Package 'fBasics'

August 8, 2022

Title Rmetrics - Markets and Basic Statistics

Date 2022-09-08

Version 4021.92

Description Provides a collection of functions to
explore and to investigate basic properties of financial returns
and related quantities.
The covered fields include techniques of explorative data analysis
and the investigation of distributional properties, including
parameter estimation and hypothesis testing. Even more there are
several utility functions for data handling and management.

Depends R (>= 2.15.1)

Imports timeDate, timeSeries, stats, grDevices, graphics, methods,
utils, MASS, spatial, gss, stabledist

Suggests interp, RUnit, tcltk

LazyData yes

License GPL (>= 2)

Encoding UTF-8

URL https://r-forge.r-project.org/scm/viewvc.php/pkg/fBasics/?root=rmetrics
)devel), https://www.rmetrics.org

BugReports https://r-forge.r-project.org/projects/rmetrics

NeedsCompilation yes

Author Diethelm Wuertz [aut] (original code),
Tobias Setz [aut],
Yohan Chalabi [aut],
Martin Maechler [ctb] (<https://orcid.org/0000-0002-8685-9910>),
CRAN Team [ctb],
Georgi N. Boshnakov [cre, ctb]

Maintainer Georgi N. Boshnakov <georgi.boshnakov@manchester.ac.uk>

Repository CRAN

Date/Publication 2022-08-08 11:40:12 UTC

R topics documented:

`fBasics-package` *Portfolio Modelling, Optimization and Backtesting*

Description

The Rmetrics "fBasics" package is a collection of functions to explore and to investigate basic properties of financial returns and related quantities.

The covered fields include techniques of explorative data analysis and the investigation of distributional properties, including parameter estimation and hypothesis testing. Evenmore there are several utility functions for data handling and managemnet.

Details

```
Package:    \tab fBasics\cr
Type:       \tab Package\cr
Date:       \tab 2014\cr
License:    \tab GPL Version 2 or later\cr
Copyright:  \tab (c) 1999-2014 Rmetrics Association\cr
Repository: \tab R-FORGE\cr
URL:        \tab \url{https://www.rmetrics.org}
```

1 Introduction

The fBasics package contains *basics tools* often required in computational finance and financial engineering. The topics are: basic statistics functions, financial return distributions, hypothesis testing, plotting routines, matrix computations and linear algebra, and some usefule utility functions.

2 Basic Statistics Functions

Financial Return Statistics

`basicStats`	`Returns a basic statistics summary`

Distribution Function of Maximum Drawdowns

`dmaxdd`	`Density function of mean Max-Drawdowns`
`pmaxdd`	`Probability function of mean Max-Drawdowns`
`rmaxdd`	`Random Variates of mean Max-Drawdowns`
`maxddStats`	`Expectation of Drawdowns for BM with drift`

Calculation of Sample Moments

sampleLmoments	Computes sample L-moments
sampleMED	Returns sample median
sampleIQR	returns sample inter quartal range
sampleSKEW	returns robust sample skewness
sampleKURT	returns robust sample kurtosis

Bivariate Interpolation:

akimaInterp	Interpolates irregularly spaced points
akimaInterpp	Interpolates and smoothes pointwise
krigeInterp	Kriges irregularly spaced data points
linearInterp	Interpolates irregularly spaced points
linearInterpp	Interpolates linearly pointwise

Utility Statistics Functions:

colStats	Computes sample statistics by col
colSums	Computes sums of values in each col
colMeans	Computes means of values in each col
colSds	Computes standard deviation of each col
colVars	Computes sample variance by col
colSkewness	Computes sample skewness by col
colKurtosis	Computes sample kurtosis by col
colMaxs	Computes maximum values in each col
colMins	Computes minimum values in each col
colProds	Computes product of values in each col
colQuantiles	Computes product of values in each col

rowStats	Computes sample statistics by row
rowSums	Computes sums of values in each row
rowMeans	Computes means of values in each row
rowSds	Computes standard deviation of each row
rowVars	Computes sample variance by row
rowSkewness	Computes sample skewness by row
rowKurtosis	Computes sample kurtosis by row
rowMaxs	Computes maximum values in each row
rowMins	Computes minimum values in each row
rowProds	Computes product of values in each row
rowQuantiles	Computes product of values in each row

3 Financial Return Distributions

Generalized Hyperbolic Distribution:

dghReturns	Density for the GH distribution
pghreturns	Probability for the GH distribution
qghreturns	Quantiles for the GH distribution
rghreturns	Random variates for the GH distribution
ghFitFits	Fits parameters of the GH distribution
ghMode	Computes mode of the GH distribution.
ghMean	Returns true mean of the GH distribution
ghVar	Returns true variance of the GH distribution
ghSkew	Returns true skewness of the GH distribution
ghKurt	Returns true kurtosis of the GH distribution
ghMoments	Returns true n-th moment of the GH distribution
ghMED	Returns true median of te GH distribution
ghIQR	Returns true inter quartal range of te GH
ghSKEW	Returns true robust skewness of te GH
ghKURT	Returns true robust kurtosis of te GH

Hyperbolic Distribution:

dhyp	Returns density for the HYP distribution
phyp	Returns probability for the HYP distribution
qhyp	Returns quantiles for the HYP distribution
rhyp	Returns random variates for the HYP distribution
hypFit	Fits parameters of the HYP distribution
hypMode	Computes mode of the HYP distribution
hypMean	Returns true mean of the HYP distribution
hypVar R	Returns true variance of the HYP distribution
hypSkew	Returns true skewness of the HYP distribution
hypKurt	Returns true kurtosis of the HYP distribution
hypMoments	Returns true n-th moment of the HYP distribution
hypMED	Returns true median of the HYP distribution
hypIQR	Returns true inter quartal range of the HYP
hypSKEW	Returns true robust skewness of the HYP
hypKURT	Returns true robust kurtosis of the HYP

Normal Inverse Gaussian:

dnig	Returns density for the NIG distribution
pnig	Returns probability for the NIG distribution
qnig	Returns quantiles for the NIG distribution
rnig	Returns random variates for the NIG distribution
.pnigC	fast C Implementation of function pnig()
.qnigC	fast CImplementation of function qnig()
nigFit	Fits parameters of a NIG distribution
.nigFit.mle	Uses max Log-likelihood estimation
.nigFit.gmm	Uses generalized method of moments
.nigFit.mps	Maximum product spacings estimation

.nigFit.vmps	Minimum variance mps estimation
nigMode	Computes mode of the NIG distribution
nigMean	Returns true mean of the NIG distribution
nigVar	Returns true variance of the NIG distribution
nigSkew	Returns true skewness of the NIG distribution
nigKurt	Returns true kurtosis of the NIG distribution
nigMoments	Returns true n-th moment of the NIG distribution
nigMED	Returns true median of the NIG distribution
nigIQR	Returns true inter quartal range of the NIG
nigSKEW	Returns true robust skewness of the NIG
nigKURT	Returns true robust kurtosis of the NIG

Generalized Hyperbolic Student-t Distribution:

dght	Returns density for the GHT distribution
pght	Returns probability for the GHT distribution
qght	Returns quantiles for the GHT distribution
rght	Returns random variates for the GHT distribution
ghtFit	Fits parameters of the GHT distribution
ghtMode	Computes mode of the GHT distribution
ghtMean	Returns true mean of the NIG distribution
ghtVar	Returns true variance of the GHT distribution
ghtSkew	Returns true skewness of the GHT distribution
ghtKurt	Returns true kurtosis of the GHT distribution
ghtMoments	Returns true n-th moment of the GHT distribution
ghtMED	Returns true median of the GHT distribution
ghtIQR	Returns true inter quartal range of the GHT
ghtSKEW	Returns true robust skewness of the GHT
ghtKURT	Returns true robust kurtosis of the GHT

Stable Distribution:

dstable	Returns density for the stable distribution
pstable	Returns probability for the stable distribution
qstable	Returns quantiles for the stable distribution
rstable	Returns random variates for the dtsble distribution
stableFit	Fits parameters of a the stable distribution
.phiStable	Creates contour table for McCulloch estimators
.PhiStable	Contour table created by function .phiStable()
.qStableFit	Estimates parameters by McCulloch's approach
.mleStableFit	Estimates stable parameters by MLE approach
.stablePlot	Plots results of stable parameter estimates
stableMode	Computes mode of the stable distribution

Generalized Lambda Distribution:

dgld	Returns density for the GLD distribution
pgld	Returns probability for the GLD distribution
qgld	Returns quantiles for the GLD distribution
rgld	Returns random variates for the GLD distribution
gldFit	Fits parameters of the GLD distribution
.gldFit.mle	fits GLD using maximum log-likelihood
.gldFit.mps	fits GLD using maximum product spacings
.gldFit.gof	fits GLD using Goodness of Fit statistics
.gldFit.hist	fits GLD using a histogram fit
.gldFit.rob	fits GLD using robust moments fit
gldMode	Computes mode of the GLD distribution.
gldMED	Returns true median of the GLD distribution
gldIQR	Returns true inter quartal range of the GLD
gldSKEW	Returns true robust skewness of the GLD
gldKURT	Returns true robust kurtosis of the GLD

Spline Smoothed Distribution:

dssd	Returns spline smoothed density function
pssd	Returns spline smoothed probability function
qssd	Returns spline smoothed quantile function
rssd	Returns spline smoothed random variates.
ssdFit	Fits parameters for a spline smoothed distribution

4 Hypthesis Testing

One Sample Nornality Tests:

ksnormTest	One sample Kolmogorov-Smirnov normality test
shapiroTest	Shapiro-Wilk normality test
jarqueberaTest	Jarque-Bera normality test
normalTest	Normality tests S-Plus compatible call
dagoTest	D'Agostino normality test
adTest	Anderson-Darling normality test
cvmTest	Cramer-von Mises normality test
lillieTest	Lilliefors (KS) normality test
pchiTest	Pearson chi-square normality test
sfTest	Shapiro-Francia normality test
jbTest	Finite sample adjusted JB LM and ALM test

One Sample Location, Scale and variance Tests:

```
locationTest          Performs locations tests on two samples
  .tTest              Unpaired t test for differences in mean
  .kw2Test            Kruskal-Wallis test for differences in locations
scaleTest             Performs scale tests on two samples
  .ansariTest         Ansari-Bradley test for differences in scale
  .moodTest           Mood test for differences in scale
varianceTest          Performs variance tests on two samples
  .varfTest           F test for differences in variances
  .bartlett2Test      Bartlett's test for differences in variances
  .fligner2Test       Fligner-Killeen test for differences in variances
```

Two Sample Tests:

```
ks2Test               Performs a two sample Kolmogorov-Smirnov test
correlationTest       Performs correlation tests on two samples
pearsonTest           Pearson product moment correlation coefficient
kendallTest           Kendall's tau correlation test
spearmanTest          Spearman's rho correlation test
```

Test Utilities:

```
'fHTEST'              S4 Class Representation
show.fHTEST           S4 Print Method
  .jbALM              Jarque Bera Augmented Lagrange Multiplier Data
  .jbLM               Jarque-Bera Lagrange Multiplier Data
  .jbTable            Finite sample p values for the Jarque Bera test
  .jbPlot             Plots probabilities
  .pjb                Returns probabilities for JB given quantiles
  .qjb                Returns quantiles for JB given probabilities
```

5 Plotting Routines

Financial Time Series Plots:

```
seriesPlot            Dispalys a time series plot
cumulatedPlot         Displays cumulated series give returns
returnPlot            Displays returns given cumulated series
drawdownPlot          Displays drawdown series from returns
```

Correlation Plots:

```
acfPlot               Displays tailored ACF plot
pacfPlot              Displays tailored partial ACF plot
teffectPlot           Displays the Taylor effect
lacfPlot              Displays lagged autocorrelations
```

Distribution Plots:

```
histPlot              Returns tailored histogram plot
densityPlot           Returns tailored density plot
logDensityPlot        Returns tailored log density plot
boxPlot               Returns side-by-side standard box plot
boxPercentile         Plotreturns box-percentile plot
qqnormPlot            Returns normal quantile-quantile plot
qqnigPlot             Returns NIG quantile-quantile plot
qqghtPlot             Rreturns  GHT quantile-quantile plot
qqgldPlot             Returns GLD quantile-quantile plot
```

Time Series Aggregation Plots:

```
scalinglawPlot        Displays scaling law behavior
```

5. Matrix Computations and Linear Algebra

Elementar Matrix Operation Addons:

```
kron                  Returns the Kronecker product
vec                   Stacks a matrix as column vector
vech                  Stacks a lower triangle matrix
pdl                   Returns regressor matrix for polynomial lags
tslag                 Returns Lagged/leading vector/matrix
```

Linear Algebra Addons:

```
inv                   Returns the inverse of a matrix
norm                  Returns the norm of a matrix
rk                    Returns the rank of a matrix
tr                    Returns the trace of a matrix
```

General Matrix Utility Addons:

```
isPositiveDefinite    Checks if a matrix is positive definite
makePositiveDefinite  Forces a matrix to be positive definite
colVec                Creates a column vector from a data vector
rowVec                Creates a row vector from a data vector
gridVector            Creates from two vectors rectangular grid
triang                Extracs lower tridiagonal part from a matrix
Triang                Extracs upper tridiagonal part from a matrix
```

Selected Matrix Examples:

```
hilbert              Creates a Hilbert matrix
pascal               Creates a Pascal matrix
```

6 Utility Functions

Color Utilities:

```
colorLocator           Plots Rs 657 named colors for selection
colorMatrix            Returns matrix of R's color names.
colorTable             Table of Color Codes and Plot Colors itself
rainbowPalette         Contiguous rainbow color palette
heatPalette            Contiguous heat color palette
terrainPalette         Contiguous terrain color palette
topoPalette            Contiguous topo color palette
cmPalette              Contiguous cm color palette
greyPalette            R's gamma-corrected gray palette
timPalette             Tim's Matlab like color palette
rampPalette            Color ramp palettes
seqPalette             Sequential color brewer palettes
divPalette             Diverging color brewer palettes
qualiPalette           Qualified color brewer palettes
focusPalette           Red, green blue focus palettes
monoPalette            Red, green blue mono palettes
```

Graphics Utilities:

```
symbolTable            Shows a table of plot symbols
characterTable         Shows a table of character codes
decor                  Adds horizontal grid and L shaped box
hgrid                  Adds horizontal grid lines
vgrid                  Adds vertical grid lines
boxL                   Adds L-shaped box
box                    Adds unterlined box
  .xrug                Adds rugs on x axis
  .yrug                Adds rugs on y axis
copyright              Adds copyright notice
interactivePlot        Plots several graphs interactively
```

Special Function Utilities:

```
Heaviside              Computes Heaviside unit step function
Sign                   Another signum function
Delta                  Computes delta function
```

```
Boxcar                Computes boxcar function
Ramp                  Computes ramp function
tsHessian             Computes Two Sided Hessian matrix
```

Other Utilities:

```
.unirootNA            Computes zero of a function without error exit
getModel              Extracts the model slot from a S4 object
getTitle              Extracts the title slot from a S4 object
getDescription        Extracts the description slot
getSlot               Extracts a specified slot from a S4 object
```

About Builtin Functions

Builtin functions are borrowed from contributed R packages and other sources. There are several reasons why we have modified and copied code from other sources and included in this package.

* The builtin code is not available on Debian, so that Linux users have no easy acces to this code.

* The original code conflicts with other code from this package or conflicts with Rmetrics design objectives.

* We only need a very small piece of functionality from the original package which may depend on other packages which are not needed.

* The package from which we builtin the code is under current development, so that the functions often change and thus leads to unexpectect behavior in the Rmetrics packages.

* The package may be incompatible since it uses other time date and time series classes than the 'timeDate' and 'timeSeries' objects and methods from Rmetrics.

We put the code in script files named *builtin-funPackage.R* where "fun" denotes the (optional) major function name, and "Package" the name of the contributed package from which we copied the original code.

Builtin functions include:

```
gelGmm                gll function from gmm package
gmmGMM                gmm function from gmm package
kweightsSandwhich     kweights from sandwhich package
glGld                 gl functions from gld package
ssdenGss              ssden from the gss package
hypHyperbolicDist     hyp from HyperbolicDist package
```

Compiled Fortran and C Code:

```
gld.c                 source code from gld package
nig.c                 source code from Kersti Aas
gss.f                 source code fromsandwhich package
```

About Rmetrics:

The `fBasics` Rmetrics package is written for educational support in teaching "Computational Finance and Financial Engineering" and licensed under the GPL.

`acfPlot` *Autocorrelation Function Plots*

Description

Returns plots of autocorrelations including the autocorrelation function ACF, the partial ACF, the lagged ACF, and the Taylor effect plot.

The functions to display stylized facts are:

`acfPlot`	autocorrelation function plot,
`pacfPlot`	partial autocorrelation function plot,
`lacfPlot`	lagged autocorrelation function plot,
`teffectPlot`	Taylor effect plot.

Usage

```
acfPlot(x, labels = TRUE, ...)
pacfPlot(x, labels = TRUE, ...)

lacfPlot(x, n = 12, lag.max = 20, type = c("returns", "values"),
    labels = TRUE, ...)

teffectPlot(x, deltas = seq(from = 0.2, to = 3, by = 0.2), lag.max = 10,
    ymax = NA, standardize = TRUE, labels = TRUE, ...)
```

Arguments

`deltas`	the exponents, a numeric vector, by default ranging from 0.2 to 3.0 in steps of 0.2.
`labels`	a logical value. Whether or not x- and y-axes should be automatically labeled and a default main title should be added to the plot. By default `TRUE`.
`lag.max`	maximum lag for which the autocorrelation should be calculated, an integer.
`n`	an integer value, the number of lags.
`standardize`	a logical value. Should the vector `x` be standardized?
`type`	[lacf] - a character string which specifies the type of the input series, either "returns" or series "values". In the case of a return series as input, the required value series is computed by cumulating the financial returns: `exp(colCumsums(x))`

x	an uni- or multivariate return series of class timeSeries or any other object which can be transformed by the function as.timeSeries() into an object of class timeSeries.
ymax	maximum y-axis value on plot, is.na(ymax) TRUE, then the value is selected automatically.
...	arguments to be passed.

Details

Autocorrelation Functions:

The functions acfPlot and pacfPlot, plot and estimate autocorrelation and partial autocorrelation function. The functions allow to get a first view on correlations within the time series. The functions are synonyme function calls for R's acf and pacf from the the ts package.

Taylor Effect:

The "Taylor Effect" describes the fact that absolute returns of speculative assets have significant serial correlation over long lags. Even more, autocorrelations of absolute returns are typically greater than those of squared returns. From these observations the Taylor effect states, that that the autocorrelations of absolute returns to the the power of delta, abs(x-mean(x))^delta reach their maximum at delta=1. The function teffect explores this behaviour. A plot is created which shows for each lag (from 1 to max.lag) the autocorrelations as a function of the exponent delta. In the case that the above formulated hypothesis is supported, all the curves should peak at the same value around delta=1.

Value

acfPlot, pacfplot,
return an object of class "acf", see acf.

lacfPlot returns a list with the following two elements: Rho, the autocorrelation function, lagged, the lagged correlations.

teffectPlot
returns a numeric matrix of order deltas by max.lag with the values of the autocorrelations.

References

Taylor S.J. (1986); *Modeling Financial Time Series*, John Wiley and Sons, Chichester.

Ding Z., Granger C.W.J., Engle R.F. (1993); *A long memory property of stock market returns and a new model*, Journal of Empirical Finance 1, 83.

Examples

```
## data -
   data(LPP2005REC, package = "timeSeries")
```

```
   SPI <- LPP2005REC[, "SPI"]
   plot(SPI, type = "l", col = "steelblue", main = "SP500")
   abline(h = 0, col = "grey")

## teffectPlot -
   # Taylor Effect:
   teffectPlot(SPI)
```

---

akimaInterp *Bivariate Spline Interpolation*

Description

Interpolates bivariate data sets using Akima spline interpolation.

Usage

```
akimaInterp(x, y = NULL, z = NULL, gridPoints = 21,
    xo = seq(min(x), max(x), length = gridPoints),
    yo = seq(min(y), max(y), length = gridPoints), extrap = FALSE)

akimaInterpp(x, y = NULL, z = NULL, xo, yo, extrap = FALSE)
```

Arguments

x, y, z	for akimaInterp the arguments x and y are two numeric vectors of grid pounts, and z is a numeric matrix or any other rectangular object which can be transformed by the function as.matrix into a matrix object. For akimaInterpp we consider either three numeric vectors of equal length or if y and z are NULL, a list with entries x, y, z, or named data frame with x in the first, y in the second, and z in the third column.
gridPoints	an integer value specifying the number of grid points in x and y direction.
xo, yo	for akimaInterp two numeric vectors of data points spanning the grid, and for akimaInterpp two numeric vectors of data points building pairs for pointwise interpolation.
extrap	a logical, if TRUE then the data points are extrapolated.

Details

Two options are available gridded and pointwise interpolation.

akimaInterp is a function wrapper to the interp function provided by the contributed R package akima. The Fortran code of the Akima spline interpolation routine was written by H. Akima.

Linear surface fitting and krige surface fitting are provided by the functions linearInterp and krigeInterp.

Value

akimaInterp returns a list with at least three entries, `x`, `y` and `z`. Note, that the returned values, can be directly used by the `persp` and `contour` 3D plotting methods.

akimaInterpp returns a data.frame with columns `"x"`, `"y"`, and `"z"`.

Note

IMPORTANT: The contributed package **akima** is not in the dependence list of the DESCRIPTION file due to license conditions. The user has to install this package from CRAN on his own responsibility, please check the license conditions.

References

Akima H., 1978, *A Method of Bivariate Interpolation and Smooth Surface Fitting for Irregularly Distributed Data Points*, ACM Transactions on Mathematical Software 4, 149-164.

