

# Package ‘qualypsoss’

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**License** GPL-3

**Title** Uncertainties of Climate Projections using Smoothing Splines

**Version** 1.1.1

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**Imports** foreach, doParallel, stats, utils, MASS, mvtnorm, graphics,  
grDevices,ggthemes,QUALYPSO

**Description** These functions use smoothing-splines for the assessment of single-member ensembles of climate projections.  
- Cheng, C.-I. and P. L. Speckman (2012) <[doi:10.1016/j.csda.2012.05.020](https://doi.org/10.1016/j.csda.2012.05.020)>.

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---

compute.change.variable

*Compute change variables*

---

### Description

Compute change variables

### Usage

compute.change.variable(climResponse, l0pt, lDim, iCpredContUnique, iCpredCont)

**Arguments**

climResponse	output from <a href="#">extract.climate.response</a>
lOpt	list of options, returned by <a href="#">QUALYPSOSS.check.option</a>
lDim	list of dimensions
iCpredContUnique	index in 1:nP indicating the reference continuous predictor for the computation of change variables.
iCpredCont	index in 1:nT indicating the reference period (reference period) for the computation of change variables.

**Value**

list with the following fields:

- **phiStar.MCMC**: MCMC draws of climate change response
- **etaStar.MCMC**: MCMC draws of deviation from the climate change response

**Author(s)**

Guillaume Evin

---

extract.climate.response

*Extract climate response for one time series z*

---

**Description**

Extract climate response for one time series z

**Usage**

```
extract.climate.response(
  ClimateProjections,
  predCont,
  predContUnique,
  nMCMC,
  lam,
  uniqueFit,
  spar = spar,
  listCR = NULL
)
```

**Arguments**

ClimateProjections	matrix of climate projections
predCont	matrix of continuous predictor corresponding to the climate projections
predContUnique	vector of predictors for which we need fitted climate reponses
nMCMC	number of MCMC samples
lam	fixed smoothing parameter lambda
uniqueFit	logical value indicating if only one fit is applied
spar	smoothing parameter spar in <code>smooth.spline</code> : must be greater than zero
listCR	list of objects for the extraction of the climate response

**Value**

list with the following fields:

- **phi.MCMC**: MCMC draws of climate response
- **eta.MCMC**: MCMC draws of deviation from the climate response
- **deltaIV.MCMC**: MCMC draws of deltaRV
- **listCR**: list of objects for faster computation on grids

**Author(s)**

Guillaume Evin

---

formatQUALYPSSoutput *formatQUALYPSSoutput*

---

**Description**

formatQUALYPSSoutput

**Usage**

```
formatQUALYPSSoutput(
  lOpt,
  lDim,
  lScen,
  ANOVA.step1,
  ANOVA.step2,
  ANOVA.step3,
  climResponse,
  change.variable
)
```

**Arguments**

lOpt	list of options, returned by <a href="#">QUALYPSOSS.check.option</a>
lDim	list of dimensions
lScen	list of scenario characteristics, output from <a href="#">QUALYPSOSS.process.scenario</a>
ANOVA.step1	list provided by <a href="#">QUALYPSOSS.ANOVA.step1</a>
ANOVA.step2	list provided by <a href="#">QUALYPSOSS.ANOVA.step2</a>
ANOVA.step3	list provided by <a href="#">QUALYPSOSS.ANOVA.step3</a>
climResponse change.variable	list containing phi, eta, provided by <a href="#">extract.climate.response</a> list containing phiStar, etaStar, provided by <a href="#">compute.change.variable</a>

**Value**

list with the following fields:

- **POINT**: list containing the mean estimate of different quantities: RESIDUALVAR (residual variability), INTERNALVAR (internal variability), GRANDMEAN (grand mean for all time steps), MAINEFFECT (list with one item per discrete predictor  $i$ , containing matrices  $n_T \times n_{Eff_i}$ , where  $n_{Eff_i}$  is the number of possible values for the discrete predictor  $i$ ). EFFECTVAR, uncertainty related to the different main effect, TOTVAR Total variability, DECOMPVAR, decomposition of the total variability (percentages) for the different components, CONTRIB\_EACH\_EFFECT, contribution of each individual effects (percentages) to the corr. effect uncertainty.
- **BAYES**: list containing quantiles of different estimated quantities, listed in **POINT**.
- **MCMC**: MCMC draws for the different quantities.

