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GeneralizedUmatrix-package

*Credible Visualization for Two-Dimensional Projections of Data*

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## Description

Projections are common dimensionality reduction methods, which represent high-dimensional data in a two-dimensional space. However, when restricting the output space to two dimensions, which results in a two dimensional scatter plot (projection) of the data, low dimensional similarities do not represent high dimensional distances coercively [Thrun, 2018] <DOI: 10.1007/978-3-658-20540-9>. This could lead to a misleading interpretation of the underlying structures [Thrun, 2018]. By means of the 3D topographic map the generalized Umatrix is able to depict errors of these two-dimensional scatter plots. The package is derived from the book of Thrun, M.C.: "Projection Based Clustering through Self-Organization and Swarm Intelligence" (2018) <DOI:10.1007/978-3-658-20540-9> and the main algorithm called simplified self-organizing map for dimensionality reduction methods is published in <DOI: 10.1016/j.mex.2020.101093>.

## Details

For a brief introduction to **GeneralizedUmatrix** please see the vignette [Introduction of the Generalized Umatrix Package](#).

For further details regarding the generalized Umatrix see [Thrun, 2018], chapter 4-5, or [Thrun/Ultsch, 2020].

If you want to verify your clustering result externally, you can use Heatmap or SilhouettePlot of the CRAN package DataVisualizations.

Index of help topics:

|                            |   |
|----------------------------|---|
| CalcUstarmatrix            | Calculate the U*matrix for a given Umatrix and Pmatrix.                                   |
| Chainlink                  | Chainlink is part of the Fundamental Clustering Problem Suit (FCPS) [Thrun/Ultsch, 2020]. |
| DefaultColorSequence       | Default color sequence for plots  |
| Delta3DWeightsC            | intern function   |
| EsomNeuronsAsList          | Converts wts data (EsomNeurons) into the list form  |
| ExtendToroidalUmatrix      | Extend Toroidal Umatrix   |
| GeneralizedUmatrix         | Generalized U-Matrix for Projection Methods published in [Thrun/Ultsch, 2020]             |
| GeneralizedUmatrix-package | Credible Visualization for Two-Dimensional Projections of Data                            |
| GeneratePmatrix            | Generates the P-matrix  |
| ListAsEsomNeurons          | Converts List to WTS  |
| LowLand                    | LowLand   |
| NormalizeUmatrix           | Normalize Umatrix   |
| ReduceToLowLand            | ReduceToLowLand   |



```

## from a tiled Umatrix (toroidal assumption)
## Not run:
Imx = ProjectionBasedClustering::interactiveGeneralizedUmatrixIsland(resUmatrix$Umatrix,
resUmatrix$Bestmatches)
plotTopographicMap(resUmatrix$Umatrix,

resUmatrix$Bestmatches, Imx = Imx)

## End(Not run)
#External Verification
## Not run:

DataVisualizations::Heatmap(Data,Cls)
#if spherical cluster strcuture
DataVisualizations::SilhouettePlot(Data,Cls)

## End(Not run)

```

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addRowWiseC                  *intern function*

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### Description

Adds the Vector DataPoint to every row of the matrix WeightVectors

### Usage

```
addRowWiseC(WeightVectors,DataPoint)
```

### Arguments

WeightVectors    WeightVectors. n weights with m components each  
DataPoint         Vector with m components

### Value

WeightVectors[1:m,1:n]



## References

[Thrun/Ultsch, 2020] Thrun, M. C., & Ultsch, A.: Clustering Benchmark Datasets Exploiting the Fundamental Clustering Problems, Data in Brief, Vol. 30(C), pp. 105501, DOI 10.1016/j.dib.2020.105501, 2020.

[Ultsch 1995] Ultsch, A.: Self organizing neural networks perform different from statistical k-means clustering, Proc. Society for Information and Classification (GFKL), Vol. 1995, Basel 8th-10th March, 1995.

[Ultsch et al.,1994] Ultsch, A., Guimaraes, G., Korus, D., & Li, H.: Knowledge extraction from artificial neural networks and applications, Parallele Datenverarbeitung mit dem Transputer, pp. 148-16 Chainlink, Springer, 1994.

## Examples

```
data(Chainlink)
str(Chainlink)

## Not run:
require(DataVisualizations)
DataVisualizations::Plot3D(Chainlink$Data,Chainlink$Cls)

## End(Not run)
```

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DefaultColorSequence *Default color sequence for plots*

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## Description

Defines the default color sequence for plots made within the Projections package.

