems has a significant research community and studying such systems is part of most modern data science curricula. While there is an abundance of software that implements recommendation algorithms, there is little in terms of supporting recommender system research and education. This paper describes the open-source software **recommenderlab** which was created with supporting research and education in mind. The package can be directly installed in R or downloaded from <https://github.com/mhahsler/recommenderlab>.

Keywords: recommender systems, collaborative filtering, evaluation.

1. Introduction

Recommender systems apply statistical and knowledge discovery techniques to the problem of making product recommendations based on previously recorded usage data (Sarwar, Karypis, Konstan, and Riedl 2000). Creating such automatically generated personalized recommendations for products including books, songs, TV shows and movies using collaborative filtering have come a long way since Information Lense, the first system using *social filtering* was created more than 30 years ago (Malone, Grant, Turbak, Brobst, and Cohen 1987). Today, recommender systems are a successful technology used by market leaders in several industries (e.g., by Amazon, Netflix, and Pandora). In retail, such recommendations can improve conversion rates by helping the customer to find products she/he wants to buy faster, promote cross-selling by suggesting additional products and can improve customer loyalty through creating a value-added relationship (Schafer, Konstan, and Riedl 2001).

Even after 30 years, recommender systems still have a very active research community. It is often not clear which of the many available algorithms is appropriate for a particular application and new approaches are constantly proposed. Many commercially available software applications implement recommender algorithms, however, this paper focuses on software support for recommender systems research which includes rapid prototyping algorithms and thorough evaluation and comparison of algorithms. For this purpose, access to the source code is paramount. Many open-source projects implementing recommender algorithms have been initiated over the years. Table 1 provides links to several popular open source implementations which provide code which can be used by researchers. The extent of (currently available) functionality as well as the target usage of the available software packages vary greatly and many projects have been abandoned over the years. A comprehensive list of

Software	Description	Language	URL
Apache Mahout	Machine learning library includes collaborative filtering	Java	http://mahout.apache.org/
Crab	Components to create recommender systems	Python	https://github.com/muricoca/crab
LensKit	Collaborative filtering algorithms from GroupLens Research	Python	http://lenskit.grouplens.org/
MyMediaLite	Recommender system algorithms.	C#/Mono	http://www.mymedialite.net/
SVDFeature	Toolkit for feature-based matrix factorization	C++	https://www.jmlr.org/papers/v13/chen12a.html
Vogoo PHP LIB	Collaborative filtering engine for personalizing web sites	PHP	http://sourceforge.net/projects/vogoo/

Table 1: Recommender System Software freely available for research.

recommender systems software is maintained by [Jenson \(2019\)](#).

Most available software focuses on creating recommender applications for deployment as a production system or they implement a single method as part of a research project. The R extension package **recommenderlab** described in this paper was designed for a completely different purpose. It aims at providing a comprehensive research infrastructure for recommender systems. The focus is on consistent and efficient data handling, easy incorporation of existing and new algorithms, experiment set up and evaluation of the results. The open-source programming language R, a popular software environment for statistical computing and data scientists ([R Core Team 2018](#)), is used as the platform since it easily allows the researcher to either implement and integrate algorithms written in a wide range of programming languages including R, Python, Java, C/C++ and already provides all needed statistical tools which is important to provide a useful research environment.

Although developed to support the author’s own research and teaching needs in 2010, there proved to be a need for research-focused software and the package **recommenderlab** turned out to be quite popular. A healthy community of users who file bug reports, suggest improvements and contribute their own algorithms has grown around the package and is coordinated using the software’s GitHub page¹. Authors not related to the developer have written a textbook about how to use the package ([Gorakala and Usulli 2015](#)). The package is used in several university courses to demonstrate the basics of recommender system development. Finally, the

¹<https://github.com/mhahsler/recommenderlab>

package was employed by several researchers to develop and test their own algorithms (e.g., Chen, Chao, and Shah 2013; Buhl, Famulare, Glazier, Harris, McDowell, Waldrip, Barnes, and Gerber 2016; Beel, Breitingner, Langer, Lommatzsch, and Gipp 2016; Lombardi and Vernerio 2017).

Package **recommenderlab** focuses on collaborative filtering which is based on the idea that given rating data by many users for many items (e.g., 1 to 5 stars), one can predict a user's rating for an item not known to her or him (see, e.g., Goldberg, Nichols, Oki, and Terry 1992) or create for each user a so called top- N lists of recommended items (see, e.g., Sarwar, Karypis, Konstan, and Riedl 2001; Deshpande and Karypis 2004). The premise is that users who agreed on the rating for some items typically also tend to agree on the rating for other items.

recommenderlab provides implementations of many popular algorithms, including the following.

- **User-based collaborative filtering (UBCF)** predicts ratings by aggregating the ratings of users who have a similar rating history to the active user (Goldberg *et al.* 1992; Resnick, Iacovou, Suchak, Bergstrom, and Riedl 1994; Shardanand and Maes 1995).
- **Item-based collaborative filtering (IBCF)** uses item-to-item similarity based on user ratings to find items that are similar to the items the active user likes (Kitts, Freed, and Vrieze 2000; Sarwar *et al.* 2001; Linden, Smith, and York 2003; Deshpande and Karypis 2004).
- **Latent factor models** use singular value decomposition (SVD) to estimate missing ratings using methods like SVD with column-mean imputation, Funk SVD or alternating least squares (Hu, Koren, and Volinsky 2008; Koren, Bell, and Volinsky 2009).
- **Association rule-based recommender (AR)** uses association rules to find recommended items (Fu, Budzik, and Hammond 2000; Mobasher, Dai, Luo, and Nakagawa 2001; Geyer-Schulz, Hahsler, and Jahn 2002; Lin, Alvarez, and Ruiz 2002; Demiriz 2004).
- **Popular items (POPULAR)** is a non-personalized algorithm which recommends to all users the most popular items they have not rated yet.
- **Randomly chosen items (RANDOM)** creates random recommendations which can be used as a baseline for recommender algorithm evaluation.
- **Re-recommend liked items (RERECOMMEND)** recommends items which the user has rated highly in the past. These recommendations can be useful for items that are typically consumed more than once (e.g., listening to songs or buying groceries).
- **Hybrid recommendations (HybridRecommender)** aggregates the recommendations of several algorithms (Çano and Morisio 2017).

We will discuss some of these algorithms in the rest of the paper. Detailed information can be found in the survey book by Desrosiers and Karypis (2011).

This rest of this paper is structured as follows. Section 2 introduces collaborative filtering and some of its popular algorithms. In section 3 we discuss the evaluation of recommender algorithms. We introduce the infrastructure provided by **recommenderlab** in section 4. In section 5 we illustrate the capabilities on the package to create and evaluate recommender algorithms. We conclude with section 6.

2. Collaborative Filtering

To understand the use of the software, a few formal definitions are necessary. We will often give examples for a movie recommender, but the examples generalize to other types of items as well. Let $\mathcal{U} = \{u_1, u_2, \dots, u_m\}$ be the set of users and $\mathcal{I} = \{i_1, i_2, \dots, i_n\}$ the set of items. Ratings are stored in a $m \times n$ user-item rating matrix $\mathbf{R} = (r_{jl})$, where each row represents a user u_j with $1 \leq j \leq m$ and columns represent items i_l with $1 \leq l \leq n$. We use \mathbf{r}_j to denote the row vector of \mathbf{R} with the ratings of user u_j . Ratings use a specific rating scale. For example, Netflix uses 1 to 5 stars. and estimated ratings are allowed to be within an interval of matching range (e.g., $[1, 5]$). Typically, only a small fraction of ratings are known and for many cells in \mathbf{R} , the values are missing. Missing values represent movies that the user has not rated and potentially also not seen yet.

Collaborative filtering aims to create recommendations for a user called the active user $u_a \in \mathcal{U}$. We define the set of items unknown to user u_a as $\mathcal{I}_a = \mathcal{I} \setminus \{i_l \in \mathcal{I} \mid r_{al} \text{ is not missing}\}$. The two typical tasks are to predict ratings for all items in \mathcal{I}_a or to create a list containing the best N recommended items from \mathcal{I}_a (i.e., a top- N recommendation list) for u_a . Predicting all missing ratings means completing the row of the rating matrix where the missing values for items in \mathcal{I}_a are replaced by ratings estimated from other data in \mathbf{R} . From this point of view, recommender systems are related to matrix completion problem. Creating a top- N list can be seen as a second step after predicting ratings for all unknown items in \mathcal{I}_a and then taking the N items with the highest predicted ratings. Some algorithms skip predicting ratings first and are able to find the top N items directly. A list of top- N recommendations for a user u_a is an partially ordered set $T_N = (\mathcal{X}, \geq)$, where $\mathcal{X} \subset \mathcal{I}_a$ and $|\mathcal{X}| \leq N$ ($|\cdot|$ denotes the cardinality of the set). Note that there may exist cases where top- N lists contain less than N items. This can happen if $|\mathcal{I}_a| < N$ or if the CF algorithm is unable to identify N items to recommend. The binary relation \geq is defined as $x \geq y$ if and only if $\hat{r}_{ax} \geq \hat{r}_{ay}$ for all $x, y \in \mathcal{X}$. Furthermore we require that $\forall_{x \in \mathcal{X}} \forall_{y \in \mathcal{I}_a} \hat{r}_{ax} \geq \hat{r}_{ay}$ to ensure that the top- N list contains only the items with the highest estimated rating.

Typically we deal with a very large number of items with unknown ratings which makes first predicting rating values for all of them computationally expensive. Some approaches (e.g., rule based approaches) can predict the top- N list directly without considering all unknown items first.

Collaborative filtering algorithms are typically divided into two groups, *memory-based CF* and *model-based CF* algorithms (Breese, Heckerman, and Kadie 1998). Memory-based CF use the whole (or at least a large sample of the) user database to create recommendations. The most prominent algorithm is user-based collaborative filtering. The disadvantages of this approach is scalability since the whole user database has to be processed online for creating recommendations. Model-based algorithms use the user database to learn a more compact model (e.g, clusters with users of similar preferences) that is later used to create

recommendations.

In the following we will present the basics of well known memory and model-based collaborative filtering algorithms. Further information about these algorithms can be found in the recent survey book chapter by [Desrosiers and Karypis \(2011\)](#).

2.1. User-based Collaborative Filtering

User-based CF ([Goldberg *et al.* 1992](#); [Resnick *et al.* 1994](#); [Shardanand and Maes 1995](#)) is a memory-based algorithm which tries to mimics word-of-mouth by analyzing rating data from many individuals. The assumption is that users with similar preferences will rate items similarly. Thus missing ratings for a user can be predicted by first finding a *neighborhood* of similar users and then aggregate the ratings of these users to form a prediction.