**Author(s)**

Guillaume Evin

---

get.det.AR1                      *get.det.AR1 return the determinant of the matrix provided by*  
[get.matrix.AR1](#)

---

**Description**

get.det.AR1 return the determinant of the matrix provided by [get.matrix.AR1](#)

**Usage**

```
get.det.AR1(nP, rho, nMO)
```

**Arguments**

nP	number of continuous predictors (e.g. future times)
rho	AR(1) correlation parameter in (-1,1)
nMO	number of possible simulation chains (missing and non-missing)

**Value**

determinant of the AR1 matrix

**Author(s)**

Guillaume Evin

---

`get.det.KMS`

*get.det.KMS return the determinant of the KMS matrix*

---

**Description**

`get.det.KMS` return the determinant of the KMS matrix

**Usage**

`get.det.KMS(nP, rho)`

**Arguments**

`nP`                    number of continuous predictors (e.g. future times)  
`rho`                    AR(1) correlation parameter in (-1,1)

**Value**

determinant of the KMS matrix

**Author(s)**

Guillaume Evin

---

`get.logdet.W`

*get.logdet.W Return the logarithm of the determinant of the matrix W*

---

**Description**

`get.logdet.W` Return the logarithm of the determinant of the matrix *W*

**Usage**

`get.logdet.W(weight.hetero, nMO, nP, rho)`

**Arguments**

- weight.hetero    output of [get.vec.weight.hetero](#)
- nMO              number of possible simulation chains (missing and non-missing)
- nP                number of continuous predictors (e.g. future times)
- rho               AR(1) correlation parameter in (-1,1)

**Value**

logarithm of the determinant of the matrix W

**Author(s)**

Guillaume Evin

---

`get.matrix.AR1`            *get.matrix.AR1* return the matrix of AR(1) correlations corresponding to the entire ensemble

---

**Description**

`get.matrix.AR1` return the matrix of AR(1) correlations corresponding to the entire ensemble

**Usage**

`get.matrix.AR1(nP, rho, nMO)`

**Arguments**

- nP                number of continuous predictors (e.g. future times)
- rho               AR(1) correlation parameter in (-1,1)
- nMO              number of possible simulation chains (missing and non-missing)

**Value**

C matrix n x n of AR(1) correlations where coden is the total number of predictions (all the predictions for all the possible simulation chains)

**Author(s)**

Guillaume Evin

---

get.matrix.AR1.inv     *get.matrix.AR1.inv return the inverse matrix of AR(1) correlations corresponding to the entire ensemble*

---

### Description

get.matrix.AR1.inv return the inverse matrix of AR(1) correlations corresponding to the entire ensemble

### Usage

```
get.matrix.AR1.inv(nP, rho, nMO)
```

### Arguments

nP	number of continuous predictors (e.g. future times)
rho	AR(1) correlation parameter in (-1,1)
nMO	number of possible simulation chains (missing and non-missing)

### Value

inverse matrix  $n \times n$  of AR(1) correlations where  $n$  is the total number of predictions (all the predictions for all the possible simulation chains)

### Author(s)

Guillaume Evin

---

get.matrix.hetero     *get.matrix.hetero returns the matrix of weights for the computation of heteroscedastic errors corresponding to the entire ensemble*

---

### Description

get.matrix.hetero returns the matrix of weights for the computation of heteroscedastic errors corresponding to the entire ensemble

### Usage

```
get.matrix.hetero(weight.hetero, nMO)
```

### Arguments

weight.hetero	output of <a href="#">get.vec.weight.hetero</a>
nMO	number of possible simulation chains (missing and non-missing)



**Value**

V matrix n x n of weights where coden is the total number of predictions (all the predictions for all the possible simulation chains)

**Author(s)**

Guillaume Evin

---

`get.matrix.hetero.inv` *get.matrix.hetero.inv* returns the inverse of the matrix of weights for the computation of heteroscedastic errors corresponding to the entire ensemble

---

**Description**

`get.matrix.hetero.inv` returns the inverse of the matrix of weights for the computation of heteroscedastic errors corresponding to the entire ensemble

**Usage**

```
get.matrix.hetero.inv(weight.hetero, nMO)
```

**Arguments**

`weight.hetero` output of [get.vec.weight.hetero](#)  
`nMO` number of possible simulation chains (missing and non-missing)