Akima H., 1996, *Algorithm 761: Scattered-Data Surface Fitting that has the Accuracy of a Cubic Polynomial*, ACM Transactions on Mathematical Software 22, 362-371.

See Also

`linearInterp`, `krigeInterp`.

Examples

```
## Does not run for r-solaris-x86
## akimaInterp -- Akima Interpolation:
if (requireNamespace("interp")) {
  set.seed(1953)
  x <- runif(999) - 0.5
  y <- runif(999) - 0.5
  z <- cos(2*pi*(x^2+y^2))
  ans <- akimaInterp(x, y, z, gridPoints = 41, extrap = FALSE)
  persp(ans, theta = -40, phi = 30, col = "steelblue",
       xlab = "x", ylab = "y", zlab = "z")
  contour(ans)
}

## Use spatial as alternative on r-solaris-x86
## spatialInterp - Generate Kriged Grid Data:
if (requireNamespace("spatial")) {
  RNGkind(kind = "Marsaglia-Multicarry", normal.kind = "Inversion")
  set.seed(4711, kind = "Marsaglia-Multicarry")
  x <- runif(999)-0.5
  y <- runif(999)-0.5
  z <- cos(2*pi*(x^2+y^2))
  ans <- krigeInterp(x, y, z, extrap = FALSE)
  persp(ans)
  title(main = "Kriging")
  contour(ans)
```

```
  title(main = "Kriging")
}
```

---

baseMethods *Generic Functions Extensions*

Description

Basic extensions which add and/or modify additional functionality which is not available in R's basic packages.

Added and/or modified functions:

attach	extends attach function,
rank	extends rank function,
stdev	adds stdev function,
termPlot	adds term plot function,
volatility	adds volatility function.

Usage

```
## Default S3 method:
stdev(x, na.rm = FALSE)

## Default S3 method:
termPlot(model, ...)

## Default S3 method:
volatility(object, ...)
```

Arguments

na.rm	an logical value - should the NA values be removed.
model	a fitted model object.
object	an object from which to extract the volatility.
x	[align] - x-coordinates of the points to be aligned. [log][sort][var] - first argument. [print.control] - cr prints an unlisted object of class control. [as.matrix.ts][as.matrix.mts] - an univariate or multivariate time series object of class "ts" or "mts" which will be transformed into an one-column or multi-column rectangular object of class "matrix". [as.POSIXlt] - an object to be converted.

... arguments to be passed.

Details

For details we refer to the original help pages.

`BasicStatistics` *Basic Time Series Statistics*

Description

Computes basic financial time series statististics.

List of Functions:

`basicStats` Computes an overview of basic statistical values.

Usage

```
basicStats(x, ci = 0.95)
```

Arguments

`ci`	confidence interval, a numeric value, by default 0.95, i.e. 95 percent.
`x`	an object of class `"timeSeries"` or any other object which can be transformed by the function `as.timeSeries` into an object of class `timeSeries`. The latter case, other then `timeSeries` objects, is more or less untested.

Value

`basicsStats`
returns a data frame with the following entries and row names: nobs, NAs, Minimum, Maximum , 1. Quartile, 3. Quartile, Mean, Median, Sum, SE Mean, LCL Mean, UCL Mean, Variance, Stdev, Skewness, Kurtosis.

Examples

```
## basicStats -
   # Simulated Monthly Return Data:
   tS = timeSeries(matrix(rnorm(12)), timeDate::timeCalendar())
   basicStats(tS)
```

BoxPlot *Time Series Box Plots*

Description

Returns a box or a box percentile plot.

List of Functions:

boxPlot	Returns a side-by-side standard box plot,
boxPercentilePlot	Returns a side-by-side box-percentile plot.

Usage

```
boxPlot(x, col = "steelblue", title = TRUE, ...)
boxPercentilePlot(x, col = "steelblue", title = TRUE, ...)
```

Arguments

col	the color for the series. In the univariate case use just a color name like the default, col="steelblue", in the multivariate case we recommend to select the colors from a color palette, e.g. col=heat.colors(ncol(x)).
title	a logical flag, by default TRUE. Should a default title added to the plot?
x	an object of class "timeSeries" or any other object which can be transformed by the function as.timeSeries into an object of class timeSeries. The latter case, other then timeSeries objects, is more or less untested.
...	optional arguments to be passed.

Value

displays a time series plot.

Examples

```
## data -
   data(LPP2005REC, package = "timeSeries")
   LPP <- LPP2005REC[, 1:6]
   plot(LPP, type = "l", col = "steelblue", main = "SP500")
   abline(h = 0, col = "grey")

## boxPlot -
   boxPlot(LPP)
```

characterTable *Table of Characters*

Description

Displays a table of numerical equivalents to Latin characters.

Usage

```
characterTable(font = 1, cex = 0.7)
```

Arguments

cex	a numeric value, determines the character size, the default size is 0.7.
font	an integer value, the number of the font, by default font number 1.

Value

characterTable

displays a table with the characters of the requested font. The character on line "xy" and column "z" of the table has code "\xyz", e.g cat("\126") prints: V for font number 1. These codes can be used as any other characters.

See Also

link{colorTable}, link{symbolTable}.

Examples

```
## Character Table for Font 2:
# characterTable(font = 1)
```

colorLocator *Color Selection*

Description

Displays R's 657 named colors for selection and returns optionally R's color names.

Usage

```
colorLocator(locator = FALSE, cex.axis = 0.7)
colorMatrix()
```

Arguments

locator	logical, if true, locator is used for interactive selection of color names, default is FALSE.
cex.axis	size of axis labels.

Details

Color Locator:

The colorLocator function plots R's 657 named colors. If locator=TRUE then you can interactively point and click to select the colors for which you want names. To end selection, right click on the mouse and select 'Stop', then R returns the selected color names.

The functions used here are wrappers to the functions provided by Tomas Aragon in the contributed R package. epitools.

Value

Color Locator:

colorsLocator() generates a plot with R colors and, when locator is true, returns matrix with graph coordinates and names of colors selected. colorsMatrix() quietly returns the matrix of names.

See Also

colorPalette, colorTable.

Examples

```
colorLocator()
```

---

colorPalette *Color Palettes*

Description

Functions to create color palettes.

The functions are:

rainbowPalette	Contiguous rainbow color palette,
heatPalette	Contiguous heat color palette,
terrainPalette	Contiguous terrain color palette,
topoPalette	Contiguous topo color palette,
cmPalette	Contiguous cm color palette,
greyPalette	R's gamma-corrected gray palette,
timPalette	Tim's Matlab like color palette,
rampPalette	Color ramp palettes,

seqPalette	Sequential color brewer palettes,
divPalette	Diverging color brewer palettes,
qualiPalette	Qualified color brewer palettes,
focusPalette	Red, green blue focus palettes,
monoPalette	Red, green blue mono palettes.

Usage

```
rainbowPalette(n = 64, ...)
heatPalette(n = 64, ...)
terrainPalette(n = 64, ...)
topoPalette(n = 64, ...)
cmPalette(n = 64, ...)

greyPalette(n = 64, ...)
timPalette(n = 64)

rampPalette(n, name = c("blue2red", "green2red", "blue2green",
    "purple2green", "blue2yellow", "cyan2magenta"))

seqPalette(n, name = c(
    "Blues", "BuGn", "BuPu", "GnBu", "Greens", "Greys", "Oranges",
    "OrRd", "PuBu", "PuBuGn", "PuRd", "Purples", "RdPu", "Reds",
    "YlGn", "YlGnBu", "YlOrBr", "YlOrRd"))
divPalette(n, name = c(
    "BrBG", "PiYG", "PRGn", "PuOr", "RdBu", "RdGy", "RdYlBu", "RdYlGn",
    "Spectral"))
qualiPalette(n, name = c(
    "Accent", "Dark2", "Paired", "Pastel1", "Pastel2", "Set1", "Set2",
    "Set3"))

focusPalette(n, name = c("redfocus", "greenfocus", "bluefocus"))
monoPalette(n, name = c("redmono", "greenmono", "bluemono"))
```

Arguments

n	an integer, giving the number of greys or colors to be constructed.
name	a character string, the name of the color set.
...	arguments to be passed, see the details section

Details

All Rmetrics' color sets are named as `fooPalette` where the prefix `foo` denotes the name of the underlying color set.

R's Contiguous Color Palettes:

Palettes for n contiguous colors are implemented in the grDevices package. To be conform with Rmetrics' naming convention for color palettes we have build a wrapper around the underlying functions. These are the rainbowPalette, heatPalette, terrainPalette, topoPalette, and the cmPalette. Conceptually, all of these functions actually use (parts of) a line cut out of the 3-dimensional color space, parametrized by the function hsv(h,s,v,gamma), where gamma=1 for the fooPalette function, and hence, equispaced hues in RGB space tend to cluster at the red, green and blue primaries. Some applications such as contouring require a palette of colors which do not wrap around to give a final color close to the starting one. To pass additional arguments to the underlying functions we refer to consult help(rainbow). With rainbow, the parameters start and end can be used to specify particular subranges of hues. Synonyme function calls are rainbow, heat.colors,terrain.colors, topo.colors, and the cm.colors.

R's Gamma-Corrected Gray Palette:

The function grayPalette chooses a series of n gamma-corrected gray levels. The range of the gray levels can be optionally monitored through the ... arguments, for details help(gray.colors), which is a synonyme function call in the grDevices package.

Tim's Matlab like Color Palette:

The function timPalette creates a color set ranging from blue to red, and passes through the colors cyan, yellow, and orange. It comes from the Matlab software, originally used in fluid dynamics simulations. The function here is a copy from R's contributed package fields doing a spline interpolation on n=64 color points.

Color Ramp Palettes:

The function rampPalette creates several color ramps. The function is implemented from Tim Keitt's contributed R package colorRamps. Supported through the argument name are the following color ramps: "blue2red", "green2red", "blue2green", "purple2green", "blue2yellow", "cyan2magenta".

Color Brewer Palettes:

The functions seqPalette, divPalette, and qualiPalette create color sets according to R's contributed RColorBrewer package. The first letter in the function name denotes the type of the color set: "s" for sequential palettes, 'd" for diverging palettes, and "q" for qualitative palettes.
Sequential palettes are suited to ordered data that progress from low to high. Lightness steps dominate the look of these schemes, with light colors for low data values to dark colors for high data values. The sequential palettes names are: Blues, BuGn, BuPu, GnBu, Greens, Greys, Oranges, OrRd, PuBu, PuBuGn, PuRd, Purples, RdPu, Reds, YlGn, YlGnBu, YlOrBr, YlOrRd.
Diverging palettes put equal emphasis on mid-range critical values and extremes at both ends of the data range. The critical class or break in the middle of the legend is emphasized with light colors and low and high extremes are emphasized with dark colors that have contrasting hues. The diverging palettes names are: BrBG, PiYG, PRGn, PuOr, RdBu, RdGy, RdYlBu, RdYlGn, Spectral.
Qualitative palettes do not imply magnitude differences between legend classes, and hues are used to create the primary visual differences between classes. Qualitative schemes are best suited to rep-

resenting nominal or categorical data. The qualitative palettes names are: Accent, Dark2, Paired, Pastel1, Pastel2, Set1, Set2, Set3.
In contrast to the original color brewer palettes, the palettes here are created by spline interpolation from the color variation with the most different values, i.e for the sequential palettes these are 9 values, for the diverging palettes these are 11 values, and for the qualitative palettes these are between 8 and 12 values dependeing on the color set.

Graph Color Palettes:

The function `perfanPalette` creates color sets inspired by R's cotributed package `Performance Analytics`. These color palettes have been designed to create readable, comparable line and bar graphs with specific objectives.
Focused Color Palettes: Color sets designed to provide focus to the data graphed as the first element. This palette is best used when there is clearly an important data set for the viewer to focus on, with the remaining data being secondary, tertiary, etc. Later elements graphed in diminishing values of gray.
Monchrome Color Palettes: These include color sets for monochrome color displays.

Value

returns a character string of color strings.

Note

The palettes are wrapper functions provided in several contributed R packages. These include:

Cynthia Brewer and Mark Harrower for the brewer palettes,
Peter Carl and Brian G. Peterson for the "PerformanceAnalytics" package,
Tim Keitt for the "colorRamps" package,
Ross Ihaka for the "colorspace" package,
Tomas Aragon for the "epitools" package,
Doug Nychka for the "fields" package,
Erich Neuwirth for the "RColorBrewer" package.

Additional undocumented hidden functions:

`.asRGB`	Converts any R color to RGB (red/green/blue),
`.chcode`	Changes from one to another number system,
`.hex.to.dec`	Converts heximal numbers do decimal numbers,
`.dec.to.hex`	Converts decimal numbers do heximal numbers.

Examples

```
## GreyPalette:
   greyPalette()
```

colorTable *Table of Colors*

Description

Displays a Table of color codes and plots the colors themselves.

Usage

```
colorTable(cex = 0.7)
```

Arguments

cex	a numeric value, determines the character size in the color plot, the default size is 0.7.

Value

colorTable

returns a table of plot plot colors with the associated color numbers.

See Also

link{characterTable}, link{symbolTable}.

Examples

```
## Color Table:
   colorTable()
```

colVec *Column and Row Vectors*

Description

Creates a column or row vector from a numeric vector.

Usage

```
colVec(x)
rowVec(x)
```

Arguments

x	a numeric vector.

Details

The functions `colVec` and `rowVec` transform a vector into a column and row vector, respectively. A column vector is a matrix object with one column, and a row vector is a matrix object with one row.

Examples

```
## Create a numeric Vector:
   x = rnorm(5)

## Column and Row Vectors:
   colVec(x)
   rowVec(x)
```

---

correlationTest *Correlation Tests*

Description

Tests if two series are correlated.

Usage

```
correlationTest(x, y, method = c("pearson", "kendall", "spearman"),
    title = NULL, description = NULL)


pearsonTest(x, y, title = NULL, description = NULL)
kendallTest(x, y, title = NULL, description = NULL)
spearmanTest(x, y, title = NULL, description = NULL)
```

Arguments

`x, y`	numeric vectors of data values.
`method`	a character string naming which test should be applied.
`title`	an optional title string, if not specified the inputs data name is deparsed.
`description`	optional description string, or a vector of character strings.

Details

The function `correlationTest` tests for association between paired samples allowing to compute Pearson's product moment correlation coefficient, Kendall's tau, or Spearman's rho.

Value

In contrast to R's output report from S3 objects of class `"htest"` a different output report is produced. The classical tests presented here return an S4 object of class `"fHTEST"`. The object contains the following slots:

`@call`	the function call.
`@data`	the data as specified by the input argument(s).
`@test`	a list whose elements contain the results from the statistical test. The information provided is similar to a list object of class `"htest"`.
`@title`	a character string with the name of the test. This can be overwritten specifying a user defined input argument.
`@description`	a character string with an optional user defined description. By default just the current date when the test was applied will be returned.

The slot `@test` returns an object of class `"list"` containing (at least) the following elements:

`statistic`	the value(s) of the test statistic.
`p.value`	the p-value(s) of the test.
`parameters`	a numeric value or vector of parameters.
`estimate`	a numeric value or vector of sample estimates.
`conf.int`	a numeric two row vector or matrix of 95
`method`	a character string indicating what type of test was performed.
`data.name`	a character string giving the name(s) of the data.

Note

Some of the test implementations are selected from R's `ctest` package.

Author(s)

R-core team for hypothesis tests implemented from R's package `ctest`.

References

Conover, W. J. (1971); *Practical nonparametric statistics*, New York: John Wiley & Sons.

Lehmann E.L. (1986); *Testing Statistical Hypotheses*, John Wiley and Sons, New York.

See Also

`locationTest`, `scaleTest`, `varianceTest`.

Examples

```
## x, y -
   x = rnorm(50)
   y = rnorm(50)

## correlationTest -
   correlationTest(x, y, "pearson")
   correlationTest(x, y, "kendall")
   spearmanTest(x, y)
```

`decor` *Functions for decorating plots*

Description

Functions for decorating plots.

Usage

```
decor()

hgrid(ny = NULL, ...)
vgrid(nx = NULL, ...)

boxL(col = "white")
box_(col = c("white", "black"))

copyright()
```

Arguments

`col`	the color of the background, `"black"` and foreground `"white"` lines of the box.
`nx, ny`	number of cells of the grid in `x` or `y` direction. When `NULL`, as per default, the grid aligns with the tick marks on the corresponding default axis (i.e., tick marks as computed by axTicks).
`...`	additional arguments passed to the `grid()` function.

Details

The plot decorating functions are:

decor simple decoration function, equivalent to `hgrid()` followed by `boxL()`,

hgrid creates horizontal grid lines,

vgrid creates vertical grid lines,

boxL creates an L-shaped box,

box_ creates a bottom line box,

copyright adds Rmetrics copyright to a plot.

Examples

```
## Test Plot Function:
   plot(x = rnorm(100), type = "l", col = "red",
     xlab = "", ylab = "Variates", las = 1)
   title("Normal Deviates", adj = 0)
   hgrid()
   boxL()
   copyright()
```

---

distCheck *Distribution Check*

Description

Tests properties of an R implementation of a distribution, i.e. of all four of its "dpqr" functions.

Usage

```
distCheck(fun = "norm", n = 1000, robust = TRUE, subdivisions = 100, ...)
```

Arguments

fun	a character string denoting the name of the distribution.
n	an integer specifying the number of random variates to be generated.
robust	logical flag, should robust estimates be used? By default TRUE.
subdivisions	integer specifying the numbers of subdivisions in integration.
...	the distributional parameters.

Examples

```
distCheck("norm", mean = 1, sd = 1)

distCheck("lnorm", meanlog = 0.5, sdlog = 2, robust=FALSE)
## here, true E(X) = exp(mu + 1/2 sigma^2) = exp(.5 + 2) = exp(2.5) = 12.182
## and      Var(X) = exp(2*mu + sigma^2)*(exp(sigma^2) - 1) =       7954.67
```

DistributionFits *Parameter Fit of a Distribution*

Description

A collection and description of moment and maximum likelihood estimators to fit the parameters of a distribution.

The functions are:

nFit	MLE parameter fit for a normal distribution,
tFit	MLE parameter fit for a Student t-distribution,
stableFit	MLE and Quantile Method stable parameter fit.

Usage

```
nFit(x, doplot = TRUE, span = "auto", title = NULL, description = NULL, ...)

tFit(x, df = 4, doplot = TRUE, span = "auto", trace = FALSE, title = NULL,
    description = NULL, ...)

stableFit(x, alpha = 1.75, beta = 0, gamma = 1, delta = 0,
    type = c("q", "mle"), doplot = TRUE, control = list(),
    trace = FALSE, title = NULL, description = NULL)

## S4 method for signature 'fDISTFIT'
show(object)
```

Arguments

control	[stableFit] - a list of control parameters, see function nlminb.
alpha, beta, gamma, delta	[stable] - The parameters are alpha, beta, gamma, and delta: value of the index parameter alpha with alpha = (0,2]; skewness parameter beta, in the range [-1, 1]; scale parameter gamma; and shift parameter delta.
description	a character string which allows for a brief description.
df	the number of degrees of freedom for the Student distribution, df > 2, maybe non-integer. By default a value of 4 is assumed.
object	[show] - an S4 class object as returned from the fitting functions.
doplot	a logical flag. Should a plot be displayed?
span	x-coordinates for the plot, by default 100 values automatically selected and ranging between the 0.001, and 0.999 quantiles. Alternatively, you can specify the range by an expression like span=seq(min, max, times = n), where, min and max are the left and right endpoints of the range, and n gives the number of the intermediate points.
title	a character string which allows for a project title.
trace	a logical flag. Should the parameter estimation process be traced?
type	a character string which allows to select the method for parameter estimation: "mle", the maximum log likelihood approach, or "qm", McCulloch's quantile method.
x	a numeric vector.
...	parameters to be parsed.

Details

Stable Parameter Estimation:

Estimation techniques based on the quantiles of an empirical sample were first suggested by Fama and Roll [1971]. However their technique was limited to symmetric distributions and suffered from a small asymptotic bias. McCulloch [1986] developed a technique that uses five quantiles from a sample to estimate `alpha` and `beta` without asymptotic bias. Unfortunately, the estimators provided by McCulloch have restriction `alpha>0.6`.

Value

The functions `tFit`, `hypFit` and `nigFit` return a list with the following components:

`estimate`	the point at which the maximum value of the log liklihood function is obtained.
`minimum`	the value of the estimated maximum, i.e. the value of the log liklihood function.
`code`	an integer indicating why the optimization process terminated.
`gradient`	the gradient at the estimated maximum.

Remark: The parameter estimation for the stable distribution via the maximum Log-Likelihood approach may take a quite long time.

Examples

```
## nFit -
   # Simulate random normal variates N(0.5, 2.0):
   set.seed(1953)
   s = rnorm(n = 1000, 0.5, 2)

## nigFit -
   # Fit Parameters:
   nFit(s, doplot = TRUE)
```

`fBasics-deprecated` *Deprecated Functions in Package fBasics*

Description

These functions are provided for compatibility with older versions of the package only, and may be defunct as soon as of the next release.

There are none currently. `dstable` etc now are defunct, as they have been available from **stabledist** since early 2011.

See Also

`Deprecated`, `Defunct`

fBasicsData *fBasics Data Sets*

Description

The following data sets are part of this package:

Capitalization	Market capitalization of domestic companies,
cars2	Data for various car models,
DowJones30	Down Jones 30 stocks,
HedgeFund	Hennessee Hedge Fund Indices,
msft.dat	Daily Microsoft OHLC prices and volume,
nyse	NYSE composite Index,
PensionFund	Swiss Pension Fund LPP-2005,
swissEconomy	Swiss Economic Data,
SWXLP	Swiss Pension Fund LPP-2000,
usdthb	Tick data of USD to THB.

Details

Capitalization:
Capitalization contains market capitalization of domestic companies from 2003 - 2008 in USD millions.

cars2:
cars2 contains the price, country, reliability, mileage, type, weight, engine displacement and net horsepower of various car models.