The neighborhood is defined in terms of similarity between users, either by taking a given number of most similar users (k nearest neighbors) or all users within a given similarity threshold. Popular similarity measures for CF are the *Pearson correlation coefficient* and the *Cosine similarity*. These measures are defined between two vectors with ratings \mathbf{x} and \mathbf{y} .

$$m_{\text{Pearson}}(\mathbf{x}, \mathbf{y}) = \frac{1}{n-1} \sum_{l=1}^n \left(\frac{x_l - \bar{\mathbf{x}}}{s_x} \right) \left(\frac{y_l - \bar{\mathbf{y}}}{s_y} \right) \quad (1)$$

and

$$m_{\text{Cosine}}(\mathbf{x}, \mathbf{y}) = \frac{\mathbf{x} \cdot \mathbf{y}}{\|\mathbf{x}\| \|\mathbf{y}\|}, \quad (2)$$

where n is the number of elements in the rating vectors and missing ratings are skipped in the calculation. s_x and s_y is the standard deviation and $\|\cdot\|$ is the l^2 -norm of a vector. To calculate the measure between two users, u_x and u_y , $\mathbf{x} = \mathbf{r}_x$ and $\mathbf{y} = \mathbf{r}_y$ represent the row vectors in \mathbf{R} with the two users' profile vectors are used. For calculating similarity using rating data only the dimensions (items) are used which were rated by both users. Note that cosine and correlation are in the range $[-1, 1]$, but similarity measures need to be in the range of $[0, 1]$. We, use the transformation

$$s = \frac{1}{2}m + 1.$$

Using the similarity, the neighborhood for the active user $\mathcal{N}(a) \subset \mathcal{U}$ can be selected by either a threshold on the similarity or by taking the k nearest neighbors. Once the users in the neighborhood are found, their ratings are aggregated to form the predicted rating for the active user u_a . The easiest form is to just average the ratings in the neighborhood. For item i_l this is

$$\hat{r}_{al} = \frac{1}{|\mathcal{N}(a)|} \sum_{i \in \mathcal{N}(a)} r_{il}. \quad (3)$$

An example of the process of creating recommendations by user-based CF is shown in [Figure 1](#). To the left is the rating matrix \mathbf{R} with 6 users and 8 items and ratings in the range 1 to 5 (stars). We want to create recommendations for the active user u_a shown at the bottom of the matrix. To find the k -neighborhood (i.e., the k nearest neighbors) we calculate the similarity between the active user and all other users based on their ratings in the database

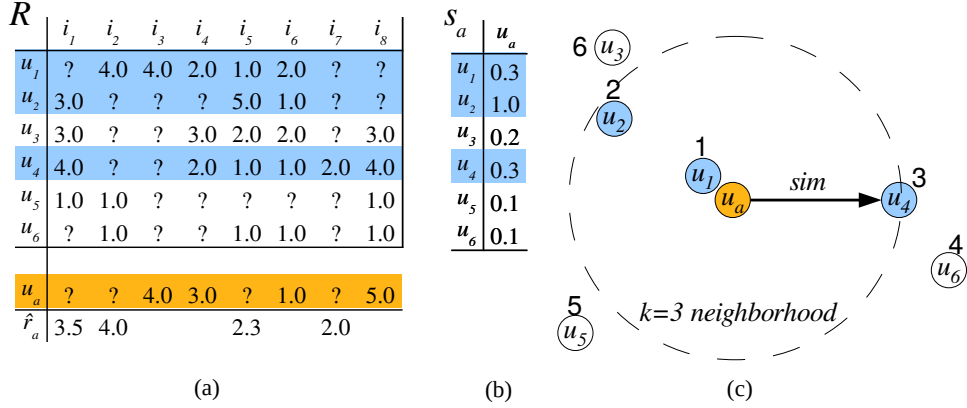


Figure 1: User-based collaborative filtering example with (a) rating matrix R and estimated ratings for the active user, (b), similarities between the active user and the other users s_a (Euclidean distance converted to similarities), and (b) the user neighborhood formation.

and then select the k users with the highest similarity. To the right in Figure 1 we see a 2-dimensional representation of the similarities (users with higher similarity are displayed closer) with the active user in the center. The $k = 3$ nearest neighbors (u_1, u_2 and u_3) are selected and marked in the database to the left. To generate an aggregated estimated rating, we compute the average ratings in the neighborhood for each item not rated by the active user. To create a top- N recommendation list, the items are ordered by predicted rating. In the small example in Figure 1 the order in the top- N list (with $N \geq 4$) is i_2, i_1, i_7 and i_5 . However, for a real application we probably would not recommend items i_7 and i_5 because of their low ratings.

The fact that some users in the neighborhood are more similar to the active user than others (see Figure 1 (b)) can be incorporated as weights into Equation (3).

$$\hat{r}_{al} = \frac{1}{\sum_{i \in \mathcal{N}(a)} s_{ai}} \sum_{i \in \mathcal{N}(a)} s_{ai} r_{il} \quad (4)$$

s_{ai} is the similarity between the active user u_a and user u_i in the neighborhood.

For rating data, the performance of the recommender algorithm can be improved by removing user rating bias where some users tend to always use higher ratings while others tend to use lower ratings. This can be done by normalizing the rating data before applying the recommender algorithm. Any normalization function $h : \mathbb{R}^{n \times m} \mapsto \mathbb{R}^{n \times m}$ can be used for preprocessing. Such a function needs to be reversible by h^{-1} to map the predicted rating on the normalized scale back to the original rating scale. Normalization is used to remove individual rating bias by users who consistently always use lower or higher ratings than other users. The most popular method is to center the rows of the user-item rating matrix by

$$h(r_{jl}) = r_{jl} - \bar{r}_j,$$

where \bar{r}_j is the mean of all available ratings in row j of the user-item rating matrix \mathbf{R} . This means that ratings are now measured for each user by how much they are above or below the user's average rating. The inverse is simply,

S	i_1	i_2	i_3	i_4	i_5	i_6	i_7	i_8	\hat{r}_a	$k=3$
i_1	-	0.1	0	0.3	0.2	0.4	0	0.1	-	
i_2	0.1	-	0.8	0.9	0	0.2	0.1	0	0.0	
i_3	0	0.8	-	0	0.4	0.1	0.3	0.5	4.6	
i_4	0.3	0.9	0	-	0	0.1	0	0.2	3.2	
i_5	0.2	0	0.4	0	-	0.1	0.2	0.1	-	
i_6	0.4	0.2	0.1	0.3	0.1	-	0	0.1	2.0	
i_7	0	0.1	0.3	0	0.2	0	-	0	4.0	
i_8	0.1	0	0.5	0.2	0.1	0.1	0	-	-	
u_a	2	?	?	?	4	?	?	5		

Figure 2: Item-based collaborative filtering

$$h^{-1}(h(r_{jl})) = h(r_{jl}) + \bar{r}_j = r_{jl}.$$

Other methods like Z-score normalization which also takes rating variance into account can be found in the literature (see, e.g., [Desrosiers and Karypis 2011](#)).

The two main problems of user-based CF are that the whole user database has to be kept in memory and that expensive similarity computation between the active user and all other users in the database has to be performed.

2.2. Item-based Collaborative Filtering

Item-based CF ([Kitts et al. 2000](#); [Sarwar et al. 2001](#); [Linden et al. 2003](#); [Deshpande and Karypis 2004](#)) is a model-based approach which produces recommendations based on the relationship between items inferred from the rating matrix. The assumption behind this approach is that users will prefer items that are similar to other items they like.

The model-building step consists of calculating a similarity matrix containing all item-to-item similarities using a given similarity measure. Popular are again Pearson correlation and Cosine similarity and Equations 1 and 2 are used. Here the rating vectors x and y are columns of \mathbf{R} representing the ratings for two items.

All pairwise similarities are stored in a $n \times n$ similarity matrix \mathbf{S} . To reduce the model size to $n \times k$ with $k \ll n$, for each item only a list of the k most similar items and their similarity values are stored. The k items which are most similar to item i_l is denoted by the set $\mathcal{S}(l)$ which can be seen as the neighborhood of size k of the item. Retaining only k similarities per item improves the space and time complexity significantly but potentially sacrifices some recommendation quality ([Sarwar et al. 2001](#)).

To make a recommendation based on the model we use the similarities to calculate a weighted sum of the user's ratings for related items.

$$\hat{r}_{al} = \frac{1}{\sum_{i \in \mathcal{S}(l)} s_{li}} \sum_{i \in \mathcal{S}(l)} s_{li} r_{ai} \quad (5)$$

Figure 2 shows an example for $n = 8$ items with $k = 3$. For the similarity matrix \mathbf{S} only

the $k = 3$ largest entries are stored per row (these entries are marked using bold face). For the example we assume that we have ratings for the active user for items i_1, i_5 and i_8 . The rows corresponding to these items are highlighted in the item similarity matrix. We can now compute the weighted sum using the similarities (only the reduced matrix with the $k = 3$ highest ratings is used) and the user's ratings. The result (below the matrix) shows that i_3 has the highest estimated rating for the active user.

Similar to user-based recommender algorithms, user-bias can be reduced by first normalizing the user-item rating matrix before computing the item-to-item similarity matrix.

Item-based CF is more efficient than user-based CF since the model (reduced similarity matrix) is relatively small ($N \times k$) and can be fully precomputed. Item-based CF is known to only produce slightly inferior results compared to user-based CF and higher order models which take the joint distribution of sets of items into account are possible (Deshpande and Karypis 2004). Furthermore, item-based CF is successfully applied in large scale recommender systems (e.g., by Amazon.com).

2.3. User and Item-Based CF using 0-1 Data

Less research is available for situations where no large amount of detailed directly elicited rating data is available. However, this is a common situation and occurs when users do not want to directly reveal their preferences by rating an item (e.g., because it is too time consuming). In this case preferences can only be inferred by analyzing usage behavior. For example, we can easily record in a supermarket setting what items a customer purchases. However, we do not know why other products were not purchased. The reason might be one of the following.

- The customer does not need the product right now.
- The customer does not know about the product. Such a product is a good candidate for recommendation.
- The customer does not like the product. Such a product should obviously not be recommended.

Mild and Reutterer (2003) and Lee, Jun, Lee, and Kim (2005) present and evaluate recommender algorithms for this setting. The same reasoning is true for recommending pages of a web site given click-stream data. Here we only have information about which pages were viewed but not why some pages were not viewed. This situation leads to binary data or more exactly to 0-1 data where 1 means that we inferred that the user has a preference for an item and 0 means that either the user does not like the item or does not know about it. Pan, Zhou, Cao, Liu, Lukose, Scholz, and Yang (2008) call this type of data in the context of collaborative filtering analogous to similar situations for classifiers *one-class data* since only the 1-class is pure and contains only positive examples. The 0-class is a mixture of positive and negative examples.

In the 0-1 case with $r_{jl} \in 0, 1$ where we define:

$$r_{jl} = \begin{cases} 1 & \text{user } u_j \text{ is known to have a preference for item } i_l \\ 0 & \text{otherwise.} \end{cases} \quad (6)$$

Two strategies to deal with one-class data is to assume all missing ratings (zeros) are negative examples or to assume that all missing ratings are unknown. In addition, Pan *et al.* (2008) propose strategies which represent a trade-off between the two extreme strategies based on wighted low rank approximations of the rating matrix and on negative example sampling which might improve results across all recommender algorithms.

