

Package ‘bgumbel’

April 1, 2021

Title Bimodal Gumbel Distribution

Version 0.0.3

Description Bimodal Gumbel distribution. General functions for performing extreme value analysis.

Imports MCMCpack, MASS, quantreg, SparseM, coda, stats

License MIT + file LICENSE

SystemRequirements gcc (>= 4.0), gfortran, clang++

NeedsCompilation yes

URL <https://CRAN.R-project.org/package=bgumbel>

Language en-US

Encoding UTF-8

LazyData false

Date 2021-03-31

RoxygenNote 7.1.1

Author Pedro C. Brom [aut, cre, cph] (<<https://orcid.org/0000-0002-1288-7695>>, <http://lattes.cnpq.br/0154064396756002>),
Cira E. G. Otiniano [aut, cph]
(<<https://orcid.org/0000-0002-5619-0478>>, <http://lattes.cnpq.br/0307717595727716>),
Roberto Vila [aut, cph] (<<https://orcid.org/0000-0003-1073-0114>>, <http://lattes.cnpq.br/4978745622057574>),
Marcelo B. Pereira [aut, cph] (<<https://orcid.org/0000-0002-1182-5193>>, <https://lattes.cnpq.br/9358366674842900>)

Maintainer Pedro C. Brom <pcbrom@gmail.com>

Repository CRAN

Date/Publication 2021-03-31 22:10:07 UTC

R topics documented:

dbgumbel	2
m1bgumbel	3

m2bgumbel	4
mlebgumbel	5
pbgumbel	6
qbgumbel	7
rbgumbel	8
Index	9

dbgumbel	<i>Bimodal Gumbel: Density Function</i>
----------	---

Description

Bimodal Gumbel: Density Function

Usage

```
dbgumbel(x, mu, sigma, delta)
```

Arguments

x	Domain.
mu	First location parameter.
sigma	Scale parameter.
delta	Second location parameter.

Value

Vector.

Examples

```
dbgumbel(x = 0, mu = -2, sigma = 1, delta = -1)
curve(dbgumbel(x, mu = -2, sigma = 1, delta = -1), xlim = c(-5, 10), ylim = c(0, .4))
integrate(dbgumbel, mu = -2, sigma = 1, delta = -1, lower = -5, upper = 0)
```

`m1bgumbel`*Bimodal Gumbel: Theoretical E(X)*

Description

Bimodal Gumbel: Theoretical E(X)

Usage`m1bgumbel(mu, sigma, delta)`**Arguments**

<code>mu</code>	First location parameter.
<code>sigma</code>	Scale parameter.
<code>delta</code>	Second location parameter.

Value

Vector.

Examples

```
(EX <- m1bgumbel(mu = -2, sigma = 1, delta = -1))

# Comparison: Theoretical E(X) and empirical mean

x <- rbgumbel(100000, mu = -2, sigma = 1, delta = -1)
mean(x)
abs(EX - mean(x))/abs(EX) # relative error

# grid 1

mu <- seq(-5, 5, length.out = 100)
delta <- seq(-5, 5, length.out = 100)
z <- outer(
  X <- mu,
  Y <- delta,
  FUN = function(x, y) m1bgumbel(mu = x, sigma = 1, delta = y)
)

persp(x = mu, y = delta, z = z, theta = -60, ticktype = 'detailed')

# grid 2

mu <- seq(-5, 5, length.out = 100)
delta <- seq(-5, 5, length.out = 100)
sigmas <- seq(.1, 10, length.out = 20)
```

```

for (sigma in sigmas) {
  z <- outer(
    X <- mu,
    Y <- delta,
    FUN = function(x, y) m1bgumbel(mu = x, sigma = sigma, delta = y)
  )
  persp(x = mu, y = delta, z = z, theta = -60, zlab = 'E(X)')
  Sys.sleep(.5)
}

```

m2bgumbel

Bimodal Gumbel: Theoretical $E(X^2)$

Description

Bimodal Gumbel: Theoretical $E(X^2)$

Usage

```
m2bgumbel(mu, sigma, delta)
```

Arguments

mu	First location parameter.
sigma	Scale parameter.
delta	Second location parameter.

Value

Vector.

Examples

```

(EX2 <- m2bgumbel(mu = -2, sigma = 1, delta = -1))

# Comparison: Theoretical  $E(X^2)$  and empirical second moment
x <- rbgumbel(100000, mu = -2, sigma = 1, delta = -1)
mean(x^2)
abs(EX2 - mean(x))/abs(EX2) # relative error

# Variance
EX <- m1bgumbel(mu = -2, sigma = 1, delta = -1)
EX2 - EX^2
var(x)
abs(EX2 - EX^2 - var(x))/abs(EX2 - EX^2) # relative error