DowJones30:
DowJones30 contains daily observations from the Dow Jones 30 Index series. Each of the thirty columns represents the closing price of a stock in the Index.

HedgeFund:
HedgeFund contains monthly percentual returns of various hedge fund strategies from Hennessee Group LLC.

msft.dat:
msft.dat contains daily prices (open, high, low and close) and volumes for the Microsoft stocks.

nyse:
nyse contains daily records of the NYSE Composite Index.

PensionFund:
PensionFund is a daily data set of the Swiss pension fund benchmark LPP-2005. The data set ranges from 2005-11-01 to 2007-04-11. The columns are named: SBI, SPI, SII, LMI, MPI, ALT, LPP25, LPP40, LPP60

swissEconomy:
swissEconomy contains the GDP per capita, exports, imports, interest rates, inflation, unemployment and population for the years 1964 - 1999 for Switzerland.

SWXLP:
SWXLP is a daily data set of the Swiss pension fund benchmark LPP-2000. The data set ranges from 2000-01-03 to 2007-05-08. The columns are named: SBI, SPI, SII, LP25, LP40, LP60.

usdthb:
usdthb Tick data of US Dollar (USD) in Thailand Bhat (THB) colleted from Reuters. Format: YYYYMMDDhhmm. Column variables: delay time, contributer, bid and ask prices, and quality flag. It covers the Asia FX crisis in June 1997.

References

Capitalization:
World Federation of Stock Exchanges, http://www.world-exchanges.org/statistics.

cars2:
Derived from the car90 dataset within the rpart package. The car90 dataset is based on the car.all dataset in S-PLUS. Original data comes from: April 1990, *Consumer Reports Magazine*, pages 235-255, 281-285 and 287-288.

DowJones30
http://www.yahoo.com.

HedgeFund:
http://www.hennesseegroup.com/indices/returns/year/2005.html.

msft.dat:
http://www.yahoo.com.

nyse:
http://www.nyse.com.

PensionFund:
SBI, SPI, SII: SIX (Swiss Exchange Zurich); LPP25, LPP40, LPP60: Banque Pictet Geneva; LMI, MPI, ALT: Recalculated from the indices and benchmarks

swissEconomy:
http://www.oecd.org/ and http://www.imf.org/.

SWXLP:
SBI, SPI, SII: SIX (Swiss Exchange Zurich); LPP25, LPP40, LPP60: Banque Pictet Geneva

usdthb:
Reuters Select Feed Terminal (1997).

Examples

```
## Plot DowJones30 Example Data Set
   series <- timeSeries::as.timeSeries(DowJones30)
   head(series)
   plot(series[,1:6], type = "l")
```

fHTEST *Tests Class Representation and Utilities*

Description

Class representation, methods and utility functions for objects of class 'fHTEST'.

The class representation and methods are:

fHTEST	Representation for an S4 object of class "fHTEST",
show	S4 print method.

Usage

```
## S4 method for signature 'fHTEST'
show(object)
```

Arguments

object	[show] - an S4 object of class "fHTEST".

Value

In contrast to R's output report from S3 objects of class "htest" a different output report is produced. The tests return an S4 object of class "fHTEST". The object contains the following slots:

@call	the function call.
@data	the data as specified by the input argument(s).
@test	a list whose elements contain the results from the statistical test. The information provided is similar to a list object of class "htest".
@title	a character string with the name of the test. This can be overwritten specifying a user defined input argument.
@description	a character string with an optional user defined description. By default just the current date when the test was applied will be returned.

The slot @test returns an object of class "list" containing the following elements:

statistic	the value(s) of the test statistic.
p.value	the p-value(s) of the test.
parameters	a numeric value or vector of parameters.
estimate	a numeric value or vector of sample estimates.
conf.int	a numeric two row vector or matrix of 95
method	a character string indicating what type of test was performed.
data.name	a character string giving the name(s) of the data.

Examples

```
## fHTEST -
   getClass("fHTEST")
   getSlots("fHTEST")
```

---

getS4 *General S4 Class Extractor Functions*

Description

A collection and description of functions to extract slots from S4 class objects.

The extractor functions are:

`getModel`	Extracts the model slot from a S4 object,
`getTitle`	Extracts the title slot from a S4 object,
`getDescription`	Extracts the description slot from a S4 object,
`getSlot`	Extracts a specified slot from a S4 object,
`getArgs`	Shows the arguments of a S4 function.

Since R version 2.14.0, a generic `getCall()` is part of R; for earlier versions, we had provided a simple version for S4 objects.

Usage

```
getModel(object)
getTitle(object)
getDescription(object)

getSlot(object, slotName)

getArgs(f, signature)
```

Arguments

`f`	a generic function or the character-string name of one.
`object`	an object of class S4.
`signature`	the signature of classes to match to the arguments of `f`
`slotName`	a character string, the name of the slot to be extracted from the S4 object.

Value

`getModel`
`getTitle`

getDescription
getSlot
return the content of the slot.

getArgs returns the names of the arguments.

Examples

```
## Example S4 Representation:
   # Hyothesis Testing with Control Settings
   setClass("hypTest",
     representation(
       call = "call",
       data = "numeric",
       test = "list",
       description = "character")
   )

## Shapiro Wilk Normaility Test
   swTest = function(x, description = "") {
     ans = shapiro.test(x)
     class(ans) = "list"
     new("hypTest",
       call = match.call(),
       data = x,
       test = ans,
       description = description)
   }
   test = swTest(x = rnorm(500), description = "500 RVs")

## Extractor Functions:
   isS4(test)
   getCall(test)
   getDescription(test)

## get arguments
args(returns)
getArgs(returns)
getArgs("returns")
getArgs(returns, "timeSeries")
getArgs("returns", "timeSeries")
```

---

gh *Generalized Hyperbolic Distribution*

Description

Calculates moments of the generalized hyperbbolic distribution function.

Usage

```
dgh(x, alpha = 1, beta = 0, delta = 1, mu = 0, lambda = -1/2, log = FALSE)
pgh(q, alpha = 1, beta = 0, delta = 1, mu = 0, lambda = -1/2)
qgh(p, alpha = 1, beta = 0, delta = 1, mu = 0, lambda = -1/2)
rgh(n, alpha = 1, beta = 0, delta = 1, mu = 0, lambda = -1/2)
```

Arguments

alpha, beta, delta, mu, lambda	numeric values. alpha is the first shape parameter; beta is the second shape parameter in the range (0, alpha); delta is the scale parameter, must be zero or positive; mu is the location parameter, by default 0; and lambda defines the sublclass, by default -1/2. These are the meanings of the parameters in the first parameterization pm=1 which is the default parameterization. In the second parameterization, pm=2 alpha and beta take the meaning of the shape parameters (usually named) zeta and rho. In the third parameterization, pm=3 alpha and beta take the meaning of the shape parameters (usually named) xi and chi. In the fourth parameterization, pm=4 alpha and beta take the meaning of the shape parameters (usually named) a.bar and b.bar.
log	a logical flag by default FALSE. Should labels and a main title drawn to the plot?
n	number of observations.
p	a numeric vector of probabilities.
x, q	a numeric vector of quantiles.

Details

The generator rgh is based on the GH algorithm given by Scott (2004).

Value

All values for the *gh functions are numeric vectors: d* returns the density, p* returns the distribution function, q* returns the quantile function, and r* generates random deviates.

All values have attributes named "param" listing the values of the distributional parameters.

Author(s)

David Scott for code implemented from R's contributed package HyperbolicDist.

References

Atkinson, A.C. (1982); *The simulation of generalized inverse Gaussian and hyperbolic random variables*, SIAM J. Sci. Stat. Comput. 3, 502–515.

Barndorff-Nielsen O. (1977); *Exponentially decreasing distributions for the logarithm of particle size*, Proc. Roy. Soc. Lond., A353, 401–419.

Barndorff-Nielsen O., Blaesild, P. (1983); *Hyperbolic distributions. In Encyclopedia of Statistical Sciences*, Eds., Johnson N.L., Kotz S. and Read C.B., Vol. 3, pp. 700–707. New York: Wiley.

Raible S. (2000); *Levy Processes in Finance: Theory, Numerics and Empirical Facts*, PhD Thesis, University of Freiburg, Germany, 161 pages.

Examples

```
## rgh -
   set.seed(1953)
   r = rgh(5000, alpha = 1, beta = 0.3, delta = 1)
   plot(r, type = "l", col = "steelblue",
     main = "gh: alpha=1 beta=0.3 delta=1")

## dgh -
   # Plot empirical density and compare with true density:
   hist(r, n = 25, probability = TRUE, border = "white", col = "steelblue")
   x = seq(-5, 5, 0.25)
   lines(x, dgh(x, alpha = 1, beta = 0.3, delta = 1))

## pgh -
   # Plot df and compare with true df:
   plot(sort(r), (1:5000/5000), main = "Probability", col = "steelblue")
   lines(x, pgh(x, alpha = 1, beta = 0.3, delta = 1))

## qgh -
   # Compute Quantiles:
   qgh(pgh(seq(-5, 5, 1), alpha = 1, beta = 0.3, delta = 1),
     alpha = 1, beta = 0.3, delta = 1)
```

`ghFit` *GH Distribution Fit*

Description

Estimates the distrinbutional parameters for a generalized hyperbolic distribution.

Usage

```
ghFit(x, alpha = 1, beta = 0, delta = 1, mu = 0, lambda = -1/2,
    scale = TRUE, doplot = TRUE, span = "auto", trace = TRUE,
    title = NULL, description = NULL, ...)
```

Arguments

`x`	a numeric vector.
`alpha, beta, delta, mu, lambda`	The parameters are `alpha`, `beta`, `delta`, `mu`, and and `lambda`: shape parameter `alpha`; skewness parameter `beta`, `abs(beta)` is in the range (0, alpha); scale parameter `delta`, `delta` must be zero or positive; location parameter `mu`, by default 0; and lambda parameter `lambda`, by default -1/2.
`scale`	a logical flag, by default `TRUE`. Should the time series be scaled by its standard deviation to achieve a more stable optimization?
`doplot`	a logical flag. Should a plot be displayed?

span	x-coordinates for the plot, by default 100 values automatically selected and ranging between the 0.001, and 0.999 quantiles. Alternatively, you can specify the range by an expression like span=seq(min, max, times = n), where, min and max are the left and right endpoints of the range, and n gives the number of the intermediate points.
trace	a logical flag. Should the parameter estimation process be traced?
title	a character string which allows for a project title.
description	a character string which allows for a brief description.
...	parameters to be parsed.

Details

The function nlm is used to minimize the "negative" maximum log-likelihood function. nlm carries out a minimization using a Newton-type algorithm.

Value

returns a list with the following components:

estimate	the point at which the maximum value of the log liklihood function is obtained.
minimum	the value of the estimated maximum, i.e. the value of the log liklihood function.
code	an integer indicating why the optimization process terminated. 1: relative gradient is close to zero, current iterate is probably solution; 2: successive iterates within tolerance, current iterate is probably solution; 3: last global step failed to locate a point lower than estimate. Either estimate is an approximate local minimum of the function or steptol is too small; 4: iteration limit exceeded; 5: maximum step size stepmax exceeded five consecutive times. Either the function is unbounded below, becomes asymptotic to a finite value from above in some direction or stepmax is too small.
gradient	the gradient at the estimated maximum.
steps	number of function calls.

Examples

```
## ghFit -
   # Simulate Random Variates:
   set.seed(1953)
   s = rgh(n = 1000, alpha = 1.5, beta = 0.3, delta = 0.5, mu = -1.0)

## ghFit -
   # Fit Parameters:
   ghFit(s, alpha = 1, beta = 0, delta = 1, mu = mean(s), doplot = TRUE)
```

ghMode *Generalized Hyperbolic Mode*

Description

Computes the mode of the generalized hyperbolic function.

Usage

```
ghMode(alpha = 1, beta = 0, delta = 1, mu = 0, lambda = -1/2)
```

Arguments

`alpha, beta, delta, mu, lambda`

shape parameter `alpha`; skewness parameter `beta`, `abs(beta)` is in the range (0, alpha); scale parameter `delta`, `delta` must be zero or positive; location parameter `mu`, by default 0. These is the meaning of the parameters in the first parameterization `pm=1` which is the default parameterization selection. In the second parameterization, `pm=2` `alpha` and `beta` take the meaning of the shape parameters (usually named) `zeta` and `rho`. In the third parameterization, `pm=3` `alpha` and `beta` take the meaning of the shape parameters (usually named) `xi` and `chi`. In the fourth parameterization, `pm=4` `alpha` and `beta` take the meaning of the shape parameters (usually named) `a.bar` and `b.bar`.

Value

returns the mode for the generalized hyperbolic distribution. A numeric value.

References

Atkinson, A.C. (1982); *The simulation of generalized inverse Gaussian and hyperbolic random variables*, SIAM J. Sci. Stat. Comput. 3, 502–515.

Barndorff-Nielsen O. (1977); *Exponentially decreasing distributions for the logarithm of particle size*, Proc. Roy. Soc. Lond., A353, 401–419.

Barndorff-Nielsen O., Blaesild, P. (1983); *Hyperbolic distributions. In Encyclopedia of Statistical Sciences*, Eds., Johnson N.L., Kotz S. and Read C.B., Vol. 3, pp. 700–707. New York: Wiley.

Raible S. (2000); *Levy Processes in Finance: Theory, Numerics and Empirical Facts*, PhD Thesis, University of Freiburg, Germany, 161 pages.

Examples

```
## ghMode -
   ghMode()
```

ghMoments *Generalized Hyperbolic Distribution Moments*

Description

Calculates moments of the generalized hyperbbolic distribution function

Usage

```
ghMean(alpha=1, beta=0, delta=1, mu=0, lambda=-1/2)
ghVar(alpha=1, beta=0, delta=1, mu=0, lambda=-1/2)
ghSkew(alpha=1, beta=0, delta=1, mu=0, lambda=-1/2)
ghKurt(alpha=1, beta=0, delta=1, mu=0, lambda=-1/2)

ghMoments(order, type = c("raw", "central", "mu"),
    alpha = 1, beta=0, delta=1, mu=0, lambda=-1/2)
```

Arguments

`alpha, beta, delta, mu, lambda`
: numeric values. `alpha` is the first shape parameter; `beta` is the second shape parameter in the range `(0, alpha)`; `delta` is the scale parameter, must be zero or positive; `mu` is the location parameter, by default 0; and `lambda` defines the sublclass, by default -1/2.

`order`
: an integer value, the order of the moment.

`type`
: a character value, `"raw"` returns the moments about zero, `"central"` returns the central moments about the mean, and `"mu"` returns the moments about the location parameter `mu`.

Value

a numerical value.

Author(s)

Diethelm Wuertz.

References

Scott, D. J., Wuertz, D. and Tran, T. T. (2008) *Moments of the Generalized Hyperbolic Distribution*. Preprint.

Examples

```
## ghMean -
   ghMean(alpha=1.1, beta=0.1, delta=0.8, mu=-0.3, lambda=1)

## ghKurt -
   ghKurt(alpha=1.1, beta=0.1, delta=0.8, mu=-0.3, lambda=1)

## ghMoments -
   ghMoments(4,
     alpha=1.1, beta=0.1, delta=0.8, mu=-0.3, lambda=1)
   ghMoments(4, "central",
     alpha=1.1, beta=0.1, delta=0.8, mu=-0.3, lambda=1)
```

---

ghRobMoments *Robust Moments for the GH*

Description

Computes the first four robust moments for the generalized hyperbolic distribution..

Usage

```
ghMED(alpha = 1, beta = 0, delta = 1, mu = 0, lambda = -1/2)
ghIQR(alpha= 1, beta = 0, delta = 1, mu = 0, lambda = -1/2)
ghSKEW(alpha = 1, beta = 0, delta = 1, mu = 0, lambda = -1/2)
ghKURT(alpha = 1, beta = 0, delta = 1, mu = 0, lambda = -1/2)
```

Arguments

`alpha, beta, delta, mu, lambda`

numeric values. `alpha` is the first shape parameter; `beta` is the second shape parameter in the range `(0, alpha)`; `delta` is the scale parameter, must be zero or positive; `mu` is the location parameter, by default 0; and `lambda` defines the sublclass, by default -1/2. These are the meanings of the parameters in the first parameterization `pm=1` which is the default parameterization. In the second parameterization, `pm=2` `alpha` and `beta` take the meaning of the shape parameters (usually named) `zeta` and `rho`. In the third parameterization, `pm=3` `alpha` and `beta` take the meaning of the shape parameters (usually named) `xi` and `chi`. In the fourth parameterization, `pm=4` `alpha` and `beta` take the meaning of the shape parameters (usually named) `a.bar` and `b.bar`.

Value

All values for the `*gh` functions are numeric vectors: `d*` returns the density, `p*` returns the distribution function, `q*` returns the quantile function, and `r*` generates random deviates.

All values have attributes named `"param"` listing the values of the distributional parameters.

Author(s)

Diethelm Wuertz.

Examples

```
## ghMED -
   # Median:
   ghMED(alpha = 1, beta = 0, delta = 1, mu = 0, lambda = -1/2)

## ghIQR -
   # Inter-quartile Range:
   ghIQR(alpha = 1, beta = 0, delta = 1, mu = 0, lambda = -1/2)

## ghSKEW -
   # Robust Skewness:
   ghSKEW(alpha = 1, beta = 0, delta = 1, mu = 0, lambda = -1/2)

## ghKURT -
   # Robust Kurtosis:
   ghKURT(alpha = 1, beta = 0, delta = 1, mu = 0, lambda = -1/2)
```

---

ghSlider *Generalized Hyperbolic Distribution Slider*

Description

Displays interactively the dependence of the generalized hyperbolic distribution on its parameters.

Usage

```
ghSlider()
```

Value

a tcl/tk based graphical user interface.

This is a nice display for educational purposes to investigate the densities and probabilities of the generalized hyperbolic distribution.

Examples

```
## ghSlider -
   # ghSlider()
```

ght *Generalized Hyperbolic Student-t*

Description

Density, distribution function, quantile function and random generation for the hyperbolic distribution.

Usage

```
dght(x, beta = 0.1, delta = 1, mu = 0, nu = 10, log = FALSE)
pght(q, beta = 0.1, delta = 1, mu = 0, nu = 10)
qght(p, beta = 0.1, delta = 1, mu = 0, nu = 10)
rght(n, beta = 0.1, delta = 1, mu = 0, nu = 10)
```

Arguments

`beta, delta, mu`	numeric values. `beta` is the skewness parameter in the range `(0, alpha)`; `delta` is the scale parameter, must be zero or positive; `mu` is the location parameter, by default 0. These are the parameters in the first parameterization.
`nu`	a numeric value, the number of degrees of freedom. Note, `alpha` takes the limit of `abs(beta)`, and `lambda=-nu/2`.
`x, q`	a numeric vector of quantiles.
`p`	a numeric vector of probabilities.
`n`	number of observations.
`log`	a logical, if TRUE, probabilities `p` are given as `log(p)`.

Value

All values for the `*ght` functions are numeric vectors: `d*` returns the density, `p*` returns the distribution function, `q*` returns the quantile function, and `r*` generates random deviates.

All values have attributes named `"param"` listing the values of the distributional parameters.

References

Atkinson, A.C. (1982); *The simulation of generalized inverse Gaussian and hyperbolic random variables*, SIAM J. Sci. Stat. Comput. 3, 502–515.

Barndorff-Nielsen O. (1977); *Exponentially decreasing distributions for the logarithm of particle size*, Proc. Roy. Soc. Lond., A353, 401–419.

Barndorff-Nielsen O., Blaesild, P. (1983); *Hyperbolic distributions. In Encyclopedia of Statistical Sciences*, Eds., Johnson N.L., Kotz S. and Read C.B., Vol. 3, pp. 700–707. New York: Wiley.

Raible S. (2000); *Levy Processes in Finance: Theory, Numerics and Empirical Facts*, PhD Thesis, University of Freiburg, Germany, 161 pages.

Examples

```
## ght -
   #
```

---

ghtFit *GHT Distribution Fit*

Description

Estimates the distributional parameters for a generalized hyperbolic Student-t distribution.

Usage

```
ghtFit(x, beta = 0.1, delta = 1, mu = 0, nu = 10,
    scale = TRUE, doplot = TRUE, span = "auto", trace = TRUE,
    title = NULL, description = NULL, ...)
```

Arguments

beta, delta, mu	numeric values. beta is the skewness parameter in the range (0, alpha); delta is the scale parameter, must be zero or positive; mu is the location parameter, by default 0. These are the parameters in the first parameterization.
nu	defines the number of degrees of freedom. Note, alpha takes the limit of abs(beta), and lambda=-nu/2.
x	a numeric vector.
scale	a logical flag, by default TRUE. Should the time series be scaled by its standard deviation to achieve a more stable optimization?
doplot	a logical flag. Should a plot be displayed?
span	x-coordinates for the plot, by default 100 values automatically selected and ranging between the 0.001, and 0.999 quantiles. Alternatively, you can specify the range by an expression like span=seq(min, max, times = n), where, min and max are the left and right endpoints of the range, and n gives the number of the intermediate points.
trace	a logical flag. Should the parameter estimation process be traced?
title	a character string which allows for a project title.
description	a character string which allows for a brief description.
...	parameters to be parsed.

Details

The function nlm is used to minimize the "negative" maximum log-likelihood function. nlm carries out a minimization using a Newton-type algorithm.

Value

returns a list with the following components:

estimate	the point at which the maximum value of the log liklihood function is obtained.
minimum	the value of the estimated maximum, i.e. the value of the log liklihood function.
code	an integer indicating why the optimization process terminated. 1: relative gradient is close to zero, current iterate is probably solution; 2: successive iterates within tolerance, current iterate is probably solution; 3: last global step failed to locate a point lower than estimate. Either estimate is an approximate local minimum of the function or steptol is too small; 4: iteration limit exceeded; 5: maximum step size stepmax exceeded five consecutive times. Either the function is unbounded below, becomes asymptotic to a finite value from above in some direction or stepmax is too small.
gradient	the gradient at the estimated maximum.
steps	number of function calls.