If we assume that users typically favor only a small fraction of the items and thus most items with no rating will be indeed negative examples. then we have no missing values and can use the approaches described above for real valued rating data. However, if we assume all zeroes are missing values, then this lead to the problem that we cannot compute similarities using Pearson correlation or Cosine similarity since the not missing parts of the vectors only contains ones. A similarity measure which only focuses on matching ones and thus prevents the problem with zeroes is the *Jaccard index*:

$$\text{sim}_{\text{Jaccard}}(\mathcal{X}, \mathcal{Y}) = \frac{|\mathcal{X} \cap \mathcal{Y}|}{|\mathcal{X} \cup \mathcal{Y}|}, \quad (7)$$

where \mathcal{X} and \mathcal{Y} are the sets of the items with a 1 in user profiles u_a and u_b , respectively. The Jaccard index can be used between users for user-based filtering and between items for item-based filtering as described above.

2.4. Recommendations for 0-1 Data Based on Association Rules

Recommender systems using association rules produce recommendations based on a dependency model for items given by a set of association rules (Fu *et al.* 2000; Mobasher *et al.* 2001; Geyer-Schulz *et al.* 2002; Lin *et al.* 2002; Demiriz 2004). The binary profile matrix \mathbf{R} is seen as a database where each user is treated as a transaction that contains the subset of items in \mathcal{I} with a rating of 1. Hence transaction k is defined as $\mathcal{T}_k = \{i_j \in \mathcal{I} | r_{jk} = 1\}$ and the whole transaction data base is $\mathcal{D} = \{\mathcal{T}_1, \mathcal{T}_2, \dots, \mathcal{T}_U\}$ where U is the number of users. To build the dependency model, a set of association rules \mathcal{R} is mined from \mathbf{R} . Association rules are rules of the form $\mathcal{X} \rightarrow \mathcal{Y}$ where $\mathcal{X}, \mathcal{Y} \subseteq \mathcal{I}$ and $\mathcal{X} \cap \mathcal{Y} = \emptyset$. For the model we only use association rules with a single item in the right-hand-side of the rule ($|\mathcal{Y}| = 1$). To select a set of useful association rules, thresholds on measures of significance and interestingness are used. Two widely applied measures are:

$$\text{support}(\mathcal{X} \rightarrow \mathcal{Y}) = \text{support}(\mathcal{X} \cup \mathcal{Y}) = \text{Freq}(\mathcal{X} \cup \mathcal{Y}) / |\mathcal{D}| = \hat{P}(E_{\mathcal{X} \cup \mathcal{Y}})$$

$$\text{confidence}(\mathcal{X} \rightarrow \mathcal{Y}) = \text{support}(\mathcal{X} \cup \mathcal{Y}) / \text{support}(\mathcal{X}) = \hat{P}(E_{\mathcal{Y}} | E_{\mathcal{X}})$$

$\text{Freq}(\mathcal{I})$ gives the number of transactions in the data base \mathcal{D} that contains all items in \mathcal{I} . $E_{\mathcal{I}}$ is the event that the itemset \mathcal{I} is contained in a transaction.

We now require $\text{support}(\mathcal{X} \rightarrow \mathcal{Y}) > s$ and $\text{confidence}(\mathcal{X} \rightarrow \mathcal{Y}) > c$ and also include a length constraint $|\mathcal{X} \cup \mathcal{Y}| \leq l$. The set of rules \mathcal{R} that satisfy these constraints form the dependency model. Although finding all association rules given thresholds on support and confidence is a hard problem (the model grows in the worse case exponential with the number of items), algorithms that efficiently find all rules in most cases are available (e.g., Agrawal and Srikant 1994; Zaki 2000; Han, Pei, Yin, and Mao 2004). Also model size can be controlled by l , s and c .

To make a recommendation for an active user u_a given the set of items \mathcal{T}_a the user likes and the set of association rules \mathcal{R} (dependency model), the following steps are necessary:

1. Find all matching rules $\mathcal{X} \rightarrow \mathcal{Y}$ for which $\mathcal{X} \subseteq \mathcal{T}_a$ in \mathcal{R} .
2. Recommend N unique right-hand-sides (\mathcal{Y}) of the matching rules with the highest confidence (or another measure of interestingness).

The dependency model is very similar to item-based CF with conditional probability-based similarity (Deshpande and Karypis 2004). It can be fully precomputed and rules with more than one items in the left-hand-side (\mathcal{X}), it incorporates higher order effects between more than two items.

2.5. Other collaborative filtering methods

Over time several other model-based approaches have been developed. A popular simple item-based approach is the *Slope One* algorithm (Lemire and Maclachlan 2005). Another family of algorithms is based on latent factors approach using matrix decomposition (Koren et al. 2009). More recently, deep learning has become a very popular method for flexible matrix completion, matrix factorization and collaborative ranking. A comprehensive survey is presented by Zhang, Yao, Sun, and Tay (2019).

These algorithms are outside the scope of this introductory paper.

3. Evaluation of Recommender Algorithms

Evaluation of recommender systems is an important topic and reviews were presented by Herlocker, Konstan, Terveen, and Riedl (2004) and Gunawardana and Shani (2009). Typically, given a rating matrix \mathbf{R} , recommender algorithms are evaluated by first partitioning the users (rows) in \mathbf{R} into two sets $\mathcal{U}_{train} \cup \mathcal{U}_{test} = \mathcal{U}$. The rows of \mathbf{R} corresponding to the training users \mathcal{U}_{train} are used to learn the recommender model. Then each user $u_a \in \mathcal{U}_{test}$ is seen as an active user. Before creating recommendations some items are withheld from the profile r_{u_a} . and it measured either how well the predicted rating matches the withheld value or, for top- N algorithms, if the items in the recommended list are rated highly by the user. Finally, the evaluation measures calculated for all test users are averaged.

To determine how to split \mathcal{U} into \mathcal{U}_{train} and \mathcal{U}_{test} we can use several approaches (Kohavi 1995).

- **Splitting:** We can randomly assign a predefined proportion of the users to the training set and all others to the test set.
- **Bootstrap sampling:** We can sample from \mathcal{U}_{test} with replacement to create the training set and then use the users not in the training set as the test set. This procedure has the advantage that for smaller data sets we can create larger training sets and still have users left for testing.
- **k -fold cross-validation:** Here we split \mathcal{U} into k sets (called folds) of approximately the same size. Then we evaluate k times, always using one fold for testing and all other folds for leaning. The k results can be averaged. This approach makes sure that each user is at least once in the test set and the averaging produces more robust results and error estimates.

Table 2: 2x2 confusion matrix

actual / predicted	negative	positive
negative	a	b
positive	c	d

The items withheld in the test data are randomly chosen. Breese *et al.* (1998) introduced the four experimental protocols called *Given 2*, *Given 5*, *Given 10* and *All-but-1*. For the *Given x* protocols for each user x randomly chosen items are given to the recommender algorithm and the remaining items are withheld for evaluation. For *All but x* the algorithm gets all but x withheld items.

In the following we discuss the evaluation of predicted ratings and then of top- N recommendation lists.

3.1. Evaluation of predicted ratings

A typical way to evaluate a prediction is to compute the deviation of the prediction from the true value. This is the basis for the *Mean Average Error (MAE)*

$$\text{MAE} = \frac{1}{|\mathcal{K}|} \sum_{(j,l) \in \mathcal{K}} |r_{jl} - \hat{r}_{jl}|, \quad (8)$$

where \mathcal{K} is the set of all user-item pairings (j, l) for which we have a predicted rating \hat{r}_{jl} and a known rating r_{jl} which was not used to learn the recommendation model.

Another popular measure is the *Root Mean Square Error (RMSE)*.

$$\text{RMSE} = \sqrt{\frac{\sum_{(j,l) \in \mathcal{K}} (r_{jl} - \hat{r}_{jl})^2}{|\mathcal{K}|}} \quad (9)$$

RMSE penalizes larger errors stronger than MAE and thus is suitable for situations where small prediction errors are not very important.

3.2. Evaluation Top- N recommendations

The items in the predicted top- N lists and the withheld items liked by the user (typically determined by a simple threshold on the actual rating) for all test users \mathcal{U}_{test} can be aggregated into a so called *confusion matrix* depicted in table 2 (see Kohavi and Provost (1998)) which corresponds exactly to the outcomes of a classical statistical experiment. The confusion matrix shows how many of the items recommended in the top- N lists (column predicted positive; $d + b$) were withheld items and thus correct recommendations (cell d) and how many were potentially incorrect (cell b). The matrix also shows how many of the not recommended items (column predicted negative; $a + c$) should have actually been recommended since they represent withheld items (cell c).

From the confusion matrix several performance measures can be derived. For the data mining task of a recommender system the performance of an algorithm depends on its ability to learn significant patterns in the data set. Performance measures used to evaluate these algorithms

have their root in machine learning. A commonly used measure is *accuracy*, the fraction of correct recommendations to total possible recommendations.

$$Accuracy = \frac{\text{correct recommendations}}{\text{total possible recommendations}} = \frac{a + d}{a + b + c + d} \quad (10)$$

A common error measure is the *mean absolute error* (*MAE*, also called *mean absolute deviation* or *MAD*).

$$MAE = \frac{1}{N} \sum_{i=1}^N |\epsilon_i| = \frac{b + c}{a + b + c + d}, \quad (11)$$

where $N = a + b + c + d$ is the total number of items which can be recommended and $|\epsilon_i|$ is the absolute error of each item. Since we deal with 0-1 data, $|\epsilon_i|$ can only be zero (in cells a and d in the confusion matrix) or one (in cells b and c). For evaluation recommender algorithms for rating data, the root mean square error is often used. For 0-1 data it reduces to the square root of MAE.

Recommender systems help to find items of interest from the set of all available items. This can be seen as a retrieval task known from information retrieval. Therefore, standard information retrieval performance measures are frequently used to evaluate recommender performance. *Precision* and *recall* are the best known measures used in information retrieval (Salton and McGill 1983; van Rijsbergen 1979).

$$Precision = \frac{\text{correctly recommended items}}{\text{total recommended items}} = \frac{d}{b + d} \quad (12)$$

$$Recall = \frac{\text{correctly recommended items}}{\text{total useful recommendations}} = \frac{d}{c + d} \quad (13)$$

Often the number of *total useful recommendations* needed for recall is unknown since the whole collection would have to be inspected. However, instead of the actual *total useful recommendations* often the total number of known useful recommendations is used. Precision and recall are conflicting properties, high precision means low recall and vice versa. To find an optimal trade-off between precision and recall a single-valued measure like the *E-measure* (van Rijsbergen 1979) can be used. The parameter α controls the trade-off between precision and recall.

$$E\text{-measure} = \frac{1}{\alpha(1/Precision) + (1 - \alpha)(1/Recall)} \quad (14)$$

A popular single-valued measure is the *F-measure*. It is defined as the harmonic mean of precision and recall.

$$F\text{-measure} = \frac{2 Precision Recall}{Precision + Recall} = \frac{2}{1/Precision + 1/Recall} \quad (15)$$

It is a special case of the E-measure with $\alpha = .5$ which places the same weight on both, precision and recall. In the recommender evaluation literature the F-measure is often referred to as the measure *F1*.