**Value**

inverse matrix n x n of weights where coden is the total number of predictions (all the predictions for all the possible simulation chains)

**Author(s)**

Guillaume Evin

---

get.matrix.KMS	<i>get.matrix.KMS Return the square Kac-Murdoch-Szego matrix for a rho correlation and n lines/columns</i>
----------------	--

---

**Description**

get.matrix.KMS Return the square Kac-Murdoch-Szego matrix for a rho correlation and n lines/columns

**Usage**

```
get.matrix.KMS(n, rho)
```

**Arguments**

n	number of lines/columns of the square matrix
rho	correlation parameter in [0,1]

**Value**

n x n Kac-Murdock-Szego matrix

**Author(s)**

Guillaume Evin

**References**

Kac, M., W. L. Murdock, and G. Szego. 1953. 'On the Eigen-Values of Certain Hermitian Forms' Journal of Rational Mechanics and Analysis 2: 767-800.

---

get.matrix.KMSinv	<i>get.matrix.KMSinv return the inverse of the square Kac-Murdock-Szego matrix for a rho correlation and n lines/columns</i>
-------------------	--

---

**Description**

get.matrix.KMSinv return the inverse of the square Kac-Murdock-Szego matrix for a rho correlation and n lines/columns

**Usage**

```
get.matrix.KMSinv(n, rho)
```

**Arguments**

n	number of lines/columns of the square matrix
rho	correlation parameter in (-1,1)

**Value**

n x n Kac-Murdock-Szego matrix

**Author(s)**

Guillaume Evin

**References**

Kac, M., W. L. Murdock, and G. Szego. 1953. 'On the Eigen-Values of Certain Hermitian Forms' Journal of Rational Mechanics and Analysis 2: 767-800.

---

get.matrix.W	<i>get.matrix.W return the matrix of <math>W = V \times C \times V</math> for the treatment of heteroscedastic and AR(1) errors see Wang (2011) section 5.3 for further details</i>
--------------	---

---

**Description**

get.matrix.W return the matrix of  $W = V \times C \times V$  for the treatment of heteroscedastic and AR(1) errors see Wang (2011) section 5.3 for further details

**Usage**

```
get.matrix.W(weight.hetero, nMO, nP, rho)
```

**Arguments**

weight.hetero	output of <a href="#">get.vec.weight.hetero</a>
nMO	number of possible simulation chains (missing and non-missing)
nP	number of continuous predictors (e.g. future times)
rho	AR(1) correlation parameter in (-1,1)

**Value**

matrix n x n where coden is the total number of predictions (all the predictions for all the possible simulation chains)

**Author(s)**

Guillaume Evin

**References**

Wang, Y. 2011. 'Spline Smoothing with Heteroscedastic and/or Correlated Errors.' Smoothing Splines. Chapman and Hall/CRC. <https://doi.org/10.1201/b10954-11>.

---

get.matrix.Winv	<i>get.matrix.Winv return the inverse matrix of <math>W = V \times C \times V</math> for the treatment of heteroscedastic and AR(1) errors see Wang (2011) section 5.3 for further details</i>
-----------------	--

---

### Description

get.matrix.Winv return the inverse matrix of  $W = V \times C \times V$  for the treatment of heteroscedastic and AR(1) errors see Wang (2011) section 5.3 for further details

### Usage

```
get.matrix.Winv(weight.hetero, nMO, nP, rho)
```

### Arguments

weight.hetero	output of <a href="#">get.vec.weight.hetero</a>
nMO	number of possible simulation chains (missing and non-missing)
nP	number of continuous predictors (e.g. future times)
rho	AR(1) correlation parameter in (-1,1)

### Value

inverse matrix  $n \times n$  of weights where coden is the total number of predictions (all the predictions for all the possible simulation chains)

### Author(s)

Guillaume Evin

### References

Wang, Y. 2011. 'Spline Smoothing with Heteroscedastic and/or Correlated Errors' Smoothing Splines. Chapman and Hall/CRC. <https://doi.org/10.1201/b10954-11>.

---

get.spectral.decomp	<i>get.spectral.decomp</i>
---------------------	----------------------------

---

### Description

compute different objects used for the application of Smoothing-Splines ANOVA (SS-ANOVA)

### Usage

```
get.spectral.decomp(SIGMA)
```

**Arguments**

SIGMA            reproducing kernel

**Value**

list with the following fields:

- **Q**: Matrix of eigen vectors  $n \times r$ ,
- **D**: Vector of nonzero eigen values (size  $r$ ),
- **r**: Number of nonzero eigen values (scalar).