Examples

```
## ghtFit -
   # Simulate Random Variates:
   set.seed(1953)

## ghtFit -
   # Fit Parameters:
```

---

ghtMode *Generalized Hyperbolic Student-t Mode*

Description

Computes the mode of the generalized hyperbolic Student-t distribution.

Usage

```
ghtMode(beta = 0.1, delta = 1, mu = 0, nu = 10)
```

Arguments

beta, delta, mu	numeric values. beta is the skewness parameter in the range (0, alpha); delta is the scale parameter, must be zero or positive; mu is the location parameter, by default 0. These are the parameters in the first parameterization.
nu	a numeric value, the number of degrees of freedom. Note, alpha takes the limit of abs(beta), and lambda=-nu/2.

Value

returns the mode for the generalized hyperbolic Student-t distribution. A numeric value.

References

Atkinson, A.C. (1982); *The simulation of generalized inverse Gaussian and hyperbolic random variables*, SIAM J. Sci. Stat. Comput. 3, 502–515.

Barndorff-Nielsen O. (1977); *Exponentially decreasing distributions for the logarithm of particle size*, Proc. Roy. Soc. Lond., A353, 401–419.

Barndorff-Nielsen O., Blaesild, P. (1983); *Hyperbolic distributions. In Encyclopedia of Statistical Sciences*, Eds., Johnson N.L., Kotz S. and Read C.B., Vol. 3, pp. 700–707. New York: Wiley.

Raible S. (2000); *Levy Processes in Finance: Theory, Numerics and Empirical Facts*, PhD Thesis, University of Freiburg, Germany, 161 pages.

Examples

```
## ghtMode -
   ghtMode()
```

`ghtMoments` *Generalized Hyperbolic Student-t Moments*

Description

Calculates moments of the generalized hyperbbolic Student-t distribution function.

Usage

```
ghtMean(beta=0.1, delta=1, mu=0, nu=10)
ghtVar(beta=0.1, delta=1, mu=0, nu=10)
ghtSkew(beta=0.1, delta=1, mu=0, nu=10)
ghtKurt(beta=0.1, delta=1, mu=0, nu=10)

ghtMoments(order, type = c("raw", "central", "mu"),
    beta=0.1, delta=1, mu=0, nu=10)
```

Arguments

`beta, delta, mu`	numeric values. `beta` is the skewness parameter in the range `(0, alpha)`; `delta` is the scale parameter, must be zero or positive; `mu` is the location parameter, by default 0. These are the parameters in the first parameterization.
`nu`	a numeric value, the number of degrees of freedom. Note, `alpha` takes the limit of `abs(beta)`, and `lambda=-nu/2`.
`order`	an integer value, the order of the moment.
`type`	a character value, `"raw"` returns the moments about zero, `"central"` returns the central moments about the mean, and `"mu"` returns the moments about the location parameter `mu`.

Value

a numerical value.

Author(s)

Diethelm Wuertz.

References

Scott, D.J., Wuertz, D. and Tran, T.T. (2008) *Moments of the Generalized Hyperbolic Distribution*. Preprint.

Examples

```
## ghtMean -
   ghtMean(beta=0.2, delta=1.2, mu=-0.5, nu=4)

## ghtKurt -
   ghtKurt(beta=0.2, delta=1.2, mu=-0.5, nu=4)

## ghtMoments -
   ghtMoments(4,
     beta=0.2, delta=1.2, mu=-0.5, nu=4)
   ghtMoments(4, "central",
     beta=0.2, delta=1.2, mu=-0.5, nu=4)
```

---

ghtRobMoments *Robust Moments for the GHT*

Description

Computes the first four robust moments for the generalized hyperbolic Student-t.

Usage

```
ghtMED(beta = 0.1, delta = 1, mu = 0, nu = 10)
ghtIQR(beta = 0.1, delta = 1, mu = 0, nu = 10)
ghtSKEW(beta = 0.1, delta = 1, mu = 0, nu = 10)
ghtKURT(beta = 0.1, delta = 1, mu = 0, nu = 10)
```

Arguments

`beta, delta, mu`	numeric values. `beta` is the skewness parameter in the range `(0, alpha)`; `delta` is the scale parameter, must be zero or positive; `mu` is the location parameter, by default 0. These are the parameters in the first parameterization.
`nu`	a numeric value, the number of degrees of freedom. Note, `alpha` takes the limit of `abs(beta)`, and `lambda=-nu/2`.

Value

All values for the *ght functions are numeric vectors: d* returns the density, p* returns the distribution function, q* returns the quantile function, and r* generates random deviates.

All values have attributes named "param" listing the values of the distributional parameters.

Author(s)

Diethelm Wuertz.

Examples

```
## ghtMED -
   # Median:
   ghtMED(beta = 0.1, delta = 1, mu = 0, nu = 10)

## ghtIQR -
   # Inter-quartile Range:
   ghtIQR(beta = 0.1, delta = 1, mu = 0, nu = 10)

## ghtSKEW -
   # Robust Skewness:
   ghtSKEW(beta = 0.1, delta = 1, mu = 0, nu = 10)

## ghtKURT -
   # Robust Kurtosis:
   ghtKURT(beta = 0.1, delta = 1, mu = 0, nu = 10)
```

---

gld *Generalized Lambda Distribution*

Description

Density, distribution function, quantile function and random generation for the generalized lambda distribution.

Usage

```
dgld(x, lambda1 = 0, lambda2 = -1, lambda3 = -1/8, lambda4 = -1/8, log = FALSE)
pgld(q, lambda1 = 0, lambda2 = -1, lambda3 = -1/8, lambda4 = -1/8)
qgld(p, lambda1 = 0, lambda2 = -1, lambda3 = -1/8, lambda4 = -1/8)
rgld(n, lambda1 = 0, lambda2 = -1, lambda3 = -1/8, lambda4 = -1/8)
```

Arguments

lambda1, lambda2, lambda3, lambda4	are numeric values where lambda1 is the location parameter, lambda2 is the location parameter, lambda3 is the first shape parameter, and lambda4 is the second shape parameter.
n	number of observations.
p	a numeric vector of probabilities.
x, q	a numeric vector of quantiles.
log	a logical, if TRUE, probabilities p are given as log(p).

Value

All values for the *gld functions are numeric vectors: d* returns the density, p* returns the distribution function, q* returns the quantile function, and r* generates random deviates.

All values have attributes named "param" listing the values of the distributional parameters.

Author(s)

Chong Gu for code implemented from R's contributed package gld.

Examples

```
## rgld -
   set.seed(1953)
   r = rgld(500,
     lambda1=0, lambda2=-1, lambda3=-1/8, lambda4=-1/8)
   plot(r, type = "l", col = "steelblue",
     main = "gld: lambda1=0 lambda2=-1 lambda3/4=-1/8")

## dgld -
   # Plot empirical density and compare with true density:
   hist(r, n = 25, probability = TRUE, border = "white",
     col = "steelblue")
   x = seq(-5, 5, 0.25)
   lines(x, dgld(x,
     lambda1=0, lambda2=-1, lambda3=-1/8, lambda4=-1/8))

## pgld -
   # Plot df and compare with true df:
   plot(sort(r), ((1:500)-0.5)/500, main = "Probability",
     col = "steelblue")
   lines(x, pgld(x,
     lambda1=0, lambda2=-1, lambda3=-1/8, lambda4=-1/8))

## qgld -
   # Compute Quantiles:
   qgld(pgld(seq(-5, 5, 1),
     lambda1=0, lambda2=-1, lambda3=-1/8, lambda4=-1/8),
     lambda1=0, lambda2=-1, lambda3=-1/8, lambda4=-1/8)
```

gldFit *GH Distribution Fit*

Description

Estimates the distrinbutional parameters for a generalized lambda distribution.

Usage

```
gldFit(x, lambda1 = 0, lambda2 = -1, lambda3 = -1/8, lambda4 = -1/8,
    method = c("mle", "mps", "gof", "hist", "rob"),
    scale = NA, doplot = TRUE, add = FALSE, span = "auto", trace = TRUE,
    title = NULL, description = NULL, ...)
```

Arguments

x	a numeric vector.
lambda1, lambda2, lambda3, lambda4	are numeric values where lambda1 is the location parameter, lambda2 is the location parameter, lambda3 is the first shape parameter, and lambda4 is the second shape parameter.
method	a character string, the estimation approach to fit the distributional parameters, see details.
scale	not used.
doplot	a logical flag. Should a plot be displayed?
add	a logical flag. Should a new fit added to an existing plot?
span	x-coordinates for the plot, by default 100 values automatically selected and ranging between the 0.001, and 0.999 quantiles. Alternatively, you can specify the range by an expression like span=seq(min, max, times = n), where, min and max are the left and rigldt endpoints of the range, and n gives the number of the intermediate points.
trace	a logical flag. Should the parameter estimation process be traced?
title	a character string which allows for a project title.
description	a character string which allows for a brief description.
...	parameters to be parsed.

Details

The function nlminb is used to minimize the objective function. The following approaches have been implemented:

"mle", maximimum log likelihoo estimation.

"mps", maximum product spacing estimation.

"gof", goodness of fit approaches, type="ad" Anderson-Darling, type="cvm" Cramer-vonMise, type="ks" Kolmogorov-Smirnov.

"hist", histogram binning approaches, "fd" Freedman-Diaconis binning, "scott", Scott histogram binning, "sturges", Sturges histogram binning.

"rob", robust moment matching.

Value

returns a list with the following components:

estimate	the point at which the maximum value of the log liklihood function is obtained.
minimum	the value of the estimated maximum, i.e. the value of the log liklihood function.
code	an integer indicating why the optimization process terminated. 1: relative gradient is close to zero, current iterate is probably solution; 2: successive iterates within tolerance, current iterate is probably solution; 3: last global step failed to locate a point lower than estimate. Either estimate is an approximate local minimum of the function or steptol is too small; 4: iteration limit exceeded; 5: maximum step size stepmax exceeded five consecutive times. Either the function is unbounded below, becomes asymptotic to a finite value from above in some direction or stepmax is too small.
gradient	the gradient at the estimated maximum.
steps	number of function calls.

Examples

```
## gldFit -
   # Simulate Random Variates:
   set.seed(1953)
   s = rgld(n = 1000, lambda1=0, lambda2=-1, lambda3=-1/8, lambda4=-1/8)

## gldFit -
   # Fit Parameters:
   gldFit(s, lambda1=0, lambda2=-1, lambda3=-1/8, lambda4=-1/8,
     doplot = TRUE, trace = TRUE)
```

---

gldMode *Generalized Lambda Distribution Mode*

Description

Computes the mode of the generalized lambda distribution.

Usage

```
gldMode(lambda1 = 0, lambda2 = -1, lambda3 = -1/8, lambda4 = -1/8)
```

Arguments

`lambda1, lambda2, lambda3, lambda4`
: are numeric values where `lambda1` is the location parameter, `lambda2` is the location parameter, `lambda3` is the first shape parameter, and `lambda4` is the second shape parameter.

Author(s)

Implemented by Diethelm Wuertz

---

gldRobMoments *Robust Moments for the GLD*

Description

Computes the first four robust moments for the Generalized Lambda Distribution.

Usage

```
gldMED(lambda1 = 0, lambda2 = -1, lambda3 = -1/8, lambda4 = -1/8)
gldIQR(lambda1 = 0, lambda2 = -1, lambda3 = -1/8, lambda4 = -1/8)
gldSKEW(lambda1 = 0, lambda2 = -1, lambda3 = -1/8, lambda4 = -1/8)
gldKURT(lambda1 = 0, lambda2 = -1, lambda3 = -1/8, lambda4 = -1/8)
```

Arguments

`lambda1, lambda2, lambda3, lambda4`
: are numeric values where `lambda1` is the location parameter, `lambda2` is the location parameter, `lambda3` is the first shape parameter, and `lambda4` is the second shape parameter.

Value

All values for the `*gld` functions are numeric vectors: `d*` returns the density, `p*` returns the distribution function, `q*` returns the quantile function, and `r*` generates random deviates.

All values have attributes named `"param"` listing the values of the distributional parameters.

Author(s)

Diethelm Wuertz.

Examples

```
## gldMED -
   # Median:
   gldMED(lambda1 = 0, lambda2 = -1, lambda3 = -1/8, lambda4 = -1/8)

## gldIQR -
   # Inter-quartile Range:
   gldIQR(lambda1 = 0, lambda2 = -1, lambda3 = -1/8, lambda4 = -1/8)

## gldSKEW -
   # Robust Skewness:
   gldSKEW(lambda1 = 0, lambda2 = -1, lambda3 = -1/8, lambda4 = -1/8)

## gldKURT -
   # Robust Kurtosis:
   gldKURT(lambda1 = 0, lambda2 = -1, lambda3 = -1/8, lambda4 = -1/8)
```

---

gridVector *Grid Vector Coordinates*

Description

Creates from two vectors rectangular grid coordinates..

Usage

```
gridVector(x, y = NULL)
```

Arguments

x, y	two numeric vectors of length m and n which span the rectangular grid of size m times n. If y takes the default value, NULL, then y=x.

Value

returns a list with two entries named $X and $Y, giving the coordinates which span the bivariate grid.

See Also

expand.grid.

Examples

```
## gridVector -
   gridVector((0:10)/10)
   gridVector((0:10)/10, (0:10)/10)
```

`Heaviside` *Heaviside and Related Functions*

Description

Functions which compute the Heaviside and related functions. These include the sign function, the delta function, the boxcar function, and the ramp function.

The functions are:

`Heaviside`	Computes Heaviside unit step function,
`Sign`	Just another signum function,
`Delta`	Computes delta function,
`Boxcar`	Computes boxcar function,
`Ramp`	Computes ramp function.

Usage

```
Heaviside(x, a = 0)
Sign(x, a = 0)
Delta(x, a = 0)
Boxcar(x, a = 0.5)
Ramp(x, a = 0)
```

Arguments

`a`	a numeric value, the location of the break.
`x`	a numeric vector.

Details

The Heaviside step function `Heaviside` is `1` for `x>a`, `1/2` for `x=a`, and `0` for `x<a`.

The Sign function `Sign` is `1` for `x>a`, `0` for `x=a`, and `-1` for `x<a`.

The delta function `Delta` is defined as: `Delta(x)` = `d/dx` `H(x-a)`.

The boxcar function `Boxcar` is defined as: `Boxcar(x)` = `H(x+a)` - `H(x-a)`.

The ramp function is defined as: `Ramp(x)= (x-a)*H(x-a)`.

Value

returns the function values of the selected function.

Note

The Heaviside function is used in the implementation of the skew Normal, Student-t, and Generalized Error distributions, distributions functions which play an important role in modelling GARCH processes.

References

Weisstein W. (2004); *http://mathworld.wolfram.com/HeavisideStepFunction.html*, Mathworld.

See Also

`GarchDistribution`, `GarchDistributionFits`.

Examples

```
## Heaviside -
   x = sort(round(c(-1, -0.5, 0, 0.5, 1, 5*rnorm(5)), 2))
   h = Heaviside(x)

## Sign -
   s = Sign(x)

## Delta -
   d = Delta(x)

## Boxcar -
   Pi = Boxcar(x)

## Ramp -
   r = Ramp(x)
   cbind(x = x, Step = h, Signum = s, Delta = d, Pi = Pi, R = r)
```

---

hilbert *Hilbert Matrix*

Description

Creates a Hilbert matrix.

Usage

```
hilbert(n)
```

Arguments

`n`	an integer value, the dimension of the square matrix.

Details

In linear algebra, a Hilbert matrix is a matrix with the unit fraction elements.

The Hilbert matrices are canonical examples of ill-conditioned matrices, making them notoriously difficult to use in numerical computation. For example, the 2-norm condition number of a 5x5 Hilbert matrix above is about 4.8e5.

The Hilbert matrix is symmetric and positive definite.

Value

`hilbert` generates a Hilbert matrix of order `n`.

References

Hilbert D., *Collected papers*, vol. II, article 21.

Beckermann B, (2000); *The condition number of real Vandermonde, Krylov and positive definite Hankel matrices*, Numerische Mathematik 85, 553–577, 2000.

Choi, M.D., (1983); *Tricks or Treats with the Hilbert Matrix*, American Mathematical Monthly 90, 301–312, 1983.

Todd, J., (1954); *The Condition Number of the Finite Segment of the Hilbert Matrix*, National Bureau of Standards, Applied Mathematics Series 39, 109–116.

Wilf, H.S., (1970); *Finite Sections of Some Classical Inequalities*, Heidelberg, Springer.

Examples

```
## Create a Hilbert Matrix:
   H = hilbert(5)
   H
```

HistogramPlot *Histogram and Density Plots*

Description

Returns a histogram, a density, or a logarithmic density plot.

List of Functions:

`histPlot`	Returns a tailored histogram plot,
`densityPlot`	Returns a tailored kernel density estimate plot,
`logDensityPlot`	Returns a tailored log kernel density estimate plot.

Usage

```
histPlot(x, labels = TRUE, col = "steelblue", fit = TRUE,
```

```
    title = TRUE, grid = TRUE, rug = TRUE, skip = FALSE, ...)
densityPlot(x, labels = TRUE, col = "steelblue", fit = TRUE, hist = TRUE,
    title = TRUE, grid = TRUE, rug = TRUE, skip = FALSE, ...)
logDensityPlot(x, labels = TRUE, col = "steelblue", robust = TRUE,
    title = TRUE, grid = TRUE, rug = TRUE, skip = FALSE, ...)
```

Arguments

col	the color for the series. In the univariate case use just a color name like the default, col="steelblue", in the multivariate case we recommend to select the colors from a color palette, e.g. col=heat.colors(ncol(x)).
fit	a logical flag, should a fit added to the Plot?
grid	a logical flag, should a grid be added to the plot? By default TRUE. To plot a horizontal lines only use grid="h" and for vertical lines use grid="h", respectively.
hist	a logical flag, by default TRUE. Should a histogram to be underlaid to the plot?
labels	a logical flag, should the plot be returned with default labels and decorated in an automated way? By default TRUE.
rug	a logical flag, by default TRUE. Should a rug representation of the data added to the plot?
skip	a logical flag, should zeros be skipped in the return Series?
robust	a logical flag, by default TRUE. Should a robust fit added to the plot?
title	a logical flag, by default TRUE. Should a default title added to the plot?
x	an object of class "timeSeries" or any other object which can be transformed by the function as.timeSeries into an object of class timeSeries. The latter case, other then timeSeries objects, is more or less untested.
...	optional arguments to be passed.

Value

displays a time series plot.

Examples

```
## data -
   data(LPP2005REC, package = "timeSeries")
   SPI <- LPP2005REC[, "SPI"]
   plot(SPI, type = "l", col = "steelblue", main = "SP500")
   abline(h = 0, col = "grey")

## histPlot -
   histPlot(SPI)

## densityPlot -
   densityPlot(SPI)
```

hyp *Hyperbolic Distribution*

Description

Density, distribution function, quantile function and random generation for the hyperbolic distribution.

Usage

```
dhyp(x, alpha = 1, beta = 0, delta = 1, mu = 0,
    pm = c("1", "2", "3", "4"), log = FALSE)
phyp(q, alpha = 1, beta = 0, delta = 1, mu = 0,
    pm = c("1", "2", "3", "4"), ...)
qhyp(p, alpha = 1, beta = 0, delta = 1, mu = 0,
    pm = c("1", "2", "3", "4"), ...)
rhyp(n, alpha = 1, beta = 0, delta = 1, mu = 0,
    pm = c("1", "2", "3", "4"))
```

Arguments

alpha, beta, delta, mu	shape parameter alpha; skewness parameter beta, abs(beta) is in the range (0, alpha); scale parameter delta, delta must be zero or positive; location parameter mu, by default 0. These is the meaning of the parameters in the first parameterization pm=1 which is the default parameterization selection. In the second parameterization, pm=2 alpha and beta take the meaning of the shape parameters (usually named) zeta and rho. In the third parameterization, pm=3 alpha and beta take the meaning of the shape parameters (usually named) xi and chi. In the fourth parameterization, pm=4 alpha and beta take the meaning of the shape parameters (usually named) a.bar and b.bar.
n	number of observations.
p	a numeric vector of probabilities.
pm	an integer value between 1 and 4 for the selection of the parameterization. The default takes the first parameterization.
x, q	a numeric vector of quantiles.
log	a logical, if TRUE, probabilities p are given as log(p).
...	arguments to be passed to the function integrate.

Details

The generator rhyp is based on the HYP algorithm given by Atkinson (1982).

Value

All values for the *hyp functions are numeric vectors: d* returns the density, p* returns the distribution function, q* returns the quantile function, and r* generates random deviates.

All values have attributes named "param" listing the values of the distributional parameters.

Author(s)

David Scott for code implemented from R's contributed package HyperbolicDist.

References

Atkinson, A.C. (1982); *The simulation of generalized inverse Gaussian and hyperbolic random variables*, SIAM J. Sci. Stat. Comput. 3, 502–515.

Barndorff-Nielsen O. (1977); *Exponentially decreasing distributions for the logarithm of particle size*, Proc. Roy. Soc. Lond., A353, 401–419.

Barndorff-Nielsen O., Blaesild, P. (1983); *Hyperbolic distributions. In Encyclopedia of Statistical Sciences*, Eds., Johnson N.L., Kotz S. and Read C.B., Vol. 3, pp. 700–707. New York: Wiley.

Raible S. (2000); *Levy Processes in Finance: Theory, Numerics and Empirical Facts*, PhD Thesis, University of Freiburg, Germany, 161 pages.