Another method used in the literature to compare two classifiers at different parameter settings is the *Receiver Operating Characteristic (ROC)*. The method was developed for signal

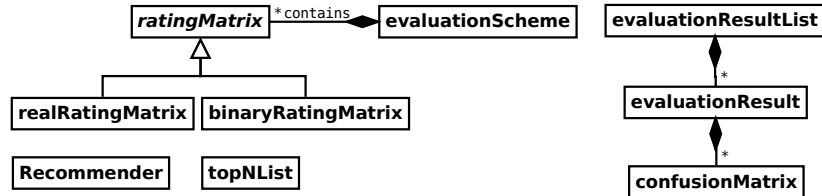


Figure 3: UML class diagram for package **recommenderlab** (Fowler 2004).

detection and goes back to the Swets model (van Rijsbergen 1979). The ROC-curve is a plot of the system's *probability of detection* (also called *sensitivity* or true positive rate TPR which is equivalent to recall as defined in formula 13) by the *probability of false alarm* (also called false positive rate FPR or $1 - \textit{specificity}$, where $\textit{specificity} = \frac{a}{a+b}$) with regard to model parameters. A possible way to compare the efficiency of two systems is by comparing the size of the area under the ROC-curve, where a bigger area indicates better performance.

4. Recommenderlab Infrastructure

recommenderlab is implemented using formal classes in the S4 class system. Figure 3 shows the main classes and their relationships.

The package uses the abstract `ratingMatrix` to provide a common interface for rating data. `ratingMatrix` implements many methods typically available for matrix-like objects. For example, `dim()`, `dimnames()`, `colCounts()`, `rowCounts()`, `colMeans()`, `rowMeans()`, `colSums()` and `rowSums()`. Additionally `sample()` can be used to sample from users (rows) and `image()` produces an image plot.

For `ratingMatrix` we provide two concrete implementations `realRatingMatrix` and `binaryRatingMatrix` to represent different types of rating matrices **R**. `realRatingMatrix` implements a rating matrix with real valued ratings stored in sparse format defined in package **Matrix**. Sparse matrices in **Matrix** typically do not store 0s explicitly, however for `realRatingMatrix` we use these sparse matrices such that instead of 0s, NAs are not explicitly stored.

`binaryRatingMatrix` implements a 0-1 rating matrix using the implementation of `itemMatrix` defined in package **arules**. `itemMatrix` stores only the ones and internally uses a sparse representation from package **Matrix**. With this class structure **recommenderlab** can be easily extended to other forms of rating matrices with different concepts for efficient storage in the future.

Class `Recommender` implements the data structure to store recommendation models. The creator method

```
Recommender(data, method, parameter = NULL)
```

takes data as a `ratingMatrix`, a method name and some optional parameters for the method and returns a `Recommender` object. Once we have a recommender object, we can predict top- N recommendations for active users using

```
predict(object, newdata, n=10, type=c("topNList", "ratings", "ratingMatrix"),
        ...).
```

`Predict` can return either top- N lists (default setting) or predicted ratings. `object` is the recommender object, `newdata` is the data for the active users. For top- N lists `n` is the maximal number of recommended items in each list and `predict()` will return an objects of class `topNList` which contains one top- N list for each active user. For `"ratings"` and `"ratingMatrix"`, `n` is ignored and an object of `realRatingMatrix` is returned. Each row contains the predicted ratings for one active user. The difference is, that for `"ratings"`, the items for which a rating exists in `newdata` have a `NA` instead of a predicted/actual ratings.

The actual implementations for the recommendation algorithms are managed using the registry mechanism provided by package `registry`. The registry called `recommenderRegistry` and stores recommendation method names and a short description. Generally, the registry mechanism is hidden from the user and the creator function `Recommender()` uses it in the background to map a recommender method name to its implementation. However, the registry can be directly queried by

```
recommenderRegistry$get_entries()
```

and new recommender algorithms can be added by the user. We will give an example for this feature in the examples section of this paper.

To evaluate recommender algorithms package `recommenderlab` provides the infrastructure to create and maintain evaluation schemes stored as an object of class `evaluationScheme` from rating data. The creator function

```
evaluationScheme(data, method="split", train=0.9, k=10, given=3)
```

creates the evaluation scheme from a data set using a method (e.g., simple split, bootstrap sampling, k -fold cross validation). Testing is performed by withholding items (parameter `given`). Breese *et al.* (1998) introduced the four experimental withholding protocols called *Given 2*, *Given 5*, *Given 10* and *All-but-1*. During testing, the *Given x* protocol presents the algorithm with only x randomly chosen items for the test user, and the algorithm is evaluated by how well it is able to predict the withheld items. For *All-but- x* , a generalization of *All-but-1*, the algorithm sees all but x withheld ratings for the test user. `given` controls x in the evaluations scheme. Positive integers result in a *Given x* protocol, while negative values produce a *All-but- x* protocol.

The function `evaluate()` is then used to evaluate several recommender algorithms using an evaluation scheme resulting in a evaluation result list (class `evaluationResultList`) with one entry (class `evaluationResult`) per algorithm. Each object of `evaluationResult` contains one or several object of `confusionMatrix` depending on the number of evaluations specified in the `evaluationScheme` (e.g., k for k -fold cross validation). With this infrastructure several recommender algorithms can be compared on a data set with a single line of code.

In the following, we will illustrate the usage of **recommenderlab** with several examples.

5. Examples

This first few examples show how to manage data in recommender lab and then we create and evaluate recommenders. First, we load the package.

```
R> library("recommenderlab")
```

5.1. Coercion to and from rating matrices

For this example we create a small artificial data set as a matrix.

```
R> m <- matrix(sample(c(as.numeric(0:5), NA), 50,
+   replace=TRUE, prob=c(rep(.4/6,6),.6)), ncol=10,
+   dimnames=list(user=paste("u", 1:5, sep=''),
+   item=paste("i", 1:10, sep=''))))
R> m
```

```
      item
user i1 i2 i3 i4 i5 i6 i7 i8 i9 i10
u1  NA  2  3  5 NA  5 NA  4 NA  NA
u2   2 NA NA NA NA NA NA NA  2  3
u3   2 NA NA NA NA  1 NA NA NA  NA
u4   2  2  1 NA NA  5 NA  0  2  NA
u5   5 NA NA NA NA NA NA  5 NA  4
```

With coercion, the matrix can be easily converted into a `realRatingMatrix` object which stores the data in sparse format (only non-NA values are stored explicitly; NA values are represented by a dot).

```
R> r <- as(m, "realRatingMatrix")
R> r
```

```
5 x 10 rating matrix of class 'realRatingMatrix' with 19 ratings.
```

```
R> getRatingMatrix(r)
```

```
5 x 10 sparse Matrix of class "dgCMatrix"
```

```
u1 . 2 3 5 . 5 . 4.000e+00 . .
u2 2 . . . . . . . . 2 3
u3 2 . . . . 1 . . . .
u4 2 2 1 . . 5 . 2.225e-308 2 .
u5 5 . . . . . . 5.000e+00 . 4
```

The `realRatingMatrix` can be coerced back into a matrix which is identical to the original matrix.

```
R> identical(as(r, "matrix"),m)
```

```
[1] TRUE
```

It can also be coerced into a list of users with their ratings for closer inspection or into a `data.frame` with user/item/rating tuples.

```
R> as(r, "list")
```

```
$`0`
```

```
i2 i3 i4 i6 i8
  2  3  5  5  4
```

```
$`1`
```

```
i1 i9 i10
  2  2  3
```

```
$`2`
```

```
i1 i6
  2  1
```

```
$`3`
```

```
          i1          i2          i3          i6          i8          i9
2.000e+00 2.000e+00 1.000e+00 5.000e+00 2.225e-308 2.000e+00
```

```
$`4`
```

```
i1 i8 i10
  5  5  4
```

```
R> head(as(r, "data.frame"))
```

	user	item	rating
5	u1	i2	2
7	u1	i3	3
9	u1	i4	5
10	u1	i6	5
13	u1	i8	4
1	u2	i1	2

The `data.frame` version is especially suited for writing rating data to a file (e.g., by `write.csv()`). Coercion from `data.frame` (user/item/rating tuples) and list into a sparse rating matrix is also provided. This way, external rating data can easily be imported into **recommenderlab**.

5.2. Normalization

An important operation for rating matrices is to normalize the entries to, e.g., centering to remove rating bias by subtracting the row mean from all ratings in the row. This is can be easily done using `normalize()`.

```
R> r_m <- normalize(r)
R> r_m
```

```
5 x 10 rating matrix of class 'realRatingMatrix' with 19 ratings.
Normalized using center on rows.
```

```
R> getRatingMatrix(r_m)
```

```
5 x 10 sparse Matrix of class "dgCMatrix"
```

```
u1 . -1.800e+00 -0.8 1.2 . 1.2 . 0.2000 . .
u2 -3.333e-01 . . . . . . . -3.333e-01 0.6667
u3 5.000e-01 . . . . -0.5 . . . .
u4 2.225e-308 2.225e-308 -1.0 . . 3.0 . -2.0000 2.225e-308 .
u5 3.333e-01 . . . . . . 0.3333 . -0.6667
```

Normalization can be reversed using `denormalize()`.

```
R> denormalize(r_m)
```

```
5 x 10 rating matrix of class 'realRatingMatrix' with 19 ratings.
```

Small portions of rating matrices can be visually inspected using `image()`.

```
R> image(r, main = "Raw Ratings")
R> image(r_m, main = "Normalized Ratings")
```

Figure 4 shows the resulting plots.

5.3. Binarization of data

A matrix with real valued ratings can be transformed into a 0-1 matrix with `binarize()` and a user specified threshold (`min_ratings`) on the raw or normalized ratings. In the following only items with a rating of 4 or higher will become a positive rating in the new binary rating matrix.

```
R> r_b <- binarize(r, minRating=4)
R> r_b
```

```
5 x 10 rating matrix of class 'binaryRatingMatrix' with 7 ratings.
```

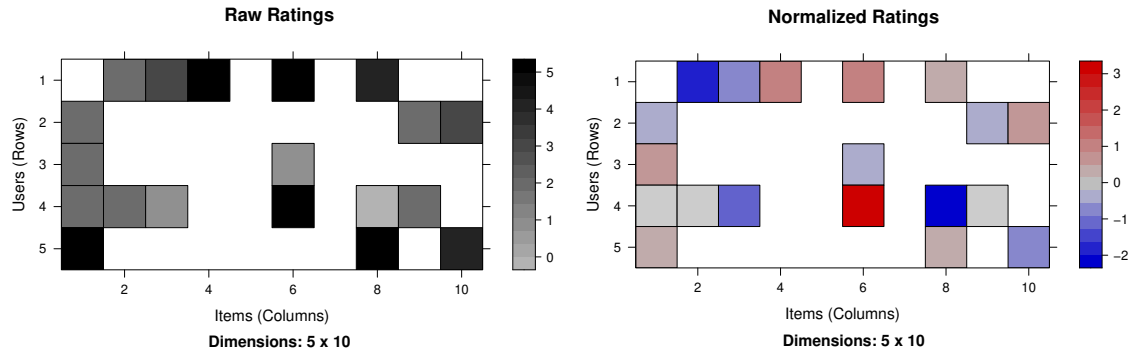


Figure 4: Image plot the artificial rating data before and after normalization.

```
R> as(r_b, "matrix")
```

```
      i1  i2  i3  i4  i5  i6  i7  i8  i9  i10
u1 FALSE FALSE FALSE TRUE FALSE TRUE FALSE TRUE FALSE FALSE
u2 FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE
u3 FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE
u4 FALSE FALSE FALSE FALSE FALSE TRUE FALSE FALSE FALSE FALSE
u5 TRUE FALSE FALSE FALSE FALSE FALSE FALSE TRUE FALSE TRUE
```

5.4. Inspection of data set properties

We will use the data set Jester5k for the rest of this section. This data set comes with **recommenderlab** and contains a sample of 5000 users from the anonymous ratings data from the Jester Online Joke Recommender System collected between April 1999 and May 2003 (Goldberg, Roeder, Gupta, and Perkins 2001). The data set contains ratings for 100 jokes on a scale from -10 to $+10$. All users in the data set have rated 36 or more jokes.

```
R> data(Jester5k)
R> Jester5k
```

5000 x 100 rating matrix of class 'realRatingMatrix' with 363209 ratings.