## Usage

```
data("DefaultColorSequence")
```

## Format

A vector with 562 different strings describing colors for plots.











**Details**

To set the Radius the ABCAnalysis of high-dimensional distances can be used [Ultsch/Lötsch, 2015]. For a detailed definition and equation of automated density estimation (Radius) see Thrun et al. 2016.

**Value**

PMatrix[1:Lines,1:Columns]

**Author(s)**

Michael Thrun

**References**

Ultsch, A.: Maps for the visualization of high-dimensional data spaces, Proc. Workshop on Self organizing Maps (WSOM), pp. 225-230, Kyushu, Japan, 2003.

Ultsch, A., Loetsch, J.: Computed ABC Analysis for Rational Selection of Most Informative Variables in Multivariate Data, PloS one, Vol. 10(6), pp. e0129767. doi 10.1371/journal.pone.0129767, 2015.

Thrun, M. C., Lerch, F., Loetsch, J., Ultsch, A.: Visualization and 3D Printing of Multivariate Data of Biomarkers, in Skala, V. (Ed.), International Conference in Central Europe on Computer Graphics, Visualization and Computer Vision,Plzen, 2016.

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ListAsEsomNeurons

*Converts List to WTS*

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**Description**

Converts wts data in list form into a 3 dimensional array

**Arguments**

wts\_list[1:(Lines\*Columns),1:Variables]

Matrix with weights in the 2nd dimension(not list() like in R)

Lines Lines/Height of the desired grid

Columns Columns/Width of the desired grid

**Details**

One could describe this function as a transformation or a special case of long to wide format, see also [EsomNeuronsAsList](#)

**Value**

EsomNeurons[1:Lines, 1:Columns, 1:Variables]

3 dimensional array containing the weights of the neural grid. For a more general explanation see reference



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|                  |                          |
|------------------|--------------------------|
| NormalizeUmatrix | <i>Normalize Umatrix</i> |
|------------------|--------------------------|

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### Description

Normalizing the U-matrix using the abstract U-Matrix concept [Loetsch/Ultsch, 2014].

### Usage

```
NormalizeUmatrix(Data, Umatrix, BestMatches)
```

### Arguments

|             |   |
|-------------|---|
| Data        | [1:n,1:d] numerical matrix of data with n cases and d variables |
| Umatrix     | [1:lines,1:Columns] matrix of U-heights                         |
| BestMatches | [1:n,1:2] Bestmatching units.                                   |

### Details

see publication [Loetsch/Ultsch, 2014].

### Value

Normalized Umatrix[1:lines,1:Columns] using the abstract U-Matrix concept.

### Author(s)

Felix Pape, Michael Thrun

### References

Loetsch, J., Ultsch, A.: Exploiting the structures of the U-matrix, in Villmann, T., Schleif, F.-M., Kaden, M. & Lange, M. (eds.), Proc. Advances in Self-Organizing Maps and Learning Vector Quantization, pp. 249-257, Springer International Publishing, Mittweida, Germany, 2014.

### Examples

```
data("Chainlink")
Data=Chainlink$Data
Cls=Chainlink$Cls
InputDistances=as.matrix(dist(Data))
res=cmdscale(d=InputDistances, k = 2, eig = TRUE, add = FALSE, x.ret = FALSE)
ProjectedPoints=as.matrix(res$points)
#see also ProjectionBasedClustering package for other common projection methods
```

```
resUmatrix=GeneralizedUmatrix(Data,ProjectedPoints)
## Normalization
```

```

normalizedUmatrix=NormalizeUmatrix(Data,resUmatrix$Umatrix,resUmatrix$Bestmatches)
## visualization
TopviewTopographicMap(GeneralizedUmatrix = normalizedUmatrix,resUmatrix$Bestmatches)

```

`plotTopographicMap`     *Visualizes the Generalized U-matrix in 3D*

### Description

The generalized U-matrix is visualized as the topographic map with hypsometric tints. The topographic map represents high-dimensional distance and density-based structures in form of a 3D landscape.

### Usage

```

plotTopographicMap(GeneralizedUmatrix, BestMatchingUnits,
  Cls=NULL, ClsColors=NULL, Imx=NULL, Names=NULL,
  BmSize=0.5, RenderingContourLines=TRUE, ...)