Examples

```
## hyp -
   set.seed(1953)
   r = rhyp(5000, alpha = 1, beta = 0.3, delta = 1)
   plot(r, type = "l", col = "steelblue",
     main = "hyp: alpha=1 beta=0.3 delta=1")

## hyp -
   # Plot empirical density and compare with true density:
   hist(r, n = 25, probability = TRUE, border = "white", col = "steelblue")
   x = seq(-5, 5, 0.25)
   lines(x, dhyp(x, alpha = 1, beta = 0.3, delta = 1))

## hyp -
   # Plot df and compare with true df:
   plot(sort(r), (1:5000/5000), main = "Probability", col = "steelblue")
   lines(x, phyp(x, alpha = 1, beta = 0.3, delta = 1))

## hyp -
   # Compute Quantiles:
   qhyp(phyp(seq(-5, 5, 1), alpha = 1, beta = 0.3, delta = 1),
     alpha = 1, beta = 0.3, delta = 1)
```

hypFit *Fit of a Hyperbolic Distribution*

Description

Estimates the parameters of a hyperbolic distribution.

Usage

```
hypFit(x, alpha = 1, beta = 0, delta = 1, mu = 0,
    scale = TRUE, doplot = TRUE, span = "auto", trace = TRUE,
    title = NULL, description = NULL, ...)
```

Arguments

alpha, beta, delta, mu	alpha is a shape parameter by default 1, beta is a skewness parameter by default 0, note abs(beta) is in the range (0, alpha), delta is a scale parameter by default 1, note, delta must be zero or positive, and mu is a location parameter, by default 0. These is the meaning of the parameters in the first parameterization pm=1 which is the default parameterization selection. In the second parameterization, pm=2 alpha and beta take the meaning of the shape parameters (usually named) zeta and rho. In the third parameterization, pm=3 alpha and beta take the meaning of the shape parameters (usually named) xi and chi. In the fourth parameterization, pm=4 alpha and beta take the meaning of the shape parameters (usually named) a.bar and b.bar.
description	a character string which allows for a brief description.
doplot	a logical flag. Should a plot be displayed?
scale	a logical flag, by default TRUE. Should the time series be scaled by its standard deviation to achieve a more stable optimization?
span	x-coordinates for the plot, by default 100 values automatically selected and ranging between the 0.001, and 0.999 quantiles. Alternatively, you can specify the range by an expression like span=seq(min, max, times = n), where, min and max are the left and right endpoints of the range, and n gives the number of the intermediate points.
title	a character string which allows for a project title.
trace	a logical flag. Should the parameter estimation process be traced?
x	a numeric vector.
...	parameters to be parsed.

Details

The function nlm is used to minimize the "negative" maximum log-likelihood function. nlm carries out a minimization using a Newton-type algorithm.

Value

The functions `tFit`, `hypFit` and `nigFit` return a list with the following components:

`estimate`	the point at which the maximum value of the log liklihood function is obtained.
`minimum`	the value of the estimated maximum, i.e. the value of the log liklihood function.
`code`	an integer indicating why the optimization process terminated. 1: relative gradient is close to zero, current iterate is probably solution; 2: successive iterates within tolerance, current iterate is probably solution; 3: last global step failed to locate a point lower than `estimate`. Either `estimate` is an approximate local minimum of the function or `steptol` is too small; 4: iteration limit exceeded; 5: maximum step size `stepmax` exceeded five consecutive times. Either the function is unbounded below, becomes asymptotic to a finite value from above in some direction or `stepmax` is too small.
`gradient`	the gradient at the estimated maximum.
`steps`	number of function calls.

Examples

```
## rhyp -
   # Simulate Random Variates:
   set.seed(1953)
   s = rhyp(n = 1000, alpha = 1.5, beta = 0.3, delta = 0.5, mu = -1.0)

## hypFit -
   # Fit Parameters:
   hypFit(s, alpha = 1, beta = 0, delta = 1, mu = mean(s), doplot = TRUE)
```

`hypMode` *Hyperbolic Mode*

Description

Computes the mode of the hyperbolic function.

Usage

```
hypMode(alpha = 1, beta = 0, delta = 1, mu = 0, pm = c(1, 2, 3, 4))
```

Arguments

`alpha, beta, delta, mu`

shape parameter `alpha`; skewness parameter `beta`, `abs(beta)` is in the range (0, alpha); scale parameter `delta`, `delta` must be zero or positive; location parameter `mu`, by default 0. These is the meaning of the parameters in the first parameterization `pm=1` which is the default parameterization selection. In the

second parameterization, pm=2 alpha and beta take the meaning of the shape parameters (usually named) zeta and rho. In the third parameterization, pm=3 alpha and beta take the meaning of the shape parameters (usually named) xi and chi. In the fourth parameterization, pm=4 alpha and beta take the meaning of the shape parameters (usually named) a.bar and b.bar.

pm — an integer value between 1 and 4 for the selection of the parameterization. The default takes the first parameterization.

Value

returns the mode in the appropriate parameterization for the hyperbolic distribution. A numeric value.

Author(s)

David Scott for code implemented from R's contributed package HyperbolicDist.

References

Atkinson, A.C. (1982); *The simulation of generalized inverse Gaussian and hyperbolic random variables*, SIAM J. Sci. Stat. Comput. 3, 502–515.

Barndorff-Nielsen O. (1977); *Exponentially decreasing distributions for the logarithm of particle size*, Proc. Roy. Soc. Lond., A353, 401–419.

Barndorff-Nielsen O., Blaesild, P. (1983); *Hyperbolic distributions. In Encyclopedia of Statistical Sciences*, Eds., Johnson N.L., Kotz S. and Read C.B., Vol. 3, pp. 700–707. New York: Wiley.

Raible S. (2000); *Levy Processes in Finance: Theory, Numerics and Empirical Facts*, PhD Thesis, University of Freiburg, Germany, 161 pages.

Examples

```
## hypMode -
   hypMode()
```

---

hypMoments *Hyperbolic Distribution Moments*

Description

Calculates moments of the hyperbbolic distribution function

Usage

```
hypMean(alpha=1, beta=0, delta=1, mu=0)
hypVar(alpha=1, beta=0, delta=1, mu=0)
hypSkew(alpha=1, beta=0, delta=1, mu=0)
hypKurt(alpha=1, beta=0, delta=1, mu=0)

hypMoments(order, type = c("raw", "central", "mu"),
    alpha=1, beta=0, delta=1, mu=0)
```

Arguments

`alpha, beta, delta, mu`	numeric values. `alpha` is the first shape parameter; `beta` is the second shape parameter in the range `(0, alpha)`; `delta` is the scale parameter, must be zero or positive; `mu` is the location parameter, by default 0.
`order`	an integer value, the order of the moment.
`type`	a character value, `"raw"` returns the moments about zero, `"central"` returns the central moments about the mean, and `"mu"` returns the moments about the location parameter `mu`.

Value

a numerical value.

Author(s)

Diethelm Wuertz.

References

Scott, D. J., Wuertz, D. and Tran, T. T. (2008) *Moments of the Generalized Hyperbolic Distribution*. Preprint.

Examples

```
## hypMean -
   hypMean(alpha=1.1, beta=0.1, delta=0.8, mu=-0.3)

## ghKurt -
   hypKurt(alpha=1.1, beta=0.1, delta=0.8, mu=-0.3)

## hypMoments -
   hypMoments(4, alpha=1.1, beta=0.1, delta=0.8, mu=-0.3)
   hypMoments(4, "central", alpha=1.1, beta=0.1, delta=0.8, mu=-0.3)
```

hypRobMoments *Robust Moments for the HYP*

Description

Computes the first four robust moments for the hyperbolic distribution.

Usage

```
hypMED(alpha = 1, beta = 0, delta = 1, mu = 0)
hypIQR(alpha = 1, beta = 0, delta = 1, mu = 0)
hypSKEW(alpha = 1, beta = 0, delta = 1, mu = 0)
hypKURT(alpha = 1, beta = 0, delta = 1, mu = 0)
```

Arguments

`alpha, beta, delta, mu`

shape parameter `alpha`; skewness parameter `beta`, `abs(beta)` is in the range (0, alpha); scale parameter `delta`, `delta` must be zero or positive; location parameter `mu`, by default 0. These is the meaning of the parameters in the first parameterization `pm=1` which is the default parameterization selection. In the second parameterization, `pm=2` `alpha` and `beta` take the meaning of the shape parameters (usually named) `zeta` and `rho`. In the third parameterization, `pm=3` `alpha` and `beta` take the meaning of the shape parameters (usually named) `xi` and `chi`. In the fourth parameterization, `pm=4` `alpha` and `beta` take the meaning of the shape parameters (usually named) `a.bar` and `b.bar`.

Value

All values for the `*hyp` functions are numeric vectors: `d*` returns the density, `p*` returns the distribution function, `q*` returns the quantile function, and `r*` generates random deviates.

All values have attributes named `"param"` listing the values of the distributional parameters.

Author(s)

Diethelm Wuertz.

Examples

```
## hypMED -
   # Median:
   hypMED(alpha = 1, beta = 0, delta = 1, mu = 0)

## hypIQR -
   # Inter-quartile Range:
   hypIQR(alpha = 1, beta = 0, delta = 1, mu = 0)

## hypSKEW -
```

```
   # Robust Skewness:
   hypSKEW(alpha = 1, beta = 0, delta = 1, mu = 0)

## hypKURT -
   # Robust Kurtosis:
   hypKURT(alpha = 1, beta = 0, delta = 1, mu = 0)
```

---

hypSlider *Hyperbolic Distribution Slider*

Description

Displays interactively the dependence of the hyperbolic distribution on its parameters.

Usage

```
hypSlider()
```

Value

a tcl/tk based graphical user interface.

This is a nice display for educational purposes to investigate the densities and probabilities of the hyperbolic distribution.

Examples

```
## hypSlider -
   #
```

Ids *Set and Retrieve Column/Row Names*

Description

Sets and retrieves column and row names. The functions are for compatibility with SPlus.

Usage

```
colIds(x, ...)
rowIds(x, ...)
```

Arguments

x	a numeric matrix.
...	arguments to be passed.

Details

Usualli in R the functions `colnames`, and `rownames` are used to retrieve and set the names of matrices. The functions `rowIds` and `colIds`, are S-Plus like synonyms.

Examples

```
## pascal -
   # Create Pascal Matrix:
   P = pascal(3)
   P

## rownames -
   rownames(P) <- letters[1:3]
   P

## colIds<- -
   colIds(P) <- as.character(1:3)
   P
```

---

interactivePlot *Interactive Plot Utility*

Description

Plots with emphasis on interactive plots.

Usage

```
interactivePlot(x, choices = paste("Plot", 1:9),
    plotFUN = paste("plot.", 1:9, sep = ""), which = "all", ...)
```

Arguments

`choices`	a vector of character strings for the choice menu. By Default `"Plot 1"` ... `"Plot 9"` allowing for 9 plots at maximum.
`plotFUN`	a vector of character strings naming the plot functions. By Default `"plot.1"` ... `"plot.9"` allowing for 9 plots at maximum.
`which`	plot selection, which graph should be displayed? If `"which"` is a character string named "ask" the user is interactively asked which to plot, if a logical vector of length `N`, those plots which are set `TRUE` are displayed, if a character string named `"all"` all plots are displayed.
`x`	an object to be plotted.
`...`	additional arguments passed to the FUN or plot function.

Examples

```
## Test Plot Function:
   testPlot = function(x, which = "all", ...) {
     # Plot Function and Addons:
     plot.1 <<- function(x, ...) plot(x, ...)
     plot.2 <<- function(x, ...) acf(x, ...)
     plot.3 <<- function(x, ...) hist(x, ...)
     plot.4 <<- function(x, ...) qqnorm(x, ...)
     # Plot:
     interactivePlot(x,
       choices = c("Series Plot", "ACF", "Histogram", "QQ Plot"),
       plotFUN = c("plot.1", "plot.2", "plot.3", "plot.4"),
       which = which, ...)
     # Return Value:
     invisible()
   }
   # Plot:
   par(mfrow = c(2, 2), cex = 0.7)
   testPlot(rnorm(500))

   # Try:
   # par(mfrow = c(1,1))
   # testPlot(rnorm(500), which = "ask")
```

`inv` *The Inverse of a Matrix*

Description

Returns the inverse of a matrix.

Usage

```
inv(x)
```

Arguments

`x`	a numeric matrix.

Value

returns the inverse matrix.

Note

The function `inv` is a synonyme to the function `solve`.

References

Golub, van Loan, (1996); *Matrix Computations*, 3rd edition. Johns Hopkins University Press.

Examples

```
## Create Pascal Matrix:
   P = pascal(5)
   P

## Compute the Inverse Matrix:
   inv(P)

## Check:
   inv(P) %*% P

## Alternatives:
   chol2inv(chol(P))
   solve(P)
```

---

krigeInterp *Bivariate Krige Interpolation*

Description

Bivariate Krige Interpolation.

Usage

```
krigeInterp(x, y = NULL, z = NULL, gridPoints = 21,
    xo = seq(min(x), max(x), length = gridPoints),
    yo = seq(min(y), max(y), length = gridPoints),
    extrap = FALSE, polDegree = 6)
```

Arguments

x, y, z	the arguments x and y are two numeric vectors of grid pounts, and z is a numeric matrix or any other rectangular object which can be transformed by the function as.matrix into a matrix object.
gridPoints	an integer value specifying the number of grid points in x and y direction.
xo, yo	two numeric vectors of data points spanning the grid.
extrap	a logical, if TRUE then the data points are extrapolated.
polDegree	the polynomial krige degree, an integer ranging between 1 and 6.

Value

krigeInterp returns a list with at least three entries, x, y and z. Note, that the returned values, can be directly used by the persp and contour 3D plotting methods.

Note

The function krigeInterp() requires the R package **spatial**.

See Also

akimaInterp, linearInterp.

Examples

```
## The akima library is not auto-installed because of a different licence.
## krigeInterp -  Kriging:
set.seed(1953)
x = runif(999) - 0.5
y = runif(999) - 0.5
z = cos(2*pi*(x^2+y^2))
ans = krigeInterp(x, y, z, extrap = FALSE)
persp(ans, theta = -40, phi = 30, col = "steelblue",
    xlab = "x", ylab = "y", zlab = "z")
contour(ans)
```

---

kron *Kronecker Product*

Description

Returns the Kronecker product.

Usage

```
kron(x, y)
```

Arguments

x, y	two numeric matrixes.

Details

The *Kronecker product* can be computed using the operator %x% or alternatively using the function kron for SPlus compatibility.

Note

kron is a synonyme to %x%.

References

Golub, van Loan, (1996); *Matrix Computations*, 3rd edition. Johns Hopkins University Press.

Examples

```
## Create Pascal Matrix:
   P = pascal(3)
   P

## Return the Kronecker Product
   kron(P, diag(3))
   P %x% diag(3)
```

`ks2Test` *Two Sample Kolmogorov–Smirnov Test*

Description

Tests if two series are distributional equivalent.

Usage

```
ks2Test(x, y, title = NULL, description = NULL)
```

Arguments

`x, y`	numeric vectors of data values.
`title`	an optional title string, if not specified the inputs data name is deparsed.
`description`	optional description string, or a vector of character strings.

Details

The test `ks2Test` performs a Kolmogorov–Smirnov two sample test that the two data samples `x` and `y` come from the same distribution, not necessarily a normal distribution. That means that it is not specified what that common distribution is.

Value

In contrast to R's output report from S3 objects of class `"htest"` a different output report is produced. The classical tests presented here return an S4 object of class `"fHTEST"`. The object contains the following slots:

`@call`	the function call.
`@data`	the data as specified by the input argument(s).
`@test`	a list whose elements contain the results from the statistical test. The information provided is similar to a list object of class `"htest"`.
`@title`	a character string with the name of the test. This can be overwritten specifying a user defined input argument.

`@description`	a character string with an optional user defined description. By default just the current date when the test was applied will be returned.

The slot `@test` returns an object of class `"list"` containing (at least) the following elements:

`statistic`	the value(s) of the test statistic.
`p.value`	the p-value(s) of the test.
`parameters`	a numeric value or vector of parameters.
`estimate`	a numeric value or vector of sample estimates.
`conf.int`	a numeric two row vector or matrix of 95
`method`	a character string indicating what type of test was performed.
`data.name`	a character string giving the name(s) of the data.

Author(s)

R-core team for hypothesis tests implemented from R's package `ctest`.

References

Conover, W. J. (1971); *Practical nonparametric statistics*, New York: John Wiley & Sons.

Lehmann E.L. (1986); *Testing Statistical Hypotheses*, John Wiley and Sons, New York.

Examples

```
## rnorm -
   # Generate Series:
   x = rnorm(50)
   y = rnorm(50)

## ks2Test -
   ks2Test(x, y)
```

---

lcg *Generator for Portable Random Innovations*

Description

Functions to generate portable random innovations. The functions run under R and S-Plus and generate the same sequence of random numbers. Supported are uniform, normal and Student-t distributed random numbers.

The functions are:

`set.lcgseed`	Set initial random seed,
`get.lcgseed`	Get the current valus of the random seed,
`runif.lcg`	Uniform linear congruational generator,
`rnorm.lcg`	Normal linear congruational generator,
`rt.lcg`	Student-t linear congruential generator.

Usage

```
set.lcgseed(seed = 4711)
get.lcgseed()

runif.lcg(n, min = 0, max = 1)
rnorm.lcg(n, mean = 0, sd = 1)
rt.lcg(n, df)
```

Arguments

df	number of degrees of freedom, a positive integer, maybe non-integer.
mean, sd	means and standard deviation of the normal distributed innovations.
min, max	lower and upper limits of the uniform distributed innovations.
seed	an integer value, the random number seed.
n	an integer, the number of random innovations to be generated.

Details

A simple portable random number generator for use in R and SPlus. We recommend to use this generator only for comparisons of calculations in R and Splus.

The generator is a linear congruential generator with parameters `LCG(a=13445, c=0, m=2^31-1, X=0)`. It is a simple random number generator which passes the bitwise randomness test.

Value

A vector of generated random innovations. The value of the current seed is stored in the variable `lcg.seed`.

References

Altman, N.S. (1988); *Bitwise Behavior of Random Number Generators*, SIAM J. Sci. Stat. Comput., 9(5), September, 941–949.

Examples

```
## set.lcgseed -
   set.lcgseed(seed = 65890)

## runif.lcg - rnorm.lcg - rt.lcg -
   cbind(runif.lcg(10), rnorm.lcg(10), rt.lcg(10, df = 4))

## get.lcgseed -
   get.lcgseed()

## Note, to overwrite rnorm, use
   # rnorm = rnorm.lcg
   # Going back to rnorm
   # rm(rnorm)
```

linearInterp *Bivariate Linear Interpolation*

Description

Bivariate Linear Interpolation. Two options are available gridded and pointwise interpolation.

Usage

```
linearInterp(x, y = NULL, z = NULL, gridPoints = 21,
    xo = seq(min(x), max(x), length = gridPoints),
    yo = seq(min(y), max(y), length = gridPoints))

linearInterpp(x, y = NULL, z = NULL, xo, yo)
```

Arguments

x, y, z	for linearInterp the arguments x and y are two numeric vectors of grid pounts, and z is a numeric matrix or any other rectangular object which can be transformed by the function as.matrix into a matrix object. For linearInterpp we consider either three numeric vectors of equal length or if y and z are NULL, a list with entries x, y, z, or named data frame with x in the first, y in the second, and z in the third column.
gridPoints	an integer value specifying the number of grid points in x and y direction.
xo, yo	for linearInterp two numeric vectors of data points spanning the grid, and for linearInterpp two numeric vectors of data points building pairs for pointwise interpolation.

Value

linearInterp

returns a list with at least three entries, x, y and z. Note, that the returned values, can be directly used by the persp and contour 3D plotting methods.

linearInterpp

returns a data.frame with columns "x", "y", and "z".

See Also

akimaInterp, and krigeInterp.

Examples

```
## linearInterp -
   # Linear Interpolation:
   if (requireNamespace("interp")) {
     set.seed(1953)
     x = runif(999) - 0.5
     y = runif(999) - 0.5
     z = cos(2*pi*(x^2+y^2))
     ans = linearInterp(x, y, z, gridPoints = 41)
     persp(ans, theta = -40, phi = 30, col = "steelblue",
        xlab = "x", ylab = "y", zlab = "z")
     contour(ans)
   }
```

---

listDescription *Description File Listing*

Description

Lists the content of a description file.

Usage

```
listDescription(package, character.only = FALSE)
```

Arguments

package	a literal character or character string denoting the name of the package to be listed.
character.only	a logical indicating whether 'package' can be assumed to be character strings.

Value

prints the description file.

See Also

listFunctions, listIndex.

Examples

```
## listDescription -
   listDescription("fBasics")
```

listFunctions *Functions Listing*

Description

Lists and counts functions from packages.

Usage

```
listFunctions(package, character.only = FALSE)
countFunctions(package, character.only = FALSE)
```

Arguments

package	a literal character or a character string denoting the name of the package to be listed.
character.only	a logical indicating whether 'package' can be assumed to be character strings.

Value

prints a list and counts of functions.

See Also

listFunctions, listIndex.

Examples

```
## listFunctions -
   listFunctions("fBasics")

## countFunctions -
   countFunctions("fBasics")
```

listIndex *Index File Listing*

Description

Lists the content of an index file.

Usage

```
listIndex(package, character.only = FALSE)
```

Arguments

package	a literal character string or a character string denoting the name of the package to be listed.
character.only	a logical indicating whether 'package' can be assumed to be character strings.

Value

prints the index file.

See Also

listDescription, listIndex.

Examples

```
## listIndex -
   listIndex("fBasics")
```

---

locationTest *Two Sample Location Tests*

Description

Tests if two series differ in their distributional location parameter.

Usage

```
locationTest(x, y, method = c("t", "kw2"),
    title = NULL, description = NULL)
```

Arguments

x, y	numeric vectors of data values.
method	a character string naming which test should be applied.
title	an optional title string, if not specified the inputs data name is deparsed.
description	optional description string, or a vector of character strings.