Jester5k contains 363209 ratings. For the following examples we use only a subset of the data containing a sample of 1000 users (we set the random number generator seed for reproducibility). For random sampling `sample()` is provided for rating matrices.

```
R> set.seed(1234)
R> r <- sample(Jester5k, 1000)
R> r
```

1000 x 100 rating matrix of class 'realRatingMatrix' with 74323 ratings.

This subset still contains 74323 ratings. Next, we inspect the ratings for the first user. We can select an individual user with the extraction operator.

```
R> rowCounts(r[1,])
```

```
u20648
      74
```

```
R> as(r[1,], "list")
```

```
$`0`
  j1   j2   j3   j4   j5   j6   j7   j8   j9  j10  j11  j12
-2.86 1.75 -4.03 -5.78 2.23 -5.44 -3.40 8.74 -4.51 3.74 0.15 -0.39
  j13  j14  j15  j16  j17  j18  j19  j20  j21  j22  j23  j24
-1.94 5.97 -7.77 1.26 2.18 -2.14 1.17 -8.64 -1.36 1.21 4.95 -9.81
  j25  j26  j27  j28  j29  j30  j31  j32  j33  j34  j35  j36
-3.35 3.01 2.33 1.36 9.08 -7.72 -9.42 0.97 -5.83 -0.83 6.36 3.54
  j37  j38  j39  j40  j41  j42  j43  j44  j45  j46  j47  j48
-3.64 0.87 2.23 3.54 -7.96 -1.41 2.62 -8.45 -0.29 -9.76 -4.47 3.11
  j49  j50  j51  j52  j53  j54  j55  j56  j57  j58  j59  j60
6.26 4.95 -9.17 -8.01 5.49 -5.97 1.70 5.00 4.13 -2.18 0.49 2.77
  j61  j62  j63  j64  j65  j66  j67  j68  j69  j70  j72  j81
-3.01 8.35 -2.77 -3.25 5.39 5.49 -1.31 -3.74 2.96 0.15 4.81 5.15
  j85  j92
2.23 -8.40
```

```
R> rowMeans(r[1,])
```

```
u20648
-0.4232
```

The user has rated 74 jokes, the list shows the ratings and the user's rating average is -0.423243243243243 .

Next, we look at several distributions to understand the data better. `getRatings()` extracts a vector with all non-missing ratings from a rating matrix.

```
R> hist(getRatings(r), breaks=100)
```

In the histogram in Figure 5 shoes an interesting distribution where all negative values occur with a almost identical frequency and the positive ratings more frequent with a steady decline towards the rating 10. Since this distribution can be the result of users with strong rating bias, we look next at the rating distribution after normalization.

```
R> hist(getRatings(normalize(r)), breaks=100)
```

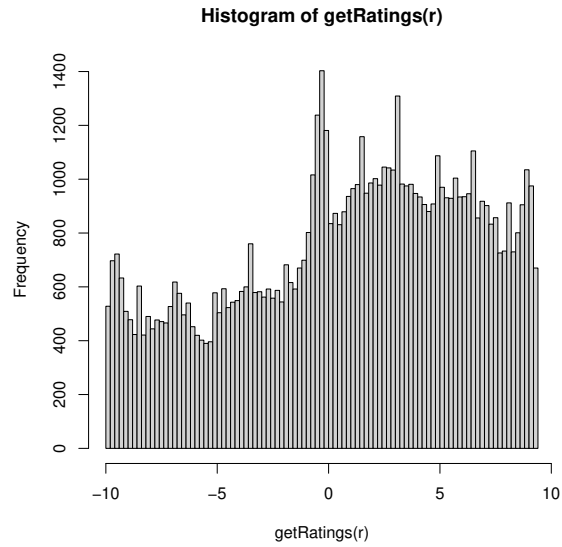


Figure 5: Raw rating distribution for as sample of Jester.

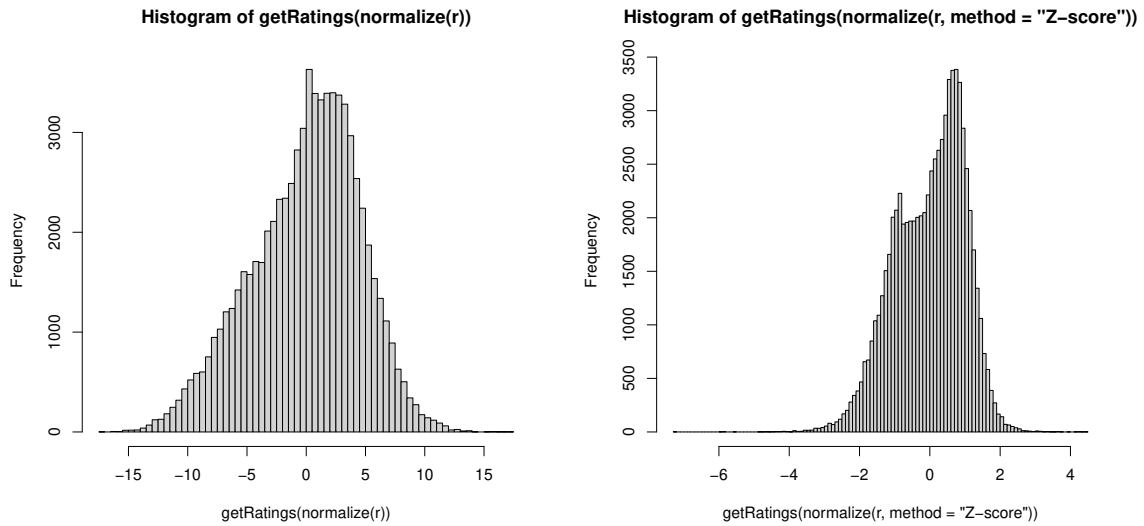


Figure 6: Histogram of normalized ratings using row centering (left) and Z-score normalization (right).

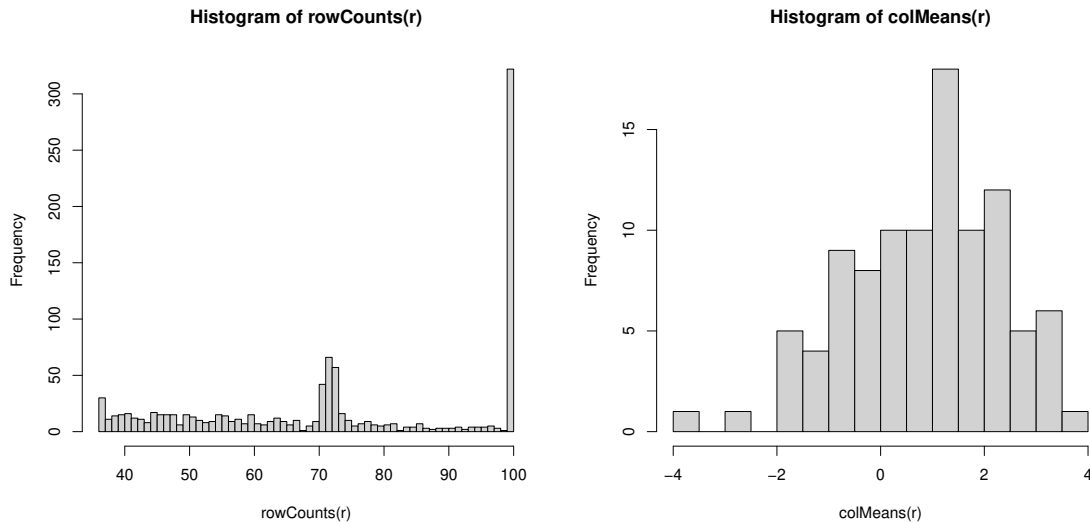


Figure 7: Distribution of the number of rated items per user (left) and of the average ratings per joke (right).

```
R> hist(getRatings(normalize(r, method="Z-score")), breaks=100)
```

Figure 6 shows that the distribution of ratings is closer to a normal distribution after row centering and Z-score normalization additionally reduces the variance to a range of roughly -3 to $+3$ standard deviations. It is interesting to see that there is a pronounced peak of ratings between zero and two.

Finally, we look at how many jokes each user has rated and what the mean rating for each Joke is.

```
R> hist(rowCounts(r), breaks=50)
```

```
R> hist(colMeans(r), breaks=20)
```

Figure 7 shows that there are unusually many users with ratings around 70 and users who have rated all jokes. The average ratings per joke look closer to a normal distribution with a mean above 0.

5.5. Creating a recommender

A recommender is created using the creator function `Recommender()`. Available recommendation methods are stored in a registry. The registry can be queried. Here we are only interested in methods for real-valued rating data.

```
R> recommenderRegistry$get_entries(dataType = "realRatingMatrix")
```

```
$HYBRID_realRatingMatrix
```

```
Recommender method: HYBRID for realRatingMatrix Description:
```

Hybrid recommender that aggregates several recommendation strategies using weighted averages. Reference: NA

Parameters:

```
recommenders weights aggregation_type
1          NULL      NULL          "sum"
```

`$ALS_realRatingMatrix`

Recommender method: ALS for realRatingMatrix Description:

Recommender for explicit ratings based on latent factors, calculated by alternating least squares algorithm. Reference: Yunhong Zhou, Dennis Wilkinson, Robert Schreiber, Rong Pan (2008). Large-Scale Parallel Collaborative Filtering for the Netflix Prize, 4th Int'l Conf. Algorithmic Aspects in Information and Management, LNCS 5034.

Parameters:

```
normalize lambda n_factors n_iterations min_item_nr seed
1          NULL    0.1          10          10          1 NULL
```

`$ALS_implicit_realRatingMatrix`

Recommender method: ALS_implicit for realRatingMatrix Description:

Recommender for implicit data based on latent factors, calculated by alternating least squares algorithm. Reference: Yifan Hu, Yehuda Koren, Chris Volinsky (2008). Collaborative Filtering for Implicit Feedback Datasets, ICDM '08 Proceedings of the 2008 Eighth IEEE International Conference on Data Mining, pages 263-272.