```

```
# grid 1

mu <- seq(-5, 5, length.out = 100)
delta <- seq(-5, 5, length.out = 100)
z <- outer(
  X <- mu,
  Y <- delta,
  FUN = function(x, y) m2bgumbel(mu = x, sigma = 1, delta = y)
)
persp(x = mu, y = delta, z = z, theta = -30, ticktype = 'detailed')

# grid 2

mu <- seq(-5, 5, length.out = 100)
delta <- seq(-5, 5, length.out = 100)
sigmas <- seq(.1, 10, length.out = 20)
for (sigma in sigmas) {
  z <- outer(
    X <- mu,
    Y <- delta,
    FUN = function(x, y) m2bgumbel(mu = x, sigma = sigma, delta = y)
  )
  persp(x = mu, y = delta, z = z, theta = -45, zlab = 'E(X^2)')
  Sys.sleep(.5)
}
```

mlebgumbel

Bimodal Gumbel: Maximum Likelihood Estimation

Description

Bimodal Gumbel: Maximum Likelihood Estimation

Usage

```
mlebgumbel(data, theta, auto = TRUE)
```

Arguments

data	A numeric vector.
theta	Vector. Starting parameter values for the minimization. Default: $\theta = c(1, 1, 1)$
auto	Logical. Automatic search for theta initial condition. Default: TRUE

Value

List.

Examples

```

# Let's generate some values

set.seed(123)
x <- rbkgumbel(1000, mu = -2, sigma = 1, delta = -1)

# Look for these references in the figure:

hist(x, probability = TRUE)
lines(density(x), col = 'blue')
abline(v = c(-2.5, -.5), col = 'red')
text(x = c(-2.5, -.5), y = c(.05, .05), c('mu\nnear here', 'delta\nnear here'))

# Time to fit!

# If argument auto = FALSE
fit <- mlebgumbel(
  data = x,
  # try some values near the region. Format: theta = c(mu, sigma, delta)
  theta = c(-3, 2, -2),
  auto = FALSE
)
print(fit)

# If argument auto = TRUE
fit <- mlebgumbel(
  data = x,
  auto = TRUE
)
print(fit)

# Kolmogorov-Smirnov Tests

mu.sigma.delta <- fit$estimate$estimate
ks.test(
  x,
  y = 'pbgumbel',
  mu = mu.sigma.delta[[1]],
  sigma = mu.sigma.delta[[2]],
  delta = mu.sigma.delta[[3]]
)

```

pbgumbel

Bimodal Gumbel: Distribution Function

Description

Bimodal Gumbel: Distribution Function

Usage

```
pbgumbel(q, mu, sigma, delta, lower.tail = TRUE)
```

Arguments

q	Quantile.
mu	First location parameter.
sigma	Scale parameter.
delta	Second location parameter.
lower.tail	Logical; if TRUE (default), probabilities are $P(X \leq x)$ otherwise, $P(X > x)$.

Value

Vector.

Examples

```
pbgumbel(0, mu = -2, sigma = 1, delta = -1)
integrate(dbgumbel, mu = -2, sigma = 1, delta = -1, lower = -Inf, upper = 0)
pbgumbel(0, mu = -2, sigma = 1, delta = -1, lower.tail = FALSE)
curve(pbgumbel(x, mu = -2, sigma = 1, delta = -1), xlim = c(-5, 10))
```

qbgumbel

Bimodal Gumbel: Quantile Function

Description

Bimodal Gumbel: Quantile Function

Usage

```
qbgumbel(p, mu, sigma, delta, initial = -10, final = 10)
```

Arguments

p	Probability.
mu	First location parameter.
sigma	Scale parameter.
delta	Second location parameter.
initial	Starting point of range in desired quantile.
final	Starting point of range in desired quantile.

Value

Vector.

Examples

```
# It is recommended to set up a pbgumbel
# graph to see the starting and ending
# range of the desired quantile.
curve(pbgumbel(x, mu = -2, sigma = 1, delta = -1), xlim = c(-5, 5))
(value <- qbgumbel(.25, mu = -2, sigma = 1, delta = -1, initial = -4, final = -2))
pbgumbel(value, mu = -2, sigma = 1, delta = -1)
```

 rbgumbel

Bimodal Gumbel: Pseudo-Random Numbers Generator

Description

Bimodal Gumbel: Pseudo-Random Numbers Generator

Usage

```
rbgumbel(n, mu, sigma, delta)
```

Arguments

n	Number of observations. If length(n) > 1, the length is taken to be the number required.
mu	First location parameter.
sigma	Scale parameter.
delta	Second location parameter.

Value

A matrix nx1.

Examples

```
x <- rbgumbel(40000, mu = -2, sigma = 1, delta = -1)
hist(x, probability = TRUE)
curve(dbgumbel(x, mu = -2, sigma = 1, delta = -1), add = TRUE, col = 'blue')
lines(density(x), col = 'red')
```


Index

dbgumbel, 2

m1bgumbel, 3

m2bgumbel, 4

m1ebgumbel, 5

pbgumbel, 6

qbgumbel, 7

rbgumbel, 8