Details

The method="t" can be used to determine if the two sample means are equal for unpaired data sets. Two variants are used, assuming equal or unequal variances.

The method="kw2" performs a Kruskal-Wallis rank sum test of the null hypothesis that the central tendencies or medians of two samples are the same. The alternative is that they differ. Note, that it is not assumed that the two samples are drawn from the same distribution. It is also worth to know that the test assumes that the variables under consideration have underlying continuous distributions.

Value

In contrast to R's output report from S3 objects of class `"htest"` a different output report is produced. The classical tests presented here return an S4 object of class `"fHTEST"`. The object contains the following slots:

`@call`	the function call.
`@data`	the data as specified by the input argument(s).
`@test`	a list whose elements contain the results from the statistical test. The information provided is similar to a list object of class `"htest"`.
`@title`	a character string with the name of the test. This can be overwritten specifying a user defined input argument.
`@description`	a character string with an optional user defined description. By default just the current date when the test was applied will be returned.

The slot `@test` returns an object of class `"list"` containing (at least) the following elements:

`statistic`	the value(s) of the test statistic.
`p.value`	the p-value(s) of the test.
`parameters`	a numeric value or vector of parameters.
`estimate`	a numeric value or vector of sample estimates.
`conf.int`	a numeric two row vector or matrix of 95
`method`	a character string indicating what type of test was performed.
`data.name`	a character string giving the name(s) of the data.

Note

Some of the test implementations are selected from R's `ctest` package.

Author(s)

R-core team for hypothesis tests implemented from R's package `ctest`.

References

Conover, W. J. (1971); *Practical nonparametric statistics*, New York: John Wiley & Sons.

Lehmann E.L. (1986); *Testing Statistical Hypotheses*, John Wiley and Sons, New York.

Examples

```
## rnorm -
   # Generate Series:
   x = rnorm(50)
   y = rnorm(50)

## locationTest -
   locationTest(x, y, "t")
   locationTest(x, y, "kw2")
```

maxdd *Drawdown Statistics*

Description

This is a collection and description of functions which compute drawdown statistics. Included are density, distribution function, and random generation for the maximum drawdown distribution. In addition the expectation of drawdowns for Brownian motion can be computed.

The functions are:

`dmaxdd`	the Density function,
`pmaxdd`	the Distribution function,
`rmaxdd`	the random number generator,
`maxddStats`	the expectation of drawdowns.

Usage

```
dmaxdd(x, sd = 1, horizon = 100, N = 1000)
pmaxdd(q, sd = 1, horizon = 100, N = 1000)
rmaxdd(n, mean = 0, sd = 1, horizon = 100)

maxddStats(mean = 0, sd = 1, horizon = 1000)
```

Arguments

`x, q`	a numeric vector of quantiles.
`n`	an integer value, the number of observations.
`mean, sd`	two numeric values, the mean and standard deviation.
`horizon`	an integer value, the (run time) horizon of the investor.
`N`	an integer value, the precession index for summations. Before you change this value please inspect Magdon-Ismail et. al. (2003).

Value

`dmaxdd`
returns for a trendless Brownian process `mean=0` and standard deviation "sd" the density from the probability that the maximum drawdown "D" is larger or equal to "h" in the interval [0,T], where "T" denotes the time `horizon` of the investor.

`pmaxdd`
returns for a trendless Brownian process `mean=0` and standard deviation "sd" the the probability that the maximum drawdown "D" is larger or equal to "h" in the interval [0,T], where "T" denotes the time `horizon` of the investor.

rmaxdd
returns for a Brownian Motion process with mean mean and standard deviation sd random variates of maximum drawdowns.

maxddStats
returns the expectation Value E[D] of maximum drawdowns of Brownian Motion for a given drift mean, variance sd, and runtime horizon of the Brownian Motion process.

Note

Currrently, for the functions dmaxdd and pmaxdd only the trend or driftless case is implemented.

References

Magdon-Ismail M., Atiya A.F., Pratap A., Abu-Mostafa Y.S. (2003); *On the Maximum Drawdown of a Brownian Motion*, Preprint, CalTech, Pasadena USA, p. 24.

Examples

```
## rmaxdd -
   # Set a random seed
   set.seed(1953)
   # horizon of the investor, time T
   horizon = 1000
   # number of MC samples, N -> infinity
   samples = 1000
   # Range of expected Drawdons
   xlim = c(0, 5)*sqrt(horizon)
   # Plot Histogram of Simulated Max Drawdowns:
   r = rmaxdd(n = samples, mean = 0, sd = 1, horizon = horizon)
   hist(x = r, n = 40, probability = TRUE, xlim = xlim,
     col = "steelblue4", border = "white", main = "Max. Drawdown Density")
   points(r, rep(0, samples), pch = 20, col = "orange", cex = 0.7)

## dmaxdd -
   x = seq(0, xlim[2], length = 200)
   d = dmaxdd(x = x, sd = 1, horizon = horizon, N = 1000)
   lines(x, d, lwd = 2)

## pmaxdd -
   # Count Frequencies of Drawdowns Greater or Equal to "h":
   n = 50
   x = seq(0, xlim[2], length = n)
   g = rep(0, times = n)
   for (i in 1:n) g[i] = length (r[r > x[i]]) / samples
   plot(x, g, type ="h", lwd = 3,
     xlab = "q", main = "Max. Drawdown Probability")
   # Compare with True Probability "G_D(h)":
   x = seq(0, xlim[2], length = 5*n)
   p = pmaxdd(q = x, sd = 1, horizon = horizon, N = 5000)
   lines(x, p, lwd = 2, col="steelblue4")

## maxddStats -
```

```
# Compute expectation Value E[D]:
maxddStats(mean = -0.5, sd = 1, horizon = 10^(1:4))
maxddStats(mean =  0.0, sd = 1, horizon = 10^(1:4))
maxddStats(mean =  0.5, sd = 1, horizon = 10^(1:4))
```

---

nig *Normal Inverse Gaussian Distribution*

Description

Density, distribution function, quantile function and random generation for the normal inverse Gaussian distribution.

Usage

```
dnig(x, alpha = 1, beta = 0, delta = 1, mu = 0, log = FALSE)
pnig(q, alpha = 1, beta = 0, delta = 1, mu = 0)
qnig(p, alpha = 1, beta = 0, delta = 1, mu = 0)
rnig(n, alpha = 1, beta = 0, delta = 1, mu = 0)
```

Arguments

alpha, beta, delta, mu	shape parameter alpha; skewness parameter beta, abs(beta) is in the range (0, alpha); scale parameter delta, delta must be zero or positive; location parameter mu, by default 0. These are the parameters in the first parameterization.
log	a logical flag by default FALSE. Should labels and a main title drawn to the plot?
n	number of observations.
p	a numeric vector of probabilities.
x, q	a numeric vector of quantiles.

Details

The random deviates are calculated with the method described by Raible (2000).

Value

All values for the *nig functions are numeric vectors: d* returns the density, p* returns the distribution function, q* returns the quantile function, and r* generates random deviates.

All values have attributes named "param" listing the values of the distributional parameters.

Author(s)

David Scott for code implemented from R's contributed package HyperbolicDist.

References

Atkinson, A.C. (1982); *The simulation of generalized inverse Gaussian and hyperbolic random variables*, SIAM J. Sci. Stat. Comput. 3, 502–515.

Barndorff-Nielsen O. (1977); *Exponentially decreasing distributions for the logarithm of particle size*, Proc. Roy. Soc. Lond., A353, 401–419.

Barndorff-Nielsen O., Blaesild, P. (1983); *Hyperbolic distributions. In Encyclopedia of Statistical Sciences*, Eds., Johnson N.L., Kotz S. and Read C.B., Vol. 3, pp. 700–707. New York: Wiley.

Raible S. (2000); *Levy Processes in Finance: Theory, Numerics and Empirical Facts*, PhD Thesis, University of Freiburg, Germany, 161 pages.

Examples

```
## nig -
   set.seed(1953)
   r = rnig(5000, alpha = 1, beta = 0.3, delta = 1)
   plot(r, type = "l", col = "steelblue",
     main = "nig: alpha=1 beta=0.3 delta=1")

## nig -
   # Plot empirical density and compare with true density:
   hist(r, n = 25, probability = TRUE, border = "white", col = "steelblue")
   x = seq(-5, 5, 0.25)
   lines(x, dnig(x, alpha = 1, beta = 0.3, delta = 1))

## nig -
   # Plot df and compare with true df:
   plot(sort(r), (1:5000/5000), main = "Probability", col = "steelblue")
   lines(x, pnig(x, alpha = 1, beta = 0.3, delta = 1))

## nig -
   # Compute Quantiles:
   qnig(pnig(seq(-5, 5, 1), alpha = 1, beta = 0.3, delta = 1),
     alpha = 1, beta = 0.3, delta = 1)
```

`nigFit` *Fit of a Normal Inverse Gaussian Distribution*

Description

Estimates the parameters of a normal inverse Gaussian distribution.

Usage

```
nigFit(x, alpha = 1, beta = 0, delta = 1, mu = 0,
    method = c("mle", "gmm", "mps", "vmps"), scale = TRUE, doplot = TRUE,
    span = "auto", trace = TRUE, title = NULL, description = NULL, ...)
```

Arguments

`alpha, beta, delta, mu`
: The parameters are `alpha`, `beta`, `delta`, and `mu`:
shape parameter `alpha`; skewness parameter `beta`, `abs(beta)` is in the range (0, alpha); scale parameter `delta`, `delta` must be zero or positive; location parameter `mu`, by default 0. These is the meaning of the parameters in the first parameterization `pm=1` which is the default parameterization selection. In the second parameterization, `pm=2` `alpha` and `beta` take the meaning of the shape parameters (usually named) `zeta` and `rho`. In the third parameterization, `pm=3` `alpha` and `beta` take the meaning of the shape parameters (usually named) `xi` and `chi`. In the fourth parameterization, `pm=4` `alpha` and `beta` take the meaning of the shape parameters (usually named) `a.bar` and `b.bar`.

`description`
: a character string which allows for a brief description.

`doplot`
: a logical flag. Should a plot be displayed?

`method`
: a character string. Either `"mle"`, Maximum Likelihood Estimation, the default, `"gmm"` Gemeralized Method of Moments Estimation, `"mps"` Maximum Product Spacings Estimation, or `"vmps"` Minimum Variance Product Spacings Estimation.

`scale`
: a logical flag, by default `TRUE`. Should the time series be scaled by its standard deviation to achieve a more stable optimization?

`span`
: x-coordinates for the plot, by default 100 values automatically selected and ranging between the 0.001, and 0.999 quantiles. Alternatively, you can specify the range by an expression like `span=seq(min, max, times = n)`, where, `min` and `max` are the left and right endpoints of the range, and `n` gives the number of the intermediate points.

`title`
: a character string which allows for a project title.

`trace`
: a logical flag. Should the parameter estimation process be traced?

`x`
: a numeric vector.

`...`
: parameters to be parsed.

Value

The functions `tFit`, `hypFit` and `nigFit` return a list with the following components:

`estimate`
: the point at which the maximum value of the log liklihood function is obtained.

`minimum`
: the value of the estimated maximum, i.e. the value of the log liklihood function.

`code`
: an integer indicating why the optimization process terminated.
1: relative gradient is close to zero, current iterate is probably solution;
2: successive iterates within tolerance, current iterate is probably solution;
3: last global step failed to locate a point lower than `estimate`. Either `estimate` is an approximate local minimum of the function or `steptol` is too small;
4: iteration limit exceeded;
5: maximum step size `stepmax` exceeded five consecutive times. Either the function is unbounded below, becomes asymptotic to a finite value from above in some direction or `stepmax` is too small.

gradient	the gradient at the estimated maximum.
steps	number of function calls.

Examples

```
## nigFit -
   # Simulate Random Variates:
   set.seed(1953)
   s = rnig(n = 1000, alpha = 1.5, beta = 0.3, delta = 0.5, mu = -1.0)

## nigFit -
   # Fit Parameters:
   nigFit(s, alpha = 1, beta = 0, delta = 1, mu = mean(s), doplot = TRUE)
```

---

nigMode *Normal Inverse Gaussian Mode*

Description

Computes the mode of the norm inverse Gaussian distribution.

Usage

```
nigMode(alpha = 1, beta = 0, delta = 1, mu = 0)
```

Arguments

alpha, beta, delta, mu	shape parameter alpha; skewness parameter beta, abs(beta) is in the range (0, alpha); scale parameter delta, delta must be zero or positive; location parameter mu, by default 0. These are the parameters in the first parameterization.

Value

returns the mode for the normal inverse Gaussian distribution. A numeric value.

References

Atkinson, A.C. (1982); *The simulation of generalized inverse Gaussian and hyperbolic random variables*, SIAM J. Sci. Stat. Comput. 3, 502–515.

Barndorff-Nielsen O. (1977); *Exponentially decreasing distributions for the logarithm of particle size*, Proc. Roy. Soc. Lond., A353, 401–419.

Barndorff-Nielsen O., Blaesild, P. (1983); *Hyperbolic distributions. In Encyclopedia of Statistical Sciences*, Eds., Johnson N.L., Kotz S. and Read C.B., Vol. 3, pp. 700–707. New York: Wiley.

Raible S. (2000); *Levy Processes in Finance: Theory, Numerics and Empirical Facts*, PhD Thesis, University of Freiburg, Germany, 161 pages.

Examples

```
## nigMode -
   nigMode()
```

---

nigMoments *Moments for the Normal Inverse Gaussian*

Description

Computes the first four moments for the normal inverse Gaussian distribution.

Usage

```
nigMean(alpha = 1, beta = 0, delta = 1, mu = 0)
nigVar(alpha = 1, beta = 0, delta = 1, mu = 0)
nigSkew(alpha = 1, beta = 0, delta = 1, mu = 0)
nigKurt(alpha = 1, beta = 0, delta = 1, mu = 0)
```

Arguments

`alpha, beta, delta, mu`
: are numeric values where `alpha` is the location parameter, `beta` is the location parameter, `delta` is the first shape parameter, and `mu` is the second shape parameter.

Value

All values for the `*nig` functions are numeric vectors: `d*` returns the density, `p*` returns the distribution function, `q*` returns the quantile function, and `r*` generates random deviates.

All values have attributes named `"param"` listing the values of the distributional parameters.

Author(s)

Diethelm Wuertz.

References

Scott, D. J., Wuertz, D. and Tran, T. T. (2008) *Moments of the Generalized Hyperbolic Distribution*. Preprint.

Examples

```
## nigMean -
   # Median:
   nigMean(alpha = 1, beta = 0, delta = 1, mu = 0)

## nigVar -
   # Inter-quartile Range:
   nigVar(alpha = 1, beta = 0, delta = 1, mu = 0)

## nigSKEW -
   # Robust Skewness:
   nigSkew(alpha = 1, beta = 0, delta = 1, mu = 0)

## nigKurt -
   # Robust Kurtosis:
   nigKurt(alpha = 1, beta = 0, delta = 1, mu = 0)
```

`nigRobMoments` *Robust Moments for the NIG*

Description

Computes the first four robust moments for the Normal Inverse Gaussian Distribution.

Usage

```
nigMED(alpha = 1, beta = 0, delta = 1, mu = 0)
nigIQR(alpha = 1, beta = 0, delta = 1, mu = 0)
nigSKEW(alpha = 1, beta = 0, delta = 1, mu = 0)
nigKURT(alpha = 1, beta = 0, delta = 1, mu = 0)
```

Arguments

`alpha, beta, delta, mu`
: are numeric values where `alpha` is the location parameter, `beta` is the location parameter, `delta` is the first shape parameter, and `mu` is the second shape parameter.

Value

All values for the `*nig` functions are numeric vectors: `d*` returns the density, `p*` returns the distribution function, `q*` returns the quantile function, and `r*` generates random deviates.

All values have attributes named `"param"` listing the values of the distributional parameters.

Author(s)

Diethelm Wuertz.

Examples

```
## nigMED -
   # Median:
   nigMED(alpha = 1, beta = 0, delta = 1, mu = 0)

## nigIQR -
   # Inter-quartile Range:
   nigIQR(alpha = 1, beta = 0, delta = 1, mu = 0)

## nigSKEW -
   # Robust Skewness:
   nigSKEW(alpha = 1, beta = 0, delta = 1, mu = 0)

## nigKURT -
   # Robust Kurtosis:
   nigKURT(alpha = 1, beta = 0, delta = 1, mu = 0)
```

---

nigShapeTriangle *NIG Shape Triangle*

Description

Plots the normal inverse Gaussian Shape Triangle.

Usage

```
nigShapeTriangle(object, add = FALSE, labels = TRUE, ...)
```

Arguments

object	an object of class "fDISTFIT" as returned by the function nigFit.
add	a logical value. Should another point added to the NIG shape triangle? By default FALSE, a new plot will be created.
labels	a logical flag by default TRUE. Should the logarithm of the density be returned?
...	arguments to be passed to the function integrate.

Value

displays the parameters of fitted distributions in the NIG shape triangle.

Author(s)

David Scott for code implemented from R's contributed package HyperbolicDist.

References

Atkinson, A.C. (1982); *The simulation of generalized inverse Gaussian and hyperbolic random variables*, SIAM J. Sci. Stat. Comput. 3, 502–515.

Barndorff-Nielsen O. (1977); *Exponentially decreasing distributions for the logarithm of particle size*, Proc. Roy. Soc. Lond., A353, 401–419.

Barndorff-Nielsen O., Blaesild, P. (1983); *Hyperbolic distributions. In Encyclopedia of Statistical Sciences*, Eds., Johnson N.L., Kotz S. and Read C.B., Vol. 3, pp. 700–707. New York: Wiley.

Raible S. (2000); *Levy Processes in Finance: Theory, Numerics and Empirical Facts*, PhD Thesis, University of Freiburg, Germany, 161 pages.

Examples

```
## nigShapeTriangle -
   #
```

`nigSlider` *nigerbolic Distribution Slider*

Description

Displays interactively the dependence of the nigerbolic distribution on its parameters.

Usage

```
nigSlider()
```

Value

a tcl/tk based graphical user interface.

This is a nice display for educational purposes to investigate the densities and probabilities of the invetrse Gaussian distribution.

Examples

```
## nigSlider -
   # nigSlider()
```

norm *Matrix Norm*

Description

Returns the norm of a matrix.

Usage

```
norm2(x, p = 2)
```

Arguments

x	a numeric matrix.
p	an integer value, 1, 2 or Inf. p=1 - The maximum absolute column sum norm which is defined as the maximum of the sum of the absolute valued elements of columns of the matrix. p=2 - The spectral norm is "the norm" of a matrix X. This value is computed as the square root of the maximum eigenvalue of CX where C is the conjugate transpose. p=Inf - The maximum absolute row sum norm is defined as the maximum of the sum of the absolute valued elements of rows of the matrix.

Details

The function norm2 computes the norm of a matrix. Three choices are possible:

p=1 - The maximum absolute column sum norm which is defined as the maximum of the sum of the absolute valued elements of columns of the matrix.

p=2 - The spectral norm is "the norm" of a matrix X. This value is computed as the square root of the maximum eigenvalue of CX where C is the conjugate transpose.

p=Inf - The maximum absolute row sum norm is defined as the maximum of the sum of the absolute valued elements of rows of the matrix.

Note, the function fBasics::norm() has become obsolete, since base::norm() has become available in the R base environment. To avoid conflicts with norm() we have renamed in the fBasics package as norm2.

Value

returns the value of the norm of the matrix.

References

Golub, van Loan, (1996); *Matrix Computations*, 3rd edition. Johns Hopkins University Press.

Examples

```
## Create Pascal Matrix:
   P <- pascal(5)
   P

## Return the Norm of the Matrix:
   norm2(P)
```

`NormalityTests` *Normality Tests*

Description

A collection and description of functions of one sample tests for testing normality of financial return series.

The functions for testing normality are:

`ksnormTest`	Kolmogorov-Smirnov normality test,
`shapiroTest`	Shapiro-Wilk's test for normality,
`jarqueberaTest`	Jarque–Bera test for normality,
`dagoTest`	D'Agostino normality test.

Functions for high precision Jarque Bera LM and ALM tests:

`jbTest`	Performs finite sample adjusted JB LM and ALM test.

Additional functions for testing normality from the 'nortest' package:

`adTest`	Anderson–Darling normality test,
`cvmTest`	Cramer–von Mises normality test,
`lillieTest`	Lilliefors (Kolmogorov-Smirnov) normality test,
`pchiTest`	Pearson chi–square normality test,
`sfTest`	Shapiro–Francia normality test.

For SPlus/Finmetrics Compatibility:

`normalTest`	test suite for some normality tests.

Usage

```
ksnormTest(x, title = NULL, description = NULL)

jbTest(x, title = NULL, description = NULL)
shapiroTest(x, title = NULL, description = NULL)
```

```
normalTest(x, method = c("sw", "jb"), na.rm = FALSE)

jarqueberaTest(x, title = NULL, description = NULL)
dagoTest(x, title = NULL, description = NULL)

adTest(x, title = NULL, description = NULL)
cvmTest(x, title = NULL, description = NULL)
lillieTest(x, title = NULL, description = NULL)
pchiTest(x, title = NULL, description = NULL)
sfTest(x, title = NULL, description = NULL)
```

Arguments

description	optional description string, or a vector of character strings.
method	[normalTest] - indicates four different methods for the normality test, "ks" for the Kolmogorov-Smirnov one–sample test, "sw" for the Shapiro-Wilk test, "jb" for the Jarque-Bera Test, and "da" for the D'Agostino Test. The default value is "ks".
na.rm	[normalTest] - a logical value. Should missing values removed before computing the tests? The default value is FALSE.
title	an optional title string, if not specified the inputs data name is deparsed.
x	a numeric vector of data values or a S4 object of class timeSeries.

Details

The hypothesis tests may be of interest for many financial and economic applications, especially for the investigation of univariate time series returns.