Parameters:

```
lambda alpha n_factors n_iterations min_item_nr seed
1    0.1    10          10          10          1 NULL
```

`$IBCF_realRatingMatrix`

Recommender method: IBCF for realRatingMatrix Description:

Recommender based on item-based collaborative filtering. Reference: NA

Parameters:

```
k  method normalize normalize_sim_matrix alpha na_as_zero
1 30 "cosine" "center"          FALSE  0.5      FALSE
```

`$LIBMF_realRatingMatrix`

Recommender method: LIBMF for realRatingMatrix Description: Matrix

factorization with LIBMF via package recosystem

(<https://cran.r-project.org/web/packages/recosystem/vignettes/introduction.html>).

Reference: NA

Parameters:

```
dim costp_l2 costq_l2 nthread verbose
1 10    0.01    0.01      1    FALSE
```

`$POPULAR_realRatingMatrix`

Recommender method: POPULAR for realRatingMatrix Description:

Recommender based on item popularity. Reference: NA

Parameters:

```

  normalize
1 "center"
                                     aggregationRatings
1 new("standardGeneric", .Data = function (x, na.rm = FALSE, dims = 1,
                                     aggregationPopularity
1 new("standardGeneric", .Data = function (x, na.rm = FALSE, dims = 1,
```

`$RANDOM_realRatingMatrix`

Recommender method: RANDOM for realRatingMatrix Description:

Produce random recommendations (real ratings). Reference: NA

Parameters: None

`$RERECOMMEND_realRatingMatrix`

Recommender method: RERECOMMEND for realRatingMatrix Description:

Re-recommends highly rated items (real ratings). Reference: NA

Parameters:

```

  randomize minRating
1          1          NA
```

`$SVD_realRatingMatrix`

Recommender method: SVD for realRatingMatrix Description:

Recommender based on SVD approximation with column-mean imputation. Reference: NA

Parameters:

```

  k maxiter normalize
1 10    100 "center"
```

`$SVDF_realRatingMatrix`

Recommender method: SVDF for realRatingMatrix Description:

Recommender based on Funk SVD with gradient descend

(<https://sifter.org/~simon/journal/20061211.html>). Reference: NA

Parameters:

```

  k gamma lambda min_epochs max_epochs min_improvement normalize verbose
1 10 0.015 0.001          50          200          0.000001 "center"  FALSE
```

`$UBCF_realRatingMatrix`

Recommender method: UBCF for realRatingMatrix Description:

Recommender based on user-based collaborative filtering.

Reference: NA

Parameters:

```

  method nn sample weighted normalize min_matching_items
1 "cosine" 25 FALSE      TRUE "center"                0
  min_predictive_items
```

```
1 0
```

Next, we create a recommender which generates recommendations solely on the popularity of items (the number of users who have the item in their profile). We create a recommender from the first 1000 users in the Jester5k data set.

```
R> r <- Recommender(Jester5k[1:1000], method = "POPULAR")
R> r
```

```
Recommender of type 'POPULAR' for 'realRatingMatrix'
learned using 1000 users.
```

The model can be obtained from a recommender using `getModel()`.

```
R> names(getModel(r))

[1] "topN"           "ratings"         "normalize"
[4] "aggregationRatings" "aggregationPopularity" "verbose"
```

```
R> getModel(r)$topN
```

Recommendations as 'topNList' with n = 100 for 1 users.

In this case the model has a top- N list to store the popularity order and further elements (average ratings, if it used normalization and the used aggregation function).

Recommendations are generated by `predict()` (consistent with its use for other types of models in R). The result are recommendations in the form of an object of class `TopNList`. Here we create top-5 recommendation lists for two users who were not used to learn the model.

```
R> recom <- predict(r, Jester5k[1001:1002], n=5)
R> recom
```

Recommendations as 'topNList' with n = 5 for 2 users.

The result contains two ordered top- N recommendation lists, one for each user. The recommended items can be inspected as a list.

```
R> as(recom, "list")

$u15553
[1] "j89" "j72" "j93" "j76" "j87"

$u7886
[1] "j89" "j72" "j93" "j76" "j1"
```


Since the top- N lists are ordered, we can extract sublists of the best items in the top- N . For example, we can get the best 3 recommendations for each list using `bestN()`.

```
R> recom3 <- bestN(recom, n = 3)
R> recom3
```

Recommendations as ‘topNList’ with $n = 3$ for 2 users.

```
R> as(recom3, "list")
```

```
$u15553
[1] "j89" "j72" "j93"
```

```
$u7886
[1] "j89" "j72" "j93"
```

Many recommender algorithms can also predict ratings. This is also implemented using `predict()` with the parameter `type` set to “ratings”.

```
R> recom <- predict(r, Jester5k[1001:1002], type="ratings")
R> recom
```

2 x 100 rating matrix of class ‘realRatingMatrix’ with 72 ratings.

```
R> as(recom, "matrix")[,1:10]
```

```
      j1  j2  j3  j4 j5 j6 j7 j8  j9 j10
u15553 NA  NA  NA  NA NA NA NA NA  NA  NA
u7886  4.005 2.918 2.944 0.998 NA NA NA NA 2.319 NA
```

Predicted ratings are returned as an object of `realRatingMatrix`. The prediction contains NA for the items rated by the active users. In the example we show the predicted ratings for the first 10 items for the two active users.

Alternatively, we can also request the complete rating matrix which includes the original ratings by the user.

```
R> recom <- predict(r, Jester5k[1001:1002], type="ratingMatrix")
R> recom
```

2 x 100 rating matrix of class ‘realRatingMatrix’ with 200 ratings.

```
R> as(recom, "matrix")[,1:10]
```

```
      j1  j2  j3  j4  j5  j6  j7  j8  j9  j10
u15553 6.756 5.669 5.695 3.749 5.616 6.989 4.683 4.802 5.070 6.790
u7886  4.005 2.918 2.944 0.998 2.865 4.238 1.932 2.050 2.319 4.039
```

5.6. Evaluation of predicted ratings

Next, we will look at the evaluation of recommender algorithms. **recommenderlab** implements several standard evaluation methods for recommender systems. Evaluation starts with creating an evaluation scheme that determines what and how data is used for training and testing. Here we create an evaluation scheme which splits the first 1000 users in Jester5k into a training set (90%) and a test set (10%). For the test set 15 items will be given to the recommender algorithm and the other items will be held out for computing the error.

```
R> e <- evaluationScheme(Jester5k[1:1000], method="split", train=0.9,
+   given=15, goodRating=5)
R> e
```

```
Evaluation scheme with 15 items given
Method: 'split' with 1 run(s).
Training set proportion: 0.900
Good ratings: >=5.000000
Data set: 1000 x 100 rating matrix of class 'realRatingMatrix' with 74164 ratings.
```

We create two recommenders (user-based and item-based collaborative filtering) using the training data.

```
R> r1 <- Recommender(getData(e, "train"), "UBCF")
R> r1
```

```
Recommender of type 'UBCF' for 'realRatingMatrix'
learned using 900 users.
```

```
R> r2 <- Recommender(getData(e, "train"), "IBCF")
R> r2
```

```
Recommender of type 'IBCF' for 'realRatingMatrix'
learned using 900 users.
```

Next, we compute predicted ratings for the known part of the test data (15 items for each user) using the two algorithms.

```
R> p1 <- predict(r1, getData(e, "known"), type="ratings")
R> p1
```

```
100 x 100 rating matrix of class 'realRatingMatrix' with 8442 ratings.
```

```
R> p2 <- predict(r2, getData(e, "known"), type="ratings")
R> p2
```

```
100 x 100 rating matrix of class 'realRatingMatrix' with 8417 ratings.
```

Finally, we can calculate the error between the prediction and the unknown part of the test data.

```
R> error <- rbind(
+   UBCF = calcPredictionAccuracy(p1, getData(e, "unknown")),
+   IBCF = calcPredictionAccuracy(p2, getData(e, "unknown"))
+ )
R> error
```

```
      RMSE  MSE  MAE
UBCF 4.547 20.68 3.559
IBCF 4.526 20.49 3.460
```

In this example user-based collaborative filtering produces a smaller prediction error.

5.7. Evaluation of a top- N recommender algorithm

For this example we create a 4-fold cross validation scheme with the the Given-3 protocol, i.e., for the test users all but three randomly selected items are withheld for evaluation.

```
R> scheme <- evaluationScheme(Jester5k[1:1000], method="cross", k=4, given=3,
+   goodRating=5)
R> scheme
```

```
Evaluation scheme with 3 items given
Method: 'cross-validation' with 4 run(s).
Good ratings: >=5.000000
Data set: 1000 x 100 rating matrix of class 'realRatingMatrix' with 74164 ratings.
```

Next we use the created evaluation scheme to evaluate the recommender method popular. We evaluate top-1, top-3, top-5, top-10, top-15 and top-20 recommendation lists.

```
R> results <- evaluate(scheme, method="POPULAR", type = "topNList",
+   n=c(1,3,5,10,15,20))
```

```
POPULAR run fold/sample [model time/prediction time]
      1 [0.005sec/0.157sec]
      2 [0.004sec/0.148sec]
      3 [0.006sec/0.17sec]
      4 [0.004sec/0.143sec]
```

```
R> results
```

Evaluation results for 4 folds/samples using method 'POPULAR'.

The result is an object of class `EvaluationResult` which contains several confusion matrices. `getConfusionMatrix()` will return the confusion matrices for the 4 runs (we used 4-fold cross evaluation) as a list. In the following we look at the first element of the list which represents the first of the 4 runs.

```
R> getConfusionMatrix(results)[[1]]
```

	TP	FP	FN	TN	N	precision	recall	TPR	FPR	n
[1,]	0.464	0.536	19.25	76.75	97	0.4640	0.03458	0.03458	0.00678	1
[2,]	1.372	1.628	18.34	75.66	97	0.4573	0.08912	0.08912	0.01988	3
[3,]	2.228	2.772	17.49	74.51	97	0.4456	0.13867	0.13867	0.03379	5
[4,]	4.352	5.648	15.36	71.64	97	0.4352	0.28256	0.28256	0.06890	10
[5,]	6.272	8.728	13.44	68.56	97	0.4181	0.40248	0.40248	0.10828	15
[6,]	7.600	12.400	12.12	64.88	97	0.3800	0.45762	0.45762	0.15522	20

For the first run we have 6 confusion matrices represented by rows, one for each of the six different top- N lists we used for evaluation. n is the number of recommendations per list. TP, FP, FN and TN are the entries for true positives, false positives, false negatives and true negatives in the confusion matrix. The remaining columns contain precomputed performance measures. The average for all runs can be obtained from the evaluation results directly using `avg()`.

```
R> avg(results)
```

	TP	FP	FN	TN	N	precision	recall	TPR	FPR	n
[1,]	0.453	0.547	18.12	77.88	97	0.4530	0.03428	0.03428	0.006685	1
[2,]	1.299	1.701	17.28	76.72	97	0.4330	0.09435	0.09435	0.020704	3
[3,]	2.119	2.881	16.46	75.54	97	0.4238	0.14437	0.14437	0.034955	5
[4,]	4.127	5.873	14.45	72.55	97	0.4127	0.27452	0.27452	0.071829	10
[5,]	5.922	9.078	12.65	69.35	97	0.3948	0.38732	0.38732	0.111440	15
[6,]	7.347	12.653	11.23	65.77	97	0.3673	0.46375	0.46375	0.155834	20