**Author(s)**

Guillaume Evin

---

`get.target.logdensity.rho`

*get.target.density.rho* Return the log-density of the full conditional distribution for the parameter *rho*

---

**Description**

`get.target.density.rho` Return the log-density of the full conditional distribution for the parameter `rho`

**Usage**

`get.target.logdensity.rho(nFull, deltaRV, distSS, weight.hetero, nMO, nP, rho)`

**Arguments**

`nFull`             $nP \times nMO$   
`deltaRV`        variance of the residual terms for the max value of the continuous predictor  
`distSS`        sum of square distances between the climate change responses and the ANOVA model  
`weight.hetero` output of [get.vec.weight.hetero](#)  
`nMO`            number of possible simulation chains (missing and non-missing)  
`nP`             number of continuous predictors (e.g. future times)  
`rho`            AR(1) correlation parameter in (-1,1)

**Value**

log-density of the full conditional distribution

**Author(s)**

Guillaume Evin

---

`get.vec.weight.hetero` *get.vec.weight.hetero* returns the vector of weights for the computation of heteroscedastic errors corresponding to one simulation chain

---

### Description

`get.vec.weight.hetero` returns the vector of weights for the computation of heteroscedastic errors corresponding to one simulation chain

### Usage

```
get.vec.weight.hetero(nP, type.weight.hetero)
```

### Arguments

`nP` length of the continuous predictor for which we want to obtain the prediction (e.g. time) we suppose that continuous predictor is regularly spaced (e.g. 1990,2000,2010,...)

`type.weight.hetero`  
"constant" (homoscedastic) or "linear" (heteroscedastic)

### Value

vector of square roots of weights of the same length than `predContUnique`

### Author(s)

Guillaume Evin

---

`get.yMCMC` *get.yMCMC*

---

### Description

Get matrix `nMCMC` x `nFull` of climate responses where `nMCMC` is the number of MCMC draws and `nFull` is the number of possible combinations of predictors (discrete AND continuous),

### Usage

```
get.yMCMC(lOpt, lDim, lScen, change.variable)
```

**Arguments**

lOpt	list of options, returned by <a href="#">QUALYPSOSS.check.option</a>
lDim	list of dimensions
lScen	list of scenario characteristics, output from <a href="#">QUALYPSOSS.process.scenario</a>
change.variable	output from <a href="#">compute.change.variable</a> containing MCMC draws of climate change response

**Value**

strongyMCMC: matrix nMCMC x nFull of climate responses

**Author(s)**

Guillaume Evin

---

plotQUALYPSOSSClimateChangeResponse

*plotQUALYPSOSSClimateChangeResponse*

---

**Description**

Plot climate change responses.

**Usage**

```
plotQUALYPSOSSClimateChangeResponse(
  QUALYPSOSSOUT,
  lim = NULL,
  col = NULL,
  xlab = "Years",
  ylab = expression(phi^{    star })),
  ...
)
```

**Arguments**

QUALYPSOSSOUT	output from <a href="#">QUALYPSOSS</a>
lim	y-axis limits (default is NULL)
col	color for the lines
xlab	x-axis label
ylab	y-axis label
...	additional arguments to be passed to <a href="#">plot</a>

**Author(s)**

Guillaume Evin

---

```
plotQUALYPSOSSClimateResponse
      plotQUALYPSOSSClimateResponse
```

---

### Description

Plot climate responses.

### Usage

```
plotQUALYPSOSSClimateResponse(
  QUALYPSOSSOUT,
  lim = NULL,
  col = NULL,
  xlab = "Years",
  ylab = expression(phi),
  ...
)
```

### Arguments

QUALYPSOSSOUT	output from <a href="#">QUALYPSOSS</a>
lim	y-axis limits (default is NULL)
col	color for the lines
xlab	x-axis label
ylab	y-axis label
...	additional arguments to be passed to <a href="#">plot</a>

### Author(s)

Guillaume Evin

---

```
plotQUALYPSOSSeffect  plotQUALYPSOSSeffect
```

---

### Description

Plot prediction of ANOVA effects for one main effect. By default, we plot we plot the credible intervals corresponding to a probability 0.95.