Normal Tests:

Several tests for testing if the records from a data set are normally distributed are available. The input to all these functions may be just a vector x or a univariate time series object x of class timeSeries.

First there exists a wrapper function which allows to call one from two normal tests either the Shapiro–Wilks test or the Jarque–Bera test. This wrapper was introduced for compatibility with S-Plus' FinMetrics package.

Also available are the Kolmogorov–Smirnov one sample test and the D'Agostino normality test.

The remaining five normal tests are the Anderson–Darling test, the Cramer–von Mises test, the Lilliefors (Kolmogorov–Smirnov) test, the Pearson chi–square test, and the Shapiro–Francia test. They are calling functions from R's contributed package nortest. The difference to the original test functions implemented in R and from contributed R packages is that the Rmetrics functions accept time series objects as input and give a more detailed output report.

The Anderson-Darling test is used to test if a sample of data came from a population with a specific distribution, here the normal distribution. The adTest goodness-of-fit test can be considered as a modification of the Kolmogorov–Smirnov test which gives more weight to the tails than does the ksnormTest.

Value

In contrast to R's output report from S3 objects of class `"htest"` a different output report is produced. The tests here return an S4 object of class `"fHTEST"`. The object contains the following slots:

`@call`	the function call.
`@data`	the data as specified by the input argument(s).
`@test`	a list whose elements contain the results from the statistical test. The information provided is similar to a list object of class `"htest"`.
`@title`	a character string with the name of the test. This can be overwritten specifying a user defined input argument.
`@description`	a character string with an optional user defined description. By default just the current date when the test was applied will be returned.

The slot `@test` returns an object of class `"list"` containing the following (otionally empty) elements:

`statistic`	the value(s) of the test statistic.
`p.value`	the p-value(s) of the test.
`parameters`	a numeric value or vector of parameters.
`estimate`	a numeric value or vector of sample estimates.
`conf.int`	a numeric two row vector or matrix of 95
`method`	a character string indicating what type of test was performed.
`data.name`	a character string giving the name(s) of the data.

The meaning of the elements of the `@test` slot is the following:

`ksnormTest`
returns the values for the 'D' statistic and p-values for the three alternatives 'two-sided, 'less' and 'greater'.

`shapiroTest`
returns the values for the 'W' statistic and the p-value.

`jarqueberaTest`
`jbTest`
returns the values for the 'Chi-squared' statistic with 2 degrees of freedom, and the asymptotic p-value. `jbTest` is the finite sample version of the Jarque Bera Lagrange multiplier, LM, and adjusted Lagrange multiplier test, ALM.

`dagoTest`
returns the values for the 'Chi-squared', the 'Z3' (Skewness) and 'Z4' (Kurtosis) statistic together with the corresponding p values.

`adTest`
returns the value for the 'A' statistic and the p-value.

`cvmTest`
returns the value for the 'W' statistic and the p-value.

`lillieTest`
returns the value for the 'D' statistic and the p-value.

`pchiTest`
returns the value for the 'P' statistic and the p-values for the adjusted and not adjusted test cases. In addition the number of classes is printed, taking the default value due to Moore (1986) computed from the expression `n.classes = ceiling(2 * (n^(2/5)))`, where `n` is the number of observations.

`sfTest`
returns the value for the 'W' statistic and the p-value.

Note

Some of the test implementations are selected from R's `ctest` and `nortest` packages.

Author(s)

R-core team for the tests from R's ctest package,
Adrian Trapletti for the runs test from R's tseries package,
Juergen Gross for the normal tests from R's nortest package,
James Filliben for the Fortran program producing the runs report,
Diethelm Wuertz and Helmut Katzgraber for the finite sample JB tests,
Diethelm Wuertz for the Rmetrics R-port.
Earlier versions of theses functions were based on Fortran code of Paul Johnson.

References

Anderson T.W., Darling D.A. (1954); *A Test of Goodness of Fit*, JASA 49:765–69.

Conover, W. J. (1971); *Practical nonparametric statistics*, New York: John Wiley & Sons.

D'Agostino R.B., Pearson E.S. (1973); *Tests for Departure from Normality*, Biometrika 60, 613–22.

D'Agostino R.B., Rosman B. (1974); *The Power of Geary's Test of Normality*, Biometrika 61, 181–84.

Durbin J. (1961); *Some Methods of Constructing Exact Tests*, Biometrika 48, 41–55.

Durbin,J. (1973); *Distribution Theory Based on the Sample Distribution Function*, SIAM, Philadelphia.

Geary R.C. (1947); *Testing for Normality*; Biometrika 36, 68–97.

Lehmann E.L. (1986); *Testing Statistical Hypotheses*, John Wiley and Sons, New York.

Linnet K. (1988); *Testing Normality of Transformed Data*, Applied Statistics 32, 180–186.

Moore, D.S. (1986); *Tests of the chi-squared type*, In: D'Agostino, R.B. and Stephens, M.A., eds., Goodness-of-Fit Techniques, Marcel Dekker, New York.

Shapiro S.S., Francia R.S. (1972); *An Approximate Analysis of Variance Test for Normality*, JASA 67, 215–216.

Shapiro S.S., Wilk M.B., Chen V. (1968); *A Comparative Study of Various Tests for Normality*, JASA 63, 1343–72.

Thode H.C. (2002); *Testing for Normality*, Marcel Dekker, New York.

Weiss M.S. (1978); *Modification of the Kolmogorov-Smirnov Statistic for Use with Correlated Data*, JASA 73, 872–75.

Wuertz D., Katzgraber H.G. (2005); *Precise finite-sample quantiles of the Jarque-Bera adjusted Lagrange multiplier test*, ETHZ Preprint.

Examples

```
## Series:
   x = rnorm(100)

## ksnormTests -
   # Kolmogorov - Smirnov One-Sampel Test
   ksnormTest(x)

## shapiroTest - Shapiro-Wilk Test
   shapiroTest(x)

## jarqueberaTest -
   # Jarque - Bera Test
   # jarqueberaTest(x)
   # jbTest(x)
```

`normRobMoments` *Robust Moments for the NORM*

Description

Computes the first four robust moments for the Normal Distribution.

Usage

```
normMED(mean = 0, sd = 1)
normIQR(mean = 0, sd = 1)
normSKEW(mean = 0, sd = 1)
normKURT(mean = 0, sd = 1)
```

Arguments

`mean`	locaiton parameter
`sd`	scale parameter

Value

All values for the `*norm` functions are numeric vectors: `d*` returns the density, `p*` returns the distribution function, `q*` returns the quantile function, and `r*` generates random deviates.

All values have attributes named `"param"` listing the values of the distributional parameters.

Author(s)

Diethelm Wuertz.

Examples

```
## normMED -
   # Median:
   normMED(mean = 0, sd = 1)

## normIQR -
   # Inter-quartile Range:
   normIQR(mean = 0, sd = 1)

## normSKEW -
   # Robust Skewness:
   normSKEW(mean = 0, sd = 1)

## normKURT -
   # Robust Kurtosis:
   normKURT(mean = 0, sd = 1)
```

---

pascal *Pascal Matrix*

Description

Creates a Pascal matrix.

Usage

```
pascal(n)
```

Arguments

n	an integer value, the dimension of the square matrix.

Details

The function `pascal` generates a Pascal matrix of order `n` which is a symmetric, positive, definite matrix with integer entries made up from Pascal's triangle. The determinant of a Pascal matrix is 1. The inverse of a Pascal matrix has integer entries. If `lambda` is an eigenvalue of a Pascal matrix, then `1/lambda` is also an eigenvalue of the matrix. Pascal matrices are ill-conditioned.

References

Call G.S., Velleman D.J., (1993); *Pascal's matrices*, American Mathematical Monthly 100, 372–376.

Edelman A., Strang G., (2004); *Pascal Matrices*, American Mathematical Monthly 111, 361–385.

Examples

```
## Create Pascal Matrix:
   P = pascal(5)
   P

## Determinant
   det(pascal(5))
   det(pascal(10))
   det(pascal(15))
   det(pascal(20))
```

---

pdl *Polynomial Distributed Lags*

Description

Returns a regressor matrix for polynomial distributed lags.

Usage

```
pdl(x, d = 2, q = 3, trim = FALSE)
```

Arguments

x	a numeric vector.
d	an integer specifying the order of the polynomial.
q	an integer specifying the number of lags to use in creating polynomial distributed lags. This must be greater than d.
trim	a logical flag; if TRUE, the missing values at the beginning of the returned matrix will be trimmed.

See Also

tslag.

Examples

```
## pdl -
   #
```

positiveDefinite *Positive Definite Matrixes*

Description

Checks if a matrix is positive definite and/or forces a matrix to be positive definite.

Usage

```
isPositiveDefinite(x)
makePositiveDefinite(x)
```

Arguments

x	a square numeric matrix.

Details

The function `isPositiveDefinite` checks if a square matrix is positive definite.

The function `makePositiveDefinite` forces a matrix to be positive definite.

Author(s)

Korbinian Strimmer.

Examples

```
## isPositiveDefinite -
   # the 3x3 Pascal Matrix is positive define
   isPositiveDefinite(pascal(3))
```

print *Print Control*

Description

Unlists and prints a control object.

Usage

```
## S3 method for class 'control'
print(x, ...)
```

Arguments

x	the object to be printed.
...	arguments to be passed.

Value

`print.control`

prints control.

Examples

```
## print -
   control = list(n = 211, seed = 54, name = "generator")
   print(control)
   class(control) = "control"
   print(control)
```

`QuantileQuantilePlots` *Quantile-Quantile Plots*

Description

Returns quantile-quantile plots for the normal, the normal inverse Gaussian, the generalized hyperbolic Student-t and the generalized lambda distribution.

List of Functions:

`qqnormPlot`	Returns a tailored Normal quantile-quantile plot,
`qqnigPlot`	Returns a tailored NIG quantile-quantile plot,
`qqghtPlot`	Returns a tailored GHT quantile-quantile plot,
`qqgldPlot`	Returns a tailored GLD quantile-quantile plot.

Usage

```
qqnormPlot(x, labels = TRUE, col = "steelblue", pch = 19,
    title = TRUE, mtext = TRUE, grid = FALSE, rug = TRUE,
    scale = TRUE, ...)
qqnigPlot(x, labels = TRUE, col = "steelblue", pch = 19,
    title = TRUE, mtext = TRUE, grid = FALSE, rug = TRUE,
    scale = TRUE, ...)
qqghtPlot(x, labels = TRUE, col = "steelblue", pch = 19,
    title = TRUE, mtext = TRUE, grid = FALSE, rug = TRUE,
    scale = TRUE, ...)
qqgldPlot(x, labels = TRUE, col = "steelblue", pch = 19,
    title = TRUE, mtext = TRUE, grid = FALSE, rug = TRUE,
    scale = TRUE, ...)
```

Arguments

x	an object of class "timeSeries" or any other object which can be transformed by the function as.timeSeries into an object of class timeSeries. The latter case, other then timeSeries objects, is more or less untested.
labels	a logical flag, should the plot be returned with default labels and decorated in an automated way? By default TRUE.
col	the color for the series. In the univariate case use just a color name like the default, col="steelblue", in the multivariate case we recommend to select the colors from a color palette, e.g. col=heat.colors(ncol(x)).
pch	an integer value, by default 19. Which plot character should be used in the plot?
title	a logical flag, by default TRUE. Should a default title added to the plot?
mtext	a logical flag, by default TRUE. Should a marginal text be printed on the third site of the graph?
grid	a logical flag, should a grid be added to the plot? By default TRUE. To plot a horizontal lines only use grid="h" and for vertical lines use grid="h", respectively.
rug	a logical flag, by default TRUE. Should a rug representation of the data added to the plot?
scale	a logical flag, by default TRUE. Should the time series be scaled for the investigation?
...	optional arguments to be passed.

Value

displays a quantile-quantile plot.

Author(s)

Diethelm Wuertz for the Rmetrics R-port.

Examples

```
## data -
   data(LPP2005REC, package = "timeSeries")
   SPI <- LPP2005REC[, "SPI"]
   plot(SPI, type = "l", col = "steelblue", main = "SP500")
   abline(h = 0, col = "grey")

## qqPlot -
   qqnormPlot(SPI)
```

ReturnSeriesGUI *Return Series Plots*

Description

A graphical user interface to display finanical time series plots.

List of Functions:

`returnSeriesGUI`	Opens a GUI for return series plots.

Usage

```
returnSeriesGUI(x)
```

Arguments

`x`	an object of class `"timeSeries"` or any other object which can be transformed by the function `as.timeSeries` into an object of class `timeSeries`. The latter case, other then `timeSeries` objects, is more or less untested.

Value

`returnSeriesGUI`
For the `returnSeriesGUI` function, beside the graphical user interface no values are returned.

Author(s)

Diethelm Wuertz for the Rmetrics R-port.

Examples

```
##
```

rk *The Rank of a Matrix*

Description

Returns the rank of a matrix.

Usage

```
rk(x, method = c("qr", "chol"))
```

Arguments

x	a numeric matrix.
method	a character string. For method = "qr" the rank is computed as qr(x)\$rank, or alternatively for method="chol" the rank is computed as attr(chol(x, pivot=TRUE), "rank").

Details

The function rk computes the rank of a matrix which is the dimension of the range of the matrix corresponding to the number of linearly independent rows or columns of the matrix, or to the number of nonzero singular values.

The rank of a matrix is also named inear map.

References

Golub, van Loan, (1996); *Matrix Computations*, 3rd edition. Johns Hopkins University Press.

Examples

```
## Create Pascal Matrix:
   P = pascal(5)
   P

## Compute the Rank:
   rk(P)
   rk(P, "chol")
```

---

rowStats *Row Statistics*

Description

Functions to compute row statistical properties of financial and economic time series data.

The functions are:

rowStats	calculates row statistics,
rowSds	calculates row standard deviations,
rowVars	calculates row variances,
rowSkewness	calculates row skewness,
rowKurtosis	calculates row kurtosis,
rowMaxs	calculates maximum values in each row,
rowMins	calculates minimum values in each row,
rowProds	computes product of all values in each row,
rowQuantiles	computes quantiles of each row.

Usage

```
rowStats(x, FUN, ...)




rowSds(x, ...)
rowVars(x, ...)
rowSkewness(x, ...)
rowKurtosis(x, ...)
rowMaxs(x, ...)
rowMins(x, ...)
rowProds(x, ...)
rowQuantiles(x, prob = 0.05, ...)

rowStdevs(x, ...)
rowAvgs(x, ...)
```

Arguments

FUN	a function name. The statistical function to be applied.
prob	a numeric value, the probability with value in [0,1].
x	a rectangular object which can be transformed into a matrix by the function as.matrix.
...	arguments to be passed.

Value

the functions return a numeric vector of the statistics.

See Also

link{colStats}.

Examples

```
## Simulated Return Data in Matrix Form:
   x = matrix(rnorm(10*10), nrow = 10)

## rowStats -
   rowStats(x, FUN = mean)

## rowMaxs -
   rowMaxs(x)
```

sampleLMoments *Sample L-Moments*

Description

Computes L-moments from an empirical sample data set.

Usage

```
sampleLmoments(x, rmax=4)
```

Arguments

x	are numeric vector, the sample values.
rmax	an integer value, the number of L-moments to be returned.

Value

All values for the *sample functions are numeric vectors: d* returns the density, p* returns the distribution function, q* returns the quantile function, and r* generates random deviates.

All values have attributes named "param" listing the values of the distributional parameters.

Author(s)

Diethelm Wuertz.

Examples

```
## Sample:
   x = rt(100, 4)

## sampleLmoments -
   sampleLmoments(x)
```

sampleRobMoments *Robust Moments for the GLD*

Description

Computes the first four robust moments for the Normal Inverse Gaussian Distribution.

Usage

```
sampleMED(x)
sampleIQR(x)
sampleSKEW(x)
sampleKURT(x)
```

Arguments

x	are numeric vector, the sample values.

Value

All values for the *sample functions are numeric vectors: d* returns the density, p* returns the distribution function, q* returns the quantile function, and r* generates random deviates.

All values have attributes named "param" listing the values of the distributional parameters.

Author(s)

Diethelm Wuertz.

Examples

```
## Sample:
   x = rt(100, 4)

## sampleMED -
   # Median:
   sampleMED(x)

## sampleIQR -
   # Inter-quartile Range:
   sampleIQR(x)

## sampleSKEW -
   # Robust Skewness:
   sampleSKEW(x)

## sampleKURT -
   # Robust Kurtosis:
   sampleKURT(x)
```

---

scaleTest *Two Sample Scale Tests*

Description

Tests if two series differ in their distributional scale parameter.

Usage

```
scaleTest(x, y, method = c("ansari", "mood"),
    title = NULL, description = NULL)
```

Arguments

x, y	numeric vectors of data values.
method	a character string naming which test should be applied.
title	an optional title string, if not specified the inputs data name is deparsed.
description	optional description string, or a vector of character strings.

Details

The method="ansari" performs the Ansari–Bradley two–sample test for a difference in scale parameters. The test returns for any sizes of the series x and y the exact p value together with its asymptotic limit.

The method="mood", is another test which performs a two–sample test for a difference in scale parameters. The underlying model is that the two samples are drawn from *f(x-l)* and *f((x-l)/s)/s*, respectively, where *l* is a common location parameter and *s* is a scale parameter. The null hypothesis is *s=1*.

Value

In contrast to R's output report from S3 objects of class "htest" a different output report is produced. The classical tests presented here return an S4 object of class "fHTEST". The object contains the following slots:

@call	the function call.
@data	the data as specified by the input argument(s).
@test	a list whose elements contain the results from the statistical test. The information provided is similar to a list object of class "htest".
@title	a character string with the name of the test. This can be overwritten specifying a user defined input argument.
@description	a character string with an optional user defined description. By default just the current date when the test was applied will be returned.

The slot @test returns an object of class "list" containing (at least) the following elements:

statistic	the value(s) of the test statistic.
p.value	the p-value(s) of the test.
parameters	a numeric value or vector of parameters.
estimate	a numeric value or vector of sample estimates.
conf.int	a numeric two row vector or matrix of 95
method	a character string indicating what type of test was performed.
data.name	a character string giving the name(s) of the data.

Note

Some of the test implementations are selected from R's ctest package.

Author(s)

R-core team for hypothesis tests implemented from R's package ctest.

References

Conover, W. J. (1971); *Practical nonparametric statistics*, New York: John Wiley & Sons.

Lehmann E.L. (1986); *Testing Statistical Hypotheses*, John Wiley and Sons, New York.

Moore, D.S. (1986); *Tests of the chi-squared type*, In: D'Agostino, R.B. and Stephens, M.A., eds., Goodness-of-Fit Techniques, Marcel Dekker, New York.

Examples

```
## rnorm -
   # Generate Series:
   x = rnorm(50)
   y = rnorm(50)

## scaleTest -
   scaleTest(x, y, "ansari")
   scaleTest(x, y, "mood")
```

ScalingLawPlot *Scaling Law Bahaviour*

Description

Evaluates the scaling exponent of a financial return series and plots the scaling law.

Usage

```
scalinglawPlot(x, span = ceiling(log(length(x)/252)/log(2)), doplot = TRUE,
    labels = TRUE, trace = TRUE, ...)
```

Arguments

doplot	a logical value. Should a plot be displayed?
labels	a logical value. Whether or not x- and y-axes should be automatically labeled and a default main title should be added to the plot. By default TRUE.
span	an integer value, determines for the qqgaussPlot the plot range, by default 5, and for the scalingPlot a reasonable number of of points for the scaling range, by default daily data with 252 business days per year are assumed.
trace	a logical value. Should the computation be traced?

x	an uni- or multivariate return series of class `timeSeries` or any other object which can be transformed by the function `as.timeSeries()` into an object of class `timeSeries`.
...	arguments to be passed.

Details

Scaling Behavior:

The function `scalingPlot` plots the scaling law of financial time series under aggregation and returns an estimate for the scaling exponent. The scaling behavior is a very striking effect of the foreign exchange market and also other markets expressing a regular structure for the volatility. Considering the average absolute return over individual data periods one finds a scaling power law which relates the mean volatility over given time intervals to the size of these intervals. The power law is in many cases valid over several orders of magnitude in time. Its exponent usually deviates significantly from a Gaussian random walk model which implies 1/2.

Value

returns a list with the following components: `Intercept`, `Exponent` the scaling exponent, and `InverseExponent` its inverse value.

Author(s)

Diethelm Wuertz for the Rmetrics R-port.

References

Taylor S.J. (1986); *Modeling Financial Time Series*, John Wiley and Sons, Chichester.

Examples

```
## data -
   data(LPP2005REC, package = "timeSeries")
   SPI <- LPP2005REC[, "SPI"]
   plot(SPI, type = "l", col = "steelblue", main = "SP500")
   abline(h = 0, col = "grey")

## teffectPlot -
   # Scaling Law Effect:
   scalinglawPlot(SPI)
```

sgh *Standardized Generalized Hyperbolic Distribution*

Description

Density, distribution function, quantile function and random generation for the standardized generalized hyperbolic distribution.

Usage

```
dsgh(x, zeta = 1, rho = 0, lambda = 1, log = FALSE)
psgh(q, zeta = 1, rho = 0, lambda = 1)
qsgh(p, zeta = 1, rho = 0, lambda = 1)
rsgh(n, zeta = 1, rho = 0, lambda = 1)
```

Arguments

zeta, rho, lambda	shape parameter zeta is positive, skewness parameter rho is in the range (-1, 1).
log	a logical flag by default FALSE. If TRUE, log values are returned.
n	number of observations.
p	a numeric vector of probabilities.
x, q	a numeric vector of quantiles.

Details

The generator rsgh is based on the GH algorithm given by Scott (2004).

Value

All values for the *sgh functions are numeric vectors: d* returns the density, p* returns the distribution function, q* returns the quantile function, and r* generates random deviates.

All values have attributes named "param" listing the values of the distributional parameters.