Evaluation results can be plotted using `plot()`. The default plot is the ROC curve which plots the true positive rate (TPR) against the false positive rate (FPR).

```
R> plot(results, annotate=TRUE)
```

For the plot where we annotated the curve with the size of the top- N list is shown in Figure 8. By using "prec/rec" as the second argument, a precision-recall plot is produced (see Figure 9).

```
R> plot(results, "prec/rec", annotate=TRUE)
```

5.8. Comparing recommender algorithms

Comparing top- N recommendations

The comparison of several recommender algorithms is one of the main functions of **recommenderlab**. For comparison also `evaluate()` is used. The only change is to use `evaluate()`

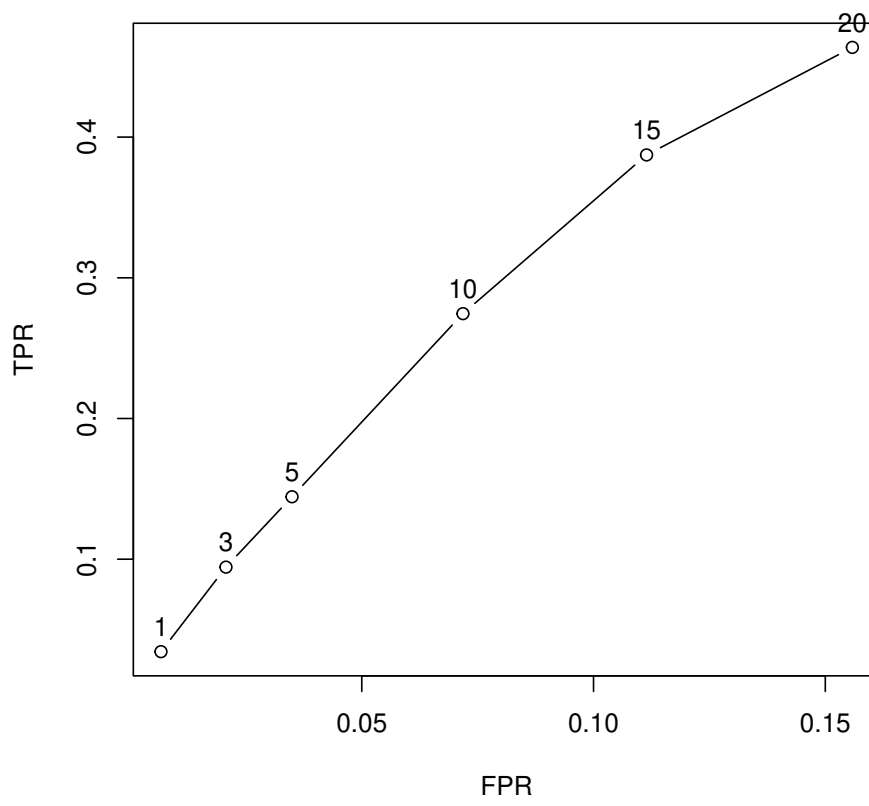


Figure 8: ROC curve for recommender method POPULAR.

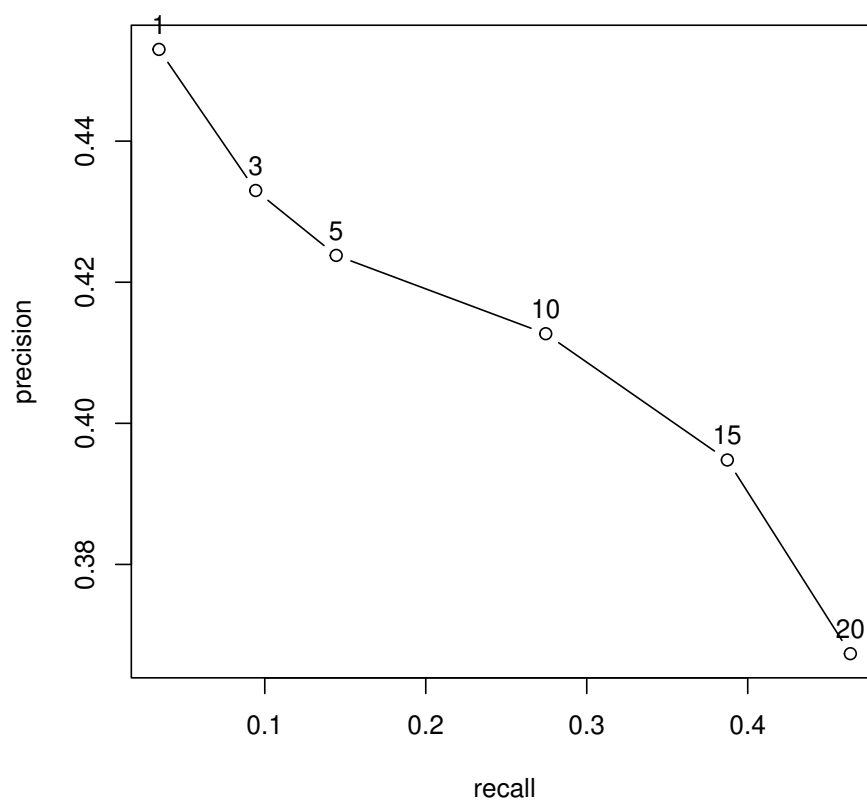


Figure 9: Precision-recall plot for method POPULAR.

with a list of algorithms together with their parameters instead of a single method name. In the following we use the evaluation scheme created above to compare the five recommender algorithms: random items, popular items, user-based CF, item-based CF, and SVD approximation. Note that when running the following code, the CF based algorithms are very slow. For the evaluation we use a “all-but-5” scheme. This is indicated by a negative number for given.

```
R> set.seed(2016)
R> scheme <- evaluationScheme(Jester5k[1:1000], method="split", train = .9,
+   given=-5, goodRating=5)
R> scheme

Evaluation scheme using all-but-5 items
Method: 'split' with 1 run(s).
Training set proportion: 0.900
Good ratings: >=5.000000
Data set: 1000 x 100 rating matrix of class 'realRatingMatrix' with 74164 ratings.

R> algorithms <- list(
+   "random items" = list(name="RANDOM", param=NULL),
+   "popular items" = list(name="POPULAR", param=NULL),
+   "user-based CF" = list(name="UBCF", param=list(nn=50)),
+   "item-based CF" = list(name="IBCF", param=list(k=50)),
+   "SVD approximation" = list(name="SVD", param=list(k = 50))
+ )
R> ## run algorithms
R> results <- evaluate(scheme, algorithms, type = "topNList",
+   n=c(1, 3, 5, 10, 15, 20))

RANDOM run fold/sample [model time/prediction time]
      1 [0.002sec/0.01sec]
POPULAR run fold/sample [model time/prediction time]
      1 [0.005sec/0.056sec]
UBCF run fold/sample [model time/prediction time]
      1 [0.004sec/0.226sec]
IBCF run fold/sample [model time/prediction time]
      1 [0.036sec/0.013sec]
SVD run fold/sample [model time/prediction time]
      1 [0.09sec/0.012sec]
```

The result is an object of class `evaluationResultList` for the five recommender algorithms.

```
R> results
```

List of evaluation results for 5 recommenders:

```
$`random items`
```

```
Evaluation results for 1 folds/samples using method 'RANDOM'.
```

```
$`popular items`
```

```
Evaluation results for 1 folds/samples using method 'POPULAR'.
```

```
$`user-based CF`
```

```
Evaluation results for 1 folds/samples using method 'UBCF'.
```

```
$`item-based CF`
```

```
Evaluation results for 1 folds/samples using method 'IBCF'.
```

```
$`SVD approximation`
```

```
Evaluation results for 1 folds/samples using method 'SVD'.
```

Individual results can be accessed by list subsetting using an index or the name specified when calling `evaluate()`.

```
R> names(results)
```

```
[1] "random items"      "popular items"      "user-based CF"
[4] "item-based CF"    "SVD approximation"
```

```
R> results[["user-based CF"]]
```

```
Evaluation results for 1 folds/samples using method 'UBCF'.
```

Again `plot()` can be used to create ROC and precision-recall plots (see Figures 10 and 11). `Plot` accepts most of the usual graphical parameters like `pch`, `type`, `lty`, etc. In addition `annotate` can be used to annotate the points on selected curves with the list length.

```
R> plot(results, annotate=c(1,3), legend="bottomright")
```

```
R> plot(results, "prec/rec", annotate=3, legend="topleft")
```

For this data set and the given evaluation scheme popular items and the user-based CF methods clearly outperform the other methods. In Figure 10 we see that they dominate (almost completely) the other method since for each length of top- N list they provide a better combination of TPR and FPR.

Comparing ratings

Next, we evaluate not top- N recommendations, but how well the algorithms can predict ratings.

```
R> ## run algorithms
```

```
R> results <- evaluate(scheme, algorithms, type = "ratings")
```

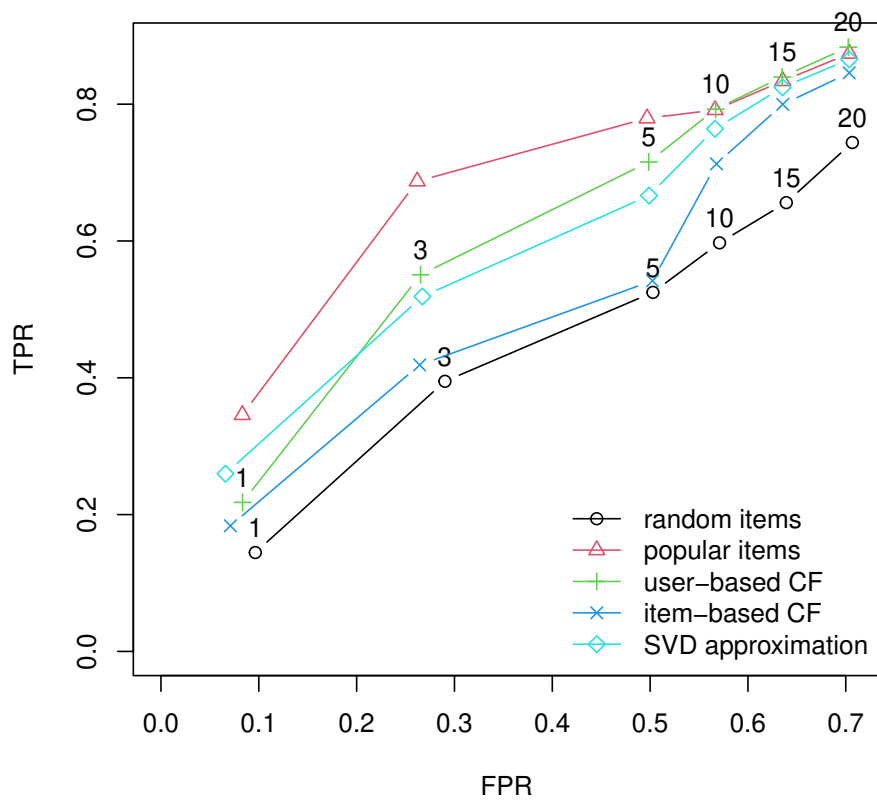



Figure 10: Comparison of ROC curves for several recommender methods for the given-3 evaluation scheme.