**Usage**

```
plotQUALYPSOSSeffect(  
  QUALYPSOSSOUT,  
  iEff,  
  CIlevel = c(0.025, 0.975),  
  lim = NULL,  
  col = 1:20,  
  xlab = "Continuous predictor",  
  ylab = "Effect",  
  addLegend = TRUE,  
  ...  
)
```

**Arguments**

QUALYPSOSSOUT	output from <a href="#">QUALYPSOSS</a>
iEff	index of the main effect to be plotted in QUALYPSOSSOUT\$listScenario\$predDiscreteUnique
CIlevel	probabilities for the credible intervals, default is equal to c(0.025, 0.975)
lim	y-axis limits (default is NULL)
col	colors for each effect
xlab	x-axis label
ylab	y-axis label
addLegend	if TRUE, a legend is added
...	additional arguments to be passed to <a href="#">plot</a>

**Author(s)**

Guillaume Evin

---

plotQUALYPSOSSgrandmean

*plotQUALYPSOSSgrandmean*

---

**Description**

Plot prediction of grand mean ensemble. By default, we plot the credible interval corresponding to a probability 0.95.

**Usage**

```
plotQUALYPSOSSgrandmean(
  QUALYPSOSSOUT,
  CIlevel = c(0.025, 0.975),
  lim = NULL,
  col = "black",
  xlab = "Continuous predictor",
  ylab = "Grand mean",
  addLegend = T,
  ...
)
```

**Arguments**

QUALYPSOSSOUT	output from <a href="#">QUALYPSOSS</a>
CIlevel	probabilities for the credible intervals, default is equal to <code>c(0.025, 0.975)</code>
lim	y-axis limits (default is NULL)
col	color for the overall mean and the credible interval
xlab	x-axis label
ylab	y-axis label
addLegend	if TRUE, a legend is added
...	additional arguments to be passed to <a href="#">plot</a>

**Author(s)**

Guillaume Evin

---

plotQUALYPSOSSTotalVarianceDecomposition  
*plotQUALYPSOSSTotalVarianceDecomposition*

---

**Description**

Plot fraction of total variance explained by each source of uncertainty.

**Usage**

```
plotQUALYPSOSSTotalVarianceDecomposition(
  QUALYPSOSSOUT,
  col = c("orange", "yellow", "cadetblue1", "blue1", "darkgreen", "darkgoldenrod4",
    "darkorchid1"),
  xlab = "Continuous predictor",
  ylab = "% Total Variance",
  addLegend = TRUE,
  ...
)
```

**Arguments**

QUALYPSOSSOUT	output from <a href="#">QUALYPSOSS</a>
col	colors for each source of uncertainty, the first two colors corresponding to internal variability and residual variability, respectively
xlab	x-axis label
ylab	y-axis label
addLegend	if TRUE, a legend is added
...	additional arguments to be passed to <a href="#">plot</a>

**Author(s)**

Guillaume Evin

---

predGlobTemp	<i>Annual average of global temperatures simulated by different CMIP5 GCMs at the planetary scale for the period 1971-2099</i>
--------------	--

---

**Description**

Annual average of global temperatures simulated by different CMIP5 GCMs at the planetary scale for the period 1971-2099

**Usage**

```
data(predGlobTemp)
```

**Format**

matrix 129 years x 20 scenarios

**Author(s)**

Guillaume Evin <guillaume.evin@inrae.fr>

---

predGlobTempUnique      *Equally spaced vector of simulated global temperatures over the period 1971-2099 for the RCP8.5*

---

**Description**

Equally spaced vector of simulated global temperatures over the period 1971-2099 for the RCP8.5

**Usage**

```
data(predGlobTempUnique)
```

**Format**

vector of length 13

**Author(s)**

Guillaume Evin <guillaume.evin@inrae.fr>

---

predTime      *Years 1971-2099 repeated for the 20 scenarios*

---

**Description**

Years 1971-2099 repeated for the 20 scenarios

**Usage**

```
data(predTime)
```

**Format**

matrix 129 years x 20 scenarios

**Author(s)**

Guillaume Evin <guillaume.evin@inrae.fr>

---

predTimeUnique      *Equally spaced vector of years over the period 1971-2099*

---

**Description**

Equally spaced vector of years over the period 1971-2099

**Usage**

data(predTimeUnique)