```

### Arguments

|                                    |   |
|------------------------------------|---|
| <code>GeneralizedUmatrix</code>    | (1:Lines,1:Columns), [1:Lines,1:Columns] Umatrix to be plotted, numerical matrix storing the U-heights, see [Thrun, 2018] for definition.   |
| <code>BestMatchingUnits</code>     | (1:n,1:2), Positions of bestmatches to be plotted as spheres onto the topographic map   |
| <code>Cls</code>                   | (1:n), numerical vector of classification of k clusters, one label for each best-match at that given point  |
| <code>ClsColors</code>             | Vector of colors that will be used to colorize the different clusters, default is <code>GeneralizedUmatrix::DefaultColorSequence</code>   |
| <code>Imx</code>                   | a mask ( <code>Imx</code> ) that will be used to cut out the umatrix  |
| <code>Names</code>                 | If set: [1:k] character vector naming the k clusters for the legend. . In this case, further parameters with the possibility to adjust are: <code>NamesCex</code> : (size); <code>NamesPosition</code> : Legend position; <code>NamesTitle</code> : title of legend; <code>NamesColors</code> : colors if <code>ClsColors</code> are not default (NULL), etc. |
| <code>BmSize</code>                | size(diameter) of the points in the visualizations. The points represent the <code>Best-MatchingUnits</code>  |
| <code>RenderingContourLines</code> | <code>FALSE</code> : disables plotting of contour lines resulting in a much faster plot.  |











## Usage

```
TopviewTopographicMap(GeneralizedUmatrix, BestMatchingUnits,  
Cls, ClsColors = NULL, Imx = NULL,  
ClsNames = NULL, BmSize = 6, DotLineWidth = 2,  
alpha = 1, ...)
```

## Arguments

|                    |   |
|--------------------|---|
| GeneralizedUmatrix | (1:Lines,1:Columns), [1:Lines,1:Columns] Umatrix to be plotted, numerical matrix storing the U-heights, see [Thrun, 2018] for definition.   |
| BestMatchingUnits  | (1:n,1:2), Positions of bestmatches to be plotted onto the Umatrix  |
| Cls                | (1:n), numerical vector of classification of k classes for the bestmatch at the given point   |
| ClsColors          | Vector of colors that will be used to colorize the different classes  |
| Imx                | a mask (Imx) that will be used to cut out the umatrix   |
| ClsNames           | If set: [1:k] character vector naming the k classes for the legend. In this case, further parameters with the possibility to adjust are: LegendCex: (size); NamesOrientation: Legend position "v" or "h"; NamesTitle: title of legend.  |
| BmSize             | size(diameter) of the points in the visualizations. The points represent the Best-MatchingUnits   |
| DotLineWidth       | ...   |
| alpha              | ...   |
| ...                | <b>Tiled</b> Should the Umatrix be drawn 4times?<br><b>main</b> set specific title in plot<br><b>ExtendBorders</b> scalar, extends Umatrix by toroidal continuation of the given Umatrix<br><b>MainCex</b> scalar, magnification to be used for legend<br><b>LegendCex</b> scalar, magnification to be used for main titles<br>_ Further Arguments relevant for interactive shiny application |

## Details

Please see [plotTopographicMap](#). This function is currently still experimental because not all functionality is fully tested yet.

## Value

plotly handler





**Arguments**

BestMatchingUnits  
(1:n,1:d) BMKey = BestMatchingUnits[,1]  
GeneralizedUmatrix  
(1:Lines,1:Columns) a GeneralizedUmatrix

**Value**

Uheights        Uheights  
BMLineCoords   BMLineCoords  
BMColCoords    BMColCoords

**Author(s)**

ALU 2021 in matlab, MCT reimplemented in

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|                 |                        |
|-----------------|------------------------|
| UmatrixColormap | <i>U-Matrix colors</i> |
|-----------------|------------------------|

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**Description**

Defines the default color sequence for plots made for Umatrix

**Usage**

data("UmatrixColormap")

**Format**

Returns the vectors for a (heat) colormap.

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|                         |                                |
|-------------------------|--------------------------------|
| UniqueBestMatchingUnits | <i>UniqueBestMatchingUnits</i> |
|-------------------------|--------------------------------|

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**Description**

UniqueBestMatchingUnits

**Usage**

UniqueBestMatchingUnits(NonUniqueBestMatchingUnits)







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