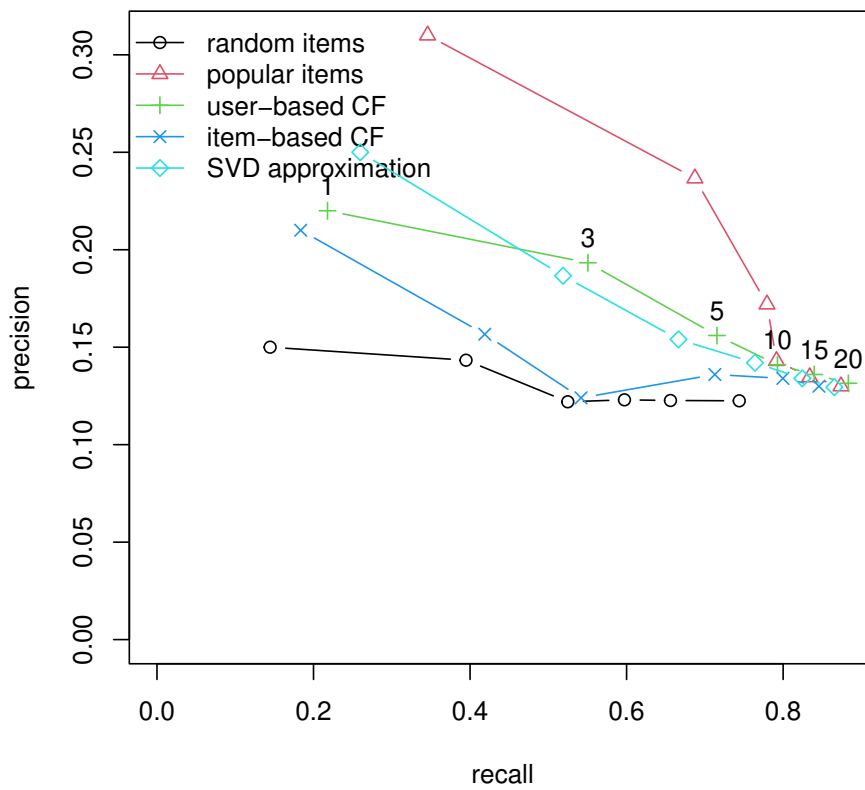


Figure 11: Comparison of precision-recall curves for several recommender methods for the given-3 evaluation scheme.

```

RANDOM run fold/sample [model time/prediction time]
      1 [0.001sec/0.004sec]
POPULAR run fold/sample [model time/prediction time]
      1 [0.005sec/0.004sec]
UBCF run fold/sample [model time/prediction time]
      1 [0.004sec/0.223sec]
IBCF run fold/sample [model time/prediction time]
      1 [0.037sec/0.007sec]
SVD run fold/sample [model time/prediction time]
      1 [0.09sec/0.008sec]

```

The result is again an object of class `evaluationResultList` for the five recommender algorithms.

```
R> results
```

List of evaluation results for 5 recommenders:

```
$`random items`
```

Evaluation results for 1 folds/samples using method 'RANDOM'.

```
$`popular items`
```

Evaluation results for 1 folds/samples using method 'POPULAR'.

```
$`user-based CF`
```

Evaluation results for 1 folds/samples using method 'UBCF'.

```
$`item-based CF`
```

Evaluation results for 1 folds/samples using method 'IBCF'.

```
$`SVD approximation`
```

Evaluation results for 1 folds/samples using method 'SVD'.

```
R> plot(results, ylim = c(0,100))
```

Plotting the results shows a barplot with the root mean square error, the mean square error and the mean absolute error (see Figures 12).

Using a 0-1 data set

For comparison we will check how the algorithms compare given less information. We convert the data set into 0-1 data and instead of a all-but-5 we use the given-3 scheme.

```
R> Jester_binary <- binarize(Jester5k, minRating=5)
```

```
R> Jester_binary <- Jester_binary[rowCounts(Jester_binary)>20]
```

```
R> Jester_binary
```

1840 x 100 rating matrix of class 'binaryRatingMatrix' with 67728 ratings.

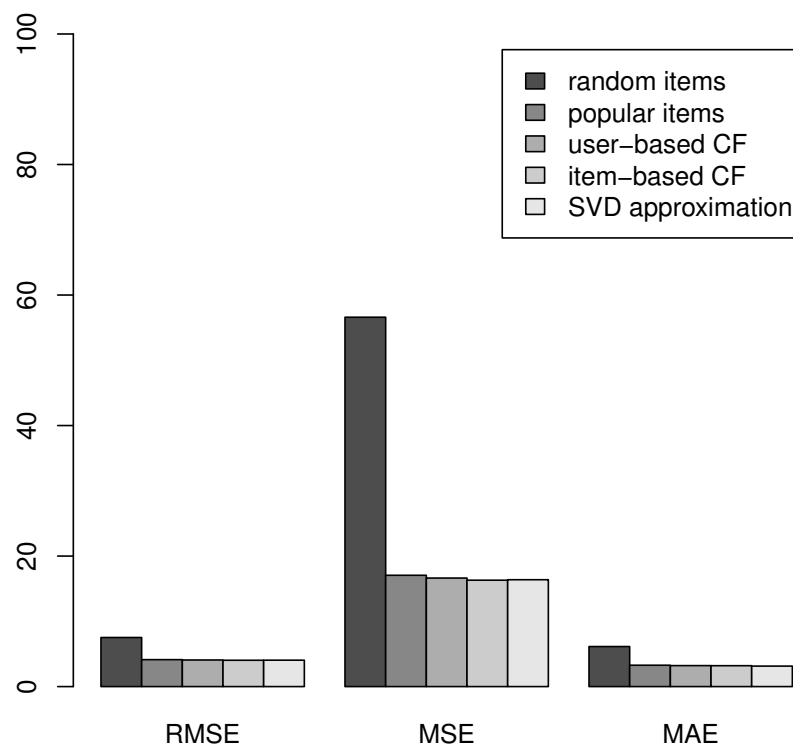


Figure 12: Comparison of RMSE, MSE, and MAE for recommender methods for the given-3 evaluation scheme.

```
R> scheme_binary <- evaluationScheme(Jester_binary[1:1000],
+   method="split", train=.9, k=1, given=3)
R> scheme_binary
```

Evaluation scheme with 3 items given

Method: 'split' with 1 run(s).

Training set proportion: 0.900

Good ratings: NA

Data set: 1000 x 100 rating matrix of class 'binaryRatingMatrix' with 36619 ratings.

```
R> results_binary <- evaluate(scheme_binary, algorithms,
+   type = "topNList", n=c(1,3,5,10,15,20))
```

```
RANDOM run fold/sample [model time/prediction time]
      1 [0.001sec/0.015sec]
POPULAR run fold/sample [model time/prediction time]
      1 [0.002sec/0.02sec]
UBCF run fold/sample [model time/prediction time]
      1 [0sec/0.332sec]
IBCF run fold/sample [model time/prediction time]
      1 [0.05sec/0.018sec]
SVD run fold/sample [model time/prediction time]
      1
```

Note that SVD does not implement a method for binary data and is thus skipped.

```
R> plot(results_binary, annotate=c(1,3), legend="topright")
```

From Figure 13 we see that given less information, the performance of user-based CF suffers the most and the simple popularity based recommender performs almost as well as item-based CF.

Similar to the examples presented here, it is easy to compare different recommender algorithms for different data sets or to compare different algorithm settings (e.g., the influence of neighborhood formation using different distance measures or different neighborhood sizes).

5.9. Implementing a new recommender algorithm

Adding a new recommender algorithm to **recommenderlab** is straight forward since it uses a registry mechanism to manage the algorithms. To implement the actual recommender algorithm we need to implement a creator function which takes a training data set, trains a model and provides a predict function which uses the model to create recommendations for new data. The model and the predict function are both encapsulated in an object of class **Recommender**.

For examples look at the files starting with **RECOM** in the packages **R** directory. A good examples is in **RECOM_POPULAR.R**.

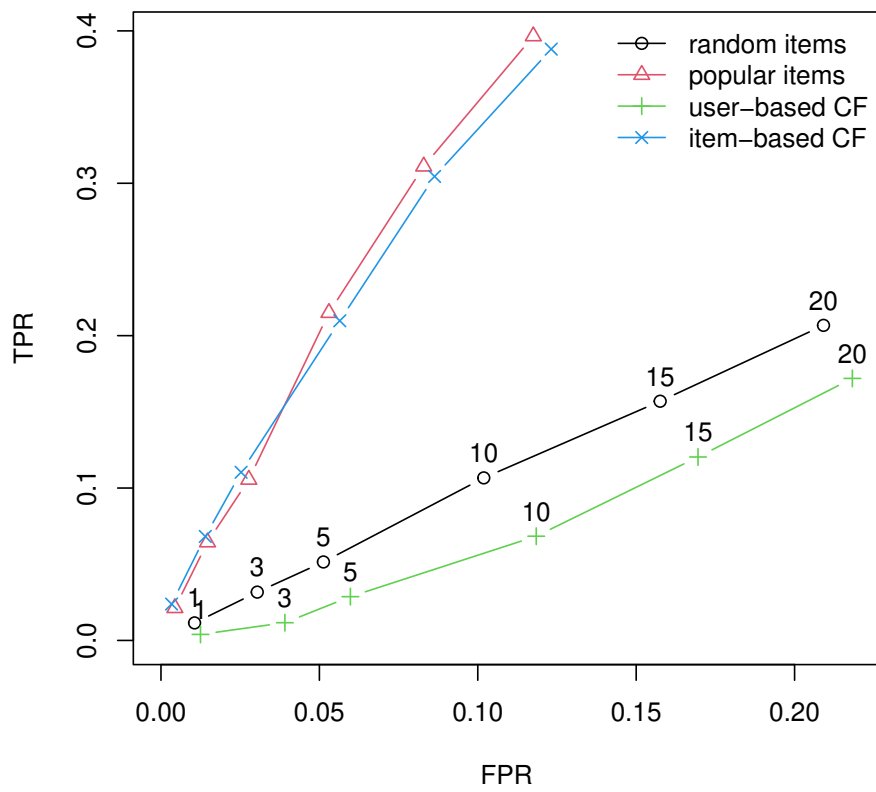


Figure 13: Comparison of ROC curves for several recommender methods for the given-3 evaluation scheme.

6. Conclusion

In this paper we described the R extension package **recommenderlab** which is especially geared towards developing and testing recommender algorithms. The package allows to create evaluation schemes following accepted methods and then use them to evaluate and compare recommender algorithms. **recommenderlab** currently includes several standard algorithms and adding new recommender algorithms to the package is facilitated by the built in registry mechanism to manage algorithms. In the future we will add more and more of these algorithms to the package and we hope that some algorithms will also be contributed by other researchers.

Acknowledgments

This research was funded in part by the NSF Industry/University Cooperative Research Center for Net-Centric Software & Systems.

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