**Format**

vector of length 13

**Author(s)**

Guillaume Evin <guillaume.evin@inrae.fr>

---

QUALYPSOSS      *QUALYPSOSS*

---

**Description**

QUALYPSOSS

**Usage**

```
QUALYPSOSS(  
  ClimateProjections,  
  scenAvail,  
  vecYears = NULL,  
  predCont = NULL,  
  predContUnique = NULL,  
  iCpredCont = NULL,  
  iCpredContUnique = NULL,  
  listOption = NULL,  
  RK = NULL  
)
```

**Arguments**

ClimateProjections	matrix $n_T \times n_S$ of climate projections where $n_T$ is the number of values for the continuous predictor (years, global temperature) and $n_S$ the number of scenarios.
scenAvail	matrix of scenario characteristics $n_S \times n_K$ where $n_K$ is the number of discrete predictors.
vecYears	(optional) vector of years of length $n_T$ (by default, a vector $1:n_T$ ).
predCont	(optional) matrix $n_T \times n_S$ of continuous predictors.
predContUnique	(optional) vector of length $n_P$ corresponding to the continuous predictor for which we want to obtain the prediction.
iCpredCont	(optional) index in $1:n_T$ indicating the reference period (reference period) for the computation of change variables.
iCpredContUnique	(optional) index in $1:n_P$ indicating the reference continuous predictor for the computation of change variables.
listOption	(optional) list of options <ul style="list-style-type: none"> <li>• <b>spar</b>: if <code>uniqueFit</code> is true, smoothing parameter passed to the function <a href="#">smooth.spline</a>.</li> <li>• <b>lambdaClimateResponse</b>: smoothing parameter <math>&gt; 0</math> for the extraction of the climate response.</li> <li>• <b>lambdaHyperParANOVA</b>: hyperparameter <math>b</math> for the <math>\lambda</math> parameter related to each predictor <math>g</math>.</li> <li>• <b>typeChangeVariable</b>: type of change variable: "abs" (absolute, value by default) or "rel" (relative).</li> <li>• <b>nBurn</b>: number of burn-in samples (default: 1000). If <code>nBurn</code> is too small, the convergence of MCMC chains might not be obtained.</li> <li>• <b>nKeep</b>: number of kept samples (default: 2000). If <code>nKeep</code> is too small, MCMC samples might not be represent correctly the posterior distributions of inferred parameters.</li> <li>• <b>quantileCompress</b>: vector of probabilities (in <math>[0,1]</math>) for which we compute the quantiles from the posterior distributions <code>quantileCompress = c(0.005, 0.025, 0.05, 0.5, 0.95, 0.975, 0.995)</code> by default.</li> <li>• <b>uniqueFit</b>: logical, if FALSE (default), climate responses are fitted using Bayesian smoothing splines, otherwise, if TRUE, a unique cubic smoothing spline is fitted for each run, using the function <a href="#">smooth.spline</a>.</li> <li>• <b>returnMCMC</b>: logical, if TRUE, the list MCMC contains MCMC chains.</li> <li>• <b>returnOnlyCR</b>: logical, if TRUE (default), only Climate Responses are fitted and returned.</li> <li>• <b>type.temporal.dep</b>: "iid" for independent errors or "AR1" (default) for autocorrelated errors.</li> <li>• <b>type.hetero</b>: "constant" for homoscedastic errors or "linear" (default) for heteroscedastic errors.</li> </ul>
RK	Reproducing kernels: list

**Value**

list with the following fields:

- **POINT**: list containing the mean estimate of different quantities: RESIDUALVAR (residual variability), INTERNALVAR (internal variability), GRANDMEAN (grand mean for all time steps), MAINEFFECT (list with one item per discrete predictor  $i$ , containing matrices  $n_T \times n_{Eff\ i}$ , where  $n_{Eff\ i}$  is the number of possible values for the discrete predictor  $i$ ). EFFECTVAR, uncertainty related to the different main effect, TOTVAR Total variability, DECOMPVAR, decomposition of the total variability (percentages) for the different components, CONTRIB\_EACH\_EFFECT, contribution of each individual effects (percentages) to the corr. effect uncertainty.
- **BAYES**: list containing quantiles of different estimated quantities, listed in **POINT**.
- **MCMC**: list containing the MCMC chains (not returned by default).
- **climateResponse**: list containing different objects related to the extraction of the climate response.  $\phiStar$  ( $\phi^*$ ) is an array  $n_Q \times n_S \times n_P$  containing climate change responses, where  $n_Q$  is the number of returned quantiles,  $n_S$  is the number of scenarios and  $n_P$  is the length of `predContUnique` (e.g. number of future years). Similarly,  $\etaStar$  ( $\eta^*$ ) contains the deviation from the climate change response.  $\phi$  ( $\phi$ ) contains the climate responses and  $\eta$  ( $\eta$ ) contains the deviations from the climate responses.
- **listCR**: list containing objects created during the extraction of the climate responses
- **ClimateProjections**: argument of the call to the function, for records.
- **predCont**: (optional) argument of the call to the function, for records.
- **predContUnique**: (optional) argument of the call to the function, for records.
- **predDiscreteUnique**: list of possible values taken by the discrete predictors given in `scenAvail`.
- **listOption**: list of options
- **listScenario**: list of scenario characteristics (obtained from `QUALYPSOSS.process.scenario`)
- **RK**: list containing the reproducing kernels

**Author(s)**

Guillaume Evin

**Examples**

```
#####
# SYNTHETIC SCENARIOS
#####
# create nS=3 fictive climate scenarios with 2 GCMs and 2 RCMs, for a period of nY=20 years
n=20
t=1:n/n

# GCM effects (sums to 0 for each t)
effGCM1 = t*2
effGCM2 = t*-2

# RCM effects (sums to 0 for each t)
effRCM1 = t*1
```

```

effRCM2 = t*-1

# These climate scenarios are a sum of effects and a random gaussian noise
scenGCM1RCM1 = effGCM1 + effRCM1 + rnorm(n=n,sd=0.5)
scenGCM1RCM2 = effGCM1 + effRCM2 + rnorm(n=n,sd=0.5)
scenGCM2RCM1 = effGCM2 + effRCM1 + rnorm(n=n,sd=0.5)
ClimateProjections = cbind(scenGCM1RCM1,scenGCM1RCM2,scenGCM2RCM1)

# Here, scenAvail indicates that the first scenario is obtained with the combination of the
# GCM "GCM1" and RCM "RCM1", the second scenario is obtained with the combination of
# the GCM "GCM1" and RCM "RCM2" and the third scenario is obtained with the combination
# of the GCM "GCM2" and RCM "RCM1".
scenAvail = data.frame(GCM=c('GCM1','GCM1','GCM2'),RCM=c('RCM1','RCM2','RCM1'))

listOption = list(nBurn=20,nKeep=30,type.temporal.dep="iid",type.hetero="constant")
QUALYPSOSSOUT = QUALYPSOSS(ClimateProjections=ClimateProjections,scenAvail=scenAvail,
listOption=listOption)

# QUALYPSOSSOUT output contains many different information about climate projections uncertainties,
# which can be plotted using the following functions.

# plotQUALYPSOSSClimateResponse draws the climate responses, for all simulation chains,
# in comparison to the raw climate responses.
plotQUALYPSOSSClimateResponse(QUALYPSOSSOUT)

# plotQUALYPSOSSClimateChangeResponse draws the climate change responses, for all simulation chains.
plotQUALYPSOSSClimateChangeResponse(QUALYPSOSSOUT)

# plotQUALYPSOSSeffect draws the estimated effects, for a discrete predictor specified by iEff,
# as a function of the continuous predictor.
plotQUALYPSOSSeffect(QUALYPSOSSOUT, iEff = 1)
plotQUALYPSOSSeffect(QUALYPSOSSOUT, iEff = 2)

# plotQUALYPSOSSgrandmean draws the estimated grand mean, as a function of the continuous predictor.
plotQUALYPSOSSgrandmean(QUALYPSOSSOUT)

# plotQUALYPSOSSTotalVarianceDecomposition draws the decomposition of the total variance responses,
# as a function of the continuous predictor.
plotQUALYPSOSSTotalVarianceDecomposition(QUALYPSOSSOUT)

```

---

QUALYPSOSS.ANOVA.step1

*QUALYPSOSS.ANOVA.step1*

---

## Description

SSANOVA decomposition of the ensemble of climate change responses using a Bayesian approach. The different fields of the returned list contain  $n$  samples from the posterior distributions of the different inferred quantities. In this first step, the residual errors are assumed iid



**Usage**

```
QUALYPSOSS.ANOVA.step1(lOpt, lDim, yMCMC, RK)
```

**Arguments**

<code>lOpt</code>	list of options, returned by <a href="#">QUALYPSOSS.check.option</a>
<code>lDim</code>	list of dimensions
<code>yMCMC</code>	array nMCMC x nFull of climate change responses
<code>RK</code>	large object containing the reproducing kernels, returned by <a href="#">QUALYPSOSS.get.RK</a>

**Value**

list containing diverse information aboutwith the following fields:

- **g.MCMC**: Smooth effects `g`: array  $n \times nFull \times K$  where `nFull` is the number of possible combinations of predictors (discrete AND continuous),
- **nu.MCMC**: Smooth effects `nu`, a list with matrices of eigen vectors
- **lambda.MCMC**: Smoothing parameters: matrix  $n \times K$ ,
- **deltaRV.MCMC**: Residual variance: vector of length `n`,
- **g.hat**: Smooth effects estimates: matrix  $nFull \times K$  where
- **nu.hat**: Smooth effects estimates: a list with estimates of eigen vectors,
- **lambda.hat**: Smoothing parameters estimates: vector of length `K`,
- **deltaRV.hat**: Residual variance estimate.
- **logLK**: vector of log-likelihood values of the draws
- **logPost**: vector of log-posterior values of the draws
- **Schwarz**: Schwarz criteria
- **BIC**: BIC criteria

**Author(s)**

Guillaume Evin

---

QUALYPSOSS.ANOVA.step2

*QUALYPSOSS.ANOVA.step2*

---

**Description**

SSANOVA decomposition of the ensemble of climate change responses using a Bayesian approach. In this second step, we infer `deltaRV` (variance of the residual errors) and `phi` (autocorrelation lag-1) considering hetero-autocorrelated residual errors, conditionally to smooth effects inferred in [QUALYPSOSS.ANOVA.step1](#)

**Usage**

```
QUALYPSOSS.ANOVA.step2(lOpt, lDim, yMCMC, gSum.step1, deltaRV.step1)
```

**Arguments**

<code>lOpt</code>	list of options, returned by <a href="#">QUALYPSOSS.check.option</a>
<code>lDim</code>	list of dimensions
<code>yMCMC</code>	array nMCMC x nFull of climate change responses
<code>gSum.step1</code>	sum of smooth effect estimates provided by <a href="#">QUALYPSOSS.ANOVA.step1</a>
<code>deltaRV.step1</code>	residual variance estimate provided by <a href="#">QUALYPSOSS.ANOVA.step1</a>

**Value**

list containing diverse information aboutwith the following fields:

- **rho.MCMC**: autocorrelation parameter of the AR(1) process: vector of length n
- **deltaRV.MCMC**: Residual variance: vector of length n,
- **rho.hat**: autocorrelation parameter estimate of the AR(1) process,
- **deltaRV.hat**: Residual variance estimate.

**Author(s)**

Guillaume Evin

---

QUALYPSOSS.ANOVA.step3

*QUALYPSOSS.ANOVA.step3*

---

**Description**

SSANOVA decomposition of the ensemble of climate change responses using a Bayesian approach. In this second step, we infer deltaRV (variance of the residual errors) and phi (autocorrelation lag-1) considering hetero-autocorrelated residual errors, conditionally to smooth effects inferred in [QUALYPSOSS.ANOVA.step1](#)

**Usage**

```
QUALYPSOSS.ANOVA.step3(
  lOpt,
  lDim,
  yMCMC,
  RK,
  g.step1,
  lambda.step1,
  rho.step2,
  deltaRV.step2
)
```

**Arguments**

lOpt	list of options, returned by <a href="#">QUALYPSOSS.check.option</a>
lDim	list of dimensions
yMCMC	array nMCMC x nFull of climate change responses
RK	large object containing the reproducing kernels, returned by <a href="#">QUALYPSOSS.get.RK</a>
g.step1	smooth effect estimates provided by <a href="#">QUALYPSOSS.ANOVA.step1</a>
lambda.step1	smooth parameter estimates provided by <a href="#">QUALYPSOSS.ANOVA.step1</a>
rho.step2	lag-1 autocorrelation estimate provided by <a href="#">QUALYPSOSS.ANOVA.step2</a>
deltaRV.step2	residual variance estimate provided by <a