Author(s)

Diethelm Wuertz.

Examples

```
## rsgh -
   set.seed(1953)
   r = rsgh(5000, zeta = 1, rho = 0.5, lambda = 1)
   plot(r, type = "l", col = "steelblue",
     main = "gh: zeta=1 rho=0.5 lambda=1")
```

```
## dsgh -
   # Plot empirical density and compare with true density:
   hist(r, n = 50, probability = TRUE, border = "white", col = "steelblue",
     ylim = c(0, 0.6))
   x = seq(-5, 5, length = 501)
   lines(x, dsgh(x, zeta = 1, rho = 0.5, lambda = 1))

## psgh -
   # Plot df and compare with true df:
   plot(sort(r), (1:5000/5000), main = "Probability", col = "steelblue")
   lines(x, psgh(x, zeta = 1, rho = 0.5, lambda = 1))

## qsgh -
   # Compute Quantiles:
   round(qsgh(psgh(seq(-5, 5, 1), zeta = 1, rho = 0.5), zeta = 1, rho = 0.5), 4)
```

---

sghFit *Standardized GH Distribution Fit*

Description

Estimates the distrinbutional parameters for a standardized generalized hyperbolic distribution.

Usage

```
sghFit(x, zeta = 1, rho = 0, lambda = 1, include.lambda = TRUE,
    scale = TRUE, doplot = TRUE, span = "auto", trace = TRUE,
    title = NULL, description = NULL, ...)
```

Arguments

x	a numeric vector.
zeta, rho, lambda	shape parameter zeta is positive, skewness parameter rho is in the range (-1, 1). and index parameter lambda, by default 1.
include.lambda	a logical flag, by default TRUE. Should the index parameter lambda included in the parameter estimate?
scale	a logical flag, by default TRUE. Should the time series be scaled by its standard deviation to achieve a more stable optimization?
doplot	a logical flag. Should a plot be displayed?
span	x-coordinates for the plot, by default 100 values automatically selected and ranging between the 0.001, and 0.999 quantiles. Alternatively, you can specify the range by an expression like span=seq(min, max, times = n), where, min and max are the left and right endpoints of the range, and n gives the number of the intermediate points.
trace	a logical flag. Should the parameter estimation process be traced?

title	a character string which allows for a project title.
description	a character string which allows for a brief description.
...	parameters to be parsed.

Value

returns a list with the following components:

estimate	the point at which the maximum value of the log liklihood function is obtained.
minimum	the value of the estimated maximum, i.e. the value of the log liklihood function.
code	an integer indicating why the optimization process terminated. 1: relative gradient is close to zero, current iterate is probably solution; 2: successive iterates within tolerance, current iterate is probably solution; 3: last global step failed to locate a point lower than estimate. Either estimate is an approximate local minimum of the function or steptol is too small; 4: iteration limit exceeded; 5: maximum step size stepmax exceeded five consecutive times. Either the function is unbounded below, becomes asymptotic to a finite value from above in some direction or stepmax is too small.
gradient	the gradient at the estimated maximum.
steps	number of function calls.

Examples

```
## sghFit -
   # Simulate Random Variates:
   set.seed(1953)
   s = rsgh(n = 2000, zeta = 0.7, rho = 0.5, lambda = 0)

## sghFit -
   # Fit Parameters:
   sghFit(s, zeta = 1, rho = 0, lambda = 1, include.lambda = TRUE,
     doplot = TRUE)
```

---

sght *Standardized generalized hyperbolic Student-t Distribution*

Description

Density, distribution function, quantile function and random generation for the standardized generalized hyperbolic distribution.

Usage

```
dsght(x, beta = 0.1, delta = 1, mu = 0, nu = 10, log = FALSE)
psght(q, beta = 0.1, delta = 1, mu = 0, nu = 10)
qsght(p, beta = 0.1, delta = 1, mu = 0, nu = 10)
rsght(n, beta = 0.1, delta = 1, mu = 0, nu = 10)
```

Arguments

beta, delta, mu	numeric values. beta is the skewness parameter in the range (0, alpha); delta is the scale parameter, must be zero or positive; mu is the location parameter, by default 0. These are the parameters in the first parameterization.
nu	a numeric value, the number of degrees of freedom. Note, alpha takes the limit of abs(beta), and lambda=-nu/2.
x, q	a numeric vector of quantiles.
p	a numeric vector of probabilities.
n	number of observations.
log	a logical, if TRUE, probabilities p are given as log(p).

Value

All values for the *sght functions are numeric vectors: d* returns the density, p* returns the distribution function, q* returns the quantile function, and r* generates random deviates.

All values have attributes named "param" listing the values of the distributional parameters.

Author(s)

Diethelm Wuertz.

Examples

```
## rsght -
   set.seed(1953)
   r = rsght(5000, beta = 0.1, delta = 1, mu = 0, nu = 10)
   plot(r, type = "l", col = "steelblue",
     main = "gh: zeta=1 rho=0.5 lambda=1")

## dsght -
   # Plot empirical density and compare with true density:
   hist(r, n = 50, probability = TRUE, border = "white", col = "steelblue")
   x = seq(-5, 5, length = 501)
   lines(x, dsght(x, beta = 0.1, delta = 1, mu = 0, nu = 10))

## psght -
   # Plot df and compare with true df:
   plot(sort(r), (1:5000/5000), main = "Probability", col = "steelblue")
   lines(x, psght(x, beta = 0.1, delta = 1, mu = 0, nu = 10))

## qsght -
   # Compute Quantiles:
   round(qsght(psght(seq(-5, 5, 1), beta = 0.1, delta = 1, mu = 0, nu =10),
               beta = 0.1, delta = 1, mu = 0, nu = 10), 4)
```

snig *Standardized Normal Inverse Gaussian Distribution*

Description

Density, distribution function, quantile function and random generation for the standardized normal inverse Gaussian distribution.

Usage

```
dsnig(x, zeta = 1, rho = 0, log = FALSE)
psnig(q, zeta = 1, rho = 0)
qsnig(p, zeta = 1, rho = 0)
rsnig(n, zeta = 1, rho = 0)
```

Arguments

zeta, rho	shape parameter zeta is positive, skewness parameter rho is in the range (-1, 1).
log	a logical flag by default FALSE. If TRUE, log values are returned.
n	number of observations.
p	a numeric vector of probabilities.
x, q	a numeric vector of quantiles.

Details

The random deviates are calculated with the method described by Raible (2000).

Value

All values for the *snig functions are numeric vectors: d* returns the density, p* returns the distribution function, q* returns the quantile function, and r* generates random deviates.

All values have attributes named "param" listing the values of the distributional parameters.

Author(s)

Diethelm Wuertz.

Examples

```
## snig -
   set.seed(1953)
   r = rsnig(5000, zeta = 1, rho = 0.5)
   plot(r, type = "l", col = "steelblue",
     main = "snig: zeta=1 rho=0.5")

## snig -
```

```
   # Plot empirical density and compare with true density:
   hist(r, n = 50, probability = TRUE, border = "white", col = "steelblue")
   x = seq(-5, 5, length = 501)
   lines(x, dsnig(x, zeta = 1, rho = 0.5))

## snig -
   # Plot df and compare with true df:
   plot(sort(r), (1:5000/5000), main = "Probability", col = "steelblue")
   lines(x, psnig(x, zeta = 1, rho = 0.5))

## snig -
   # Compute Quantiles:
   qsnig(psnig(seq(-5, 5, 1), zeta = 1, rho = 0.5), zeta = 1, rho = 0.5)
```

---

snigFit *Fit of a Standardized NIG Distribution*

Description

Estimates the parameters of a standardized normal inverse Gaussian distribution.

Usage

```
snigFit(x, zeta = 1, rho = 0, scale = TRUE, doplot = TRUE,
    span = "auto", trace = TRUE, title = NULL, description = NULL, ...)
```

Arguments

zeta, rho	shape parameter zeta is positive, skewness parameter rho is in the range (-1, 1).
description	a character string which allows for a brief description.
doplot	a logical flag. Should a plot be displayed?
scale	a logical flag, by default TRUE. Should the time series be scaled by its standard deviation to achieve a more stable optimization?
span	x-coordinates for the plot, by default 100 values automatically selected and ranging between the 0.001, and 0.999 quantiles. Alternatively, you can specify the range by an expression like span=seq(min, max, times = n), where, min and max are the left and right endpoints of the range, and n gives the number of the intermediate points.
title	a character string which allows for a project title.
trace	a logical flag. Should the parameter estimation process be traced?
x	a numeric vector.
...	parameters to be parsed.

Value

The function snigFit returns a list with the following components:

estimate	the point at which the maximum value of the log liklihood function is obtained.
minimum	the value of the estimated maximum, i.e. the value of the log liklihood function.
code	an integer indicating why the optimization process terminated. 1: relative gradient is close to zero, current iterate is probably solution; 2: successive iterates within tolerance, current iterate is probably solution; 3: last global step failed to locate a point lower than estimate. Either estimate is an approximate local minimum of the function or steptol is too small; 4: iteration limit exceeded; 5: maximum step size stepmax exceeded five consecutive times. Either the function is unbounded below, becomes asymptotic to a finite value from above in some direction or stepmax is too small.
gradient	the gradient at the estimated maximum.
steps	number of function calls.

Examples

```
## snigFit -
   # Simulate Random Variates:
   set.seed(1953)
   s = rsnig(n = 2000, zeta = 0.7, rho = 0.5)

## snigFit -
   # Fit Parameters:
   snigFit(s, zeta = 1, rho = 0, doplot = TRUE)
```

---

ssd *Spline Smoothed Distribution*

Description

Density, distribution function, quantile function and random generation from smoothing spline estimates.

Usage

```
dssd(x, param, log = FALSE)
pssd(q, param)
qssd(p, param)
rssd(n, param)
```

Arguments

param	an object as returned by the function ssdFit..
log	a logical flag by default FALSE. Should labels and a main title drawn to the plot?
n	number of observations.
p	a numeric vector of probabilities.
x, q	a numeric vector of quantiles.

Value

All values for the *ssd functions are numeric vectors: d* returns the density, p* returns the distribution function, q* returns the quantile function, and r* generates random deviates.

All values have attributes named "param" listing the values of the distributional parameters.

Author(s)

Diethelm Wuertz, Chong Gu for the underlying gss package.

References

Gu, C. (2002), *Smoothing Spline ANOVA Models*, New York Springer–Verlag.

Gu, C. and Wang, J. (2003), *Penalized likelihood density estimation: Direct cross-validation and scalable approximation*, Statistica Sinica, 13, 811–826.

Examples

```
## ssdFit -
   set.seed(1953)
   r = rnorm(500)
   hist(r, breaks = "FD", probability = TRUE,
     col = "steelblue", border = "white")

## ssdFit -
   param = ssdFit(r)

## dssd -
   u = seq(min(r), max(r), len = 301)
   v = dssd(u, param)
   lines(u, v, col = "orange", lwd = 2)
```

ssdFit *Fit Density Using Smoothing Splines*

Description

Estimates the parameters of a density function using smoothing splines.

Usage

```
ssdFit(x)
```

Arguments

x	a numeric vector.

Value

The function ssdFit, hypFit returns an object of class ssden. The returned object can be used to evaluate density, probabilities and quantiles.

Author(s)

Diethelm Wuertz, Chong Gu for the underlying gss package.

References

Gu, C. (2002), *Smoothing Spline ANOVA Models*, New York Springer–Verlag.

Gu, C. and Wang, J. (2003), *Penalized likelihood density estimation: Direct cross-validation and scalable approximation*, Statistica Sinica, 13, 811–826.

Examples

```
## ssdFit -
   set.seed(1953)
   r = rnorm(500)
   hist(r, breaks = "FD", probability = TRUE,
     col = "steelblue", border = "white")

## ssdFit -
   param = ssdFit(r)

## dssd -
   u = seq(min(r), max(r), len = 301)
   v = dssd(u, param)
   lines(u, v, col = "orange", lwd = 2)
```

StableSlider *Slider GUI for Stable Distribution*

Description

The `stableSlider()` function provides interactive displays of density and probabilities of stable distributions.

Usage

```
stableSlider(col= "steelblue", col.med = "gray30")
```

Arguments

`col, col.med`	optional arguments for the slider.

Value

The `stableSlider()` function displays densities and probabilities of the skew stable distribution, for educational purposes.

Author(s)

Diethelm Wuertz for the Rmetrics R-port.

References

see those in `dstable`, in package **stabledist**.

Examples

```
if(dev.interactive())
   stableSlider()
```

symbolTable *Table of Symbols*

Description

Displays a Table of plot characters and symbols.

Usage

```
symbolTable(font = par('font'), cex = 0.7)
```

Arguments

cex	a numeric value, determines the character size, the default size is 0.7.
font	an integer value, the number of the font, by default font number 1.

Value

symbolTable

displays a table with the plot characters and symbols numbered from 0 to 255 and returns invisible the name of the font.

See Also

link{characterTable}, link{colorTable}.

Examples

```
## symbolTable -
   # Default Symbol Table:
# symbolTable()
```

TimeSeriesPlots *Financial Time Series Plots*

Description

Returns an index/price, a return, or a drawdown plot.

List of Functions:

seriesPlot	Returns a tailored return series plot,
cumulatedPlot	Displays a cumulated series given the returns,
returnPlot	Displays returns given the cumulated series,
drawdownPlot	Displays drawdowns given the return series.

Usage

```
seriesPlot(x, labels = TRUE, type = "l", col = "steelblue",
    title = TRUE, grid = TRUE, box = TRUE, rug = TRUE, ...)
cumulatedPlot(x, index = 100, labels = TRUE, type = "l", col = "steelblue",
    title = TRUE, grid = TRUE, box = TRUE, rug = TRUE, ...)
returnPlot(x, labels = TRUE, type = "l", col = "steelblue",
    title = TRUE, grid = TRUE, box = TRUE, rug = TRUE, ...)
drawdownPlot(x, labels = TRUE, type = "l", col = "steelblue",
    title = TRUE, grid = TRUE, box = TRUE, rug = TRUE, ...)
```

Arguments

box	a logical flag, should a box be added to the plot? By default TRUE.
col	the color for the series. In the univariate case use just a color name like the default, col="steelblue", in the multivariate case we recommend to select the colors from a color palette, e.g. col=heat.colors(ncol(x)).
grid	a logical flag, should a grid be added to the plot? By default TRUE.
index	a numeric value, by default 100. The function cumulates column by colum the returns and multiplies the result with the index value: index*exp(colCumsums(x)).
labels	a logical flag, should the plot be returned with default labels and decorated in an automated way? By default TRUE.
rug	a logical flag, by default TRUE. Should a rug representation of the data added to the plot?
title	a logical flag, by default TRUE. Should a default title added to the plot?
type	what type of plot should be drawn? By default we use a line plot, type="l". An alternative plot style which produces nice figures is for example type="h".
x	an object of class "timeSeries" or any other object which can be transformed by the function as.timeSeries into an object of class timeSeries. The latter case, other then timeSeries objects, is more or less untested.
...	optional arguments to be passed.

Details

The plot functions can be used to plot univariate and multivariate time series of class timeSeries.

The graphical parameters type and col can be set by the values specified through the argument list. In the case of multivariate time series col can be specified by the values returned by a color palette.

Automated titles including main title, x- and y-lables, grid lines, box style and rug represenatations cann be selected by setting these arguments to TRUE which is the default. If the title flag is unset, then the main title, x-, and y-labels are empty strings. This allows to set user defined labels with the function title after the plot is drawn.

Beside type, col, main, xlab and ylab, all other par arguments can be passed to the plot function.

If the labels flag is unset to FALSE, then no decorations will be added tothe plot, and the plot can be fully decorated by the user.

Value

displays a time series plot.

Examples

```
## seriesPlot -
   data(LPP2005REC, package = "timeSeries")
   tS <- as.timeSeries(LPP2005REC)
   seriesPlot(tS)
```

tr *Trace of a Matrix*

Description

Returns trace of a matrix.

Usage

```
tr(x)
```

Arguments

x	a numeric matrix.

Details

The function tr computes the trace of a square matrix which is the sum of the diagonal elements of the matrix under consideration.

References

Golub, van Loan, (1996); *Matrix Computations*, 3rd edition. Johns Hopkins University Press.

Examples

```
## Create Pascal Matrix:
   P = pascal(3)
   P

## Trace:
   tr(P)
```

triang *Upper and Lower Triangular Matrixes*

Description

Extracs the pper or lower tridiagonal part from a matrix.

Usage

```
triang(x)
Triang(x)
```

Arguments

x	a numeric matrix.

Details

The functions triang and Triang allow to transform a square matrix to a lower or upper triangular form. A triangular matrix is either an upper triangular matrix or lower triangular matrix. For the first case all matrix elements a[i,j] of matrix A are zero for i>j, whereas in the second case we have just the opposite situation. A lower triangular matrix is sometimes also called left triangular. In fact, triangular matrices are so useful that much computational linear algebra begins with factoring or decomposing a general matrix or matrices into triangular form. Some matrix factorization methods are the Cholesky factorization and the LU-factorization. Even including the factorization step, enough later operations are typically avoided to yield an overall time savings. Triangular matrices have the following properties: the inverse of a triangular matrix is a triangular matrix, the product of two triangular matrices is a triangular matrix, the determinant of a triangular matrix is the product of the diagonal elements, the eigenvalues of a triangular matrix are the diagonal elements.

References

Higham, N.J., (2002); *Accuracy and Stability of Numerical Algorithms*, 2nd ed., SIAM.

Golub, van Loan, (1996); *Matrix Computations*, 3rd edition. Johns Hopkins University Press.

Examples

```
## Create Pascal Matrix:
   P = pascal(3)
   P

## Create lower triangle matrix
   L = triang(P)
   L
```

---

tsHessian *Two sided approximated Hessian*

Description

Computes two sided (TS) approximated Hessian.

Usage

```
tsHessian(x, fun, ...)
```

Arguments

x	argument to be passed to fun.
fun	function.
...	additional parameters to be passed to fun.

Author(s)

A function borrowed from Kevin Sheppard's Matlab garch toolbox as implemented by Alexios Ghalanos in his **rgarch** package

---

tslag *Lagged or Leading Vector/Matrix*

Description

Creates a lagged or leading vector/matrix of selected order(s).

Usage

```
tslag(x, k = 1, trim = FALSE)
```

Arguments

k	an integer value, the number of positions the new series is to lag or to lead the input series.
x	a numeric vector or matrix, missing values are allowed.
trim	a logical flag, if TRUE, the missing values at the beginning ans/or end of the returned series will be trimmed. The default value is FALSE.

See Also

pdl.

Examples

```
## tslag -
   #
```

---

varianceTest *Two Sample Variance Tests*

Description

Tests if two series differ in their distributional variance parameter.

Usage

```
varianceTest(x, y, method = c("varf", "bartlett", "fligner"),
    title = NULL, description = NULL)
```

Arguments

x, y	numeric vectors of data values.
method	a character string naming which test should be applied.
title	an optional title string, if not specified the inputs data name is deparsed.
description	optional description string, or a vector of character strings.

Details

The method="varf" can be used to compare variances of two normal samples performing an F test. The null hypothesis is that the ratio of the variances of the populations from which they were drawn is equal to one.

The method="bartlett" performs the Bartlett test of the null hypothesis that the variances in each of the samples are the same. This fact of equal variances across samples is also called *homogeneity of variances*. Note, that Bartlett's test is sensitive to departures from normality. That is, if the samples come from non-normal distributions, then Bartlett's test may simply be testing for non-normality. The Levene test (not yet implemented) is an alternative to the Bartlett test that is less sensitive to departures from normality.

The method="fligner" performs the Fligner-Killeen test of the null that the variances in each of the two samples are the same.

Value

In contrast to R's output report from S3 objects of class "htest" a different output report is produced. The classical tests presented here return an S4 object of class "fHTEST". The object contains the following slots:

@call	the function call.
@data	the data as specified by the input argument(s).
@test	a list whose elements contain the results from the statistical test. The information provided is similar to a list object of class "htest".
@title	a character string with the name of the test. This can be overwritten specifying a user defined input argument.
@description	a character string with an optional user defined description. By default just the current date when the test was applied will be returned.

The slot @test returns an object of class "list" containing (at least) the following elements:

statistic	the value(s) of the test statistic.
p.value	the p-value(s) of the test.
parameters	a numeric value or vector of parameters.
estimate	a numeric value or vector of sample estimates.
conf.int	a numeric two row vector or matrix of 95
method	a character string indicating what type of test was performed.
data.name	a character string giving the name(s) of the data.

Note

Some of the test implementations are selected from R's `ctest` package.

Author(s)

R-core team for hypothesis tests implemented from R's package `ctest`.

References

Conover, W. J. (1971); *Practical nonparametric statistics*, New York: John Wiley & Sons.

Lehmann E.L. (1986); *Testing Statistical Hypotheses*, John Wiley and Sons, New York.

Examples

```
## rnorm -
   # Generate Series:
   x = rnorm(50)
   y = rnorm(50)

## varianceTest -
   varianceTest(x, y, "varf")
   varianceTest(x, y, "bartlett")
   varianceTest(x, y, "fligner")
```

`vec` *Stacking Vectors and Matrixes*

Description

Stacks either a lower triangle matrix or a matrix.

Usage

```
vec(x)
vech(x)
```

Arguments

`x`	a numeric matrix.

Details

The function `vec` implements the operator that stacks a matrix as a column vector, to be more precise in a matrix with one column. vec(X) = (X11, X21, ..., XN1, X12, X22, ..., XNN).

The function `vech` implements the operator that stacks the lower triangle of a NxN matrix as an N(N+1)/2x1 vector: vech(X) =(X11, X21, X22, X31, ..., XNN), to be more precise in a matrix with one row.

Examples

```
## Create Pascal Matrix:
   P = pascal(3)

## Stack a matrix
   vec(P)

## Stack the lower triangle
   vech(P)
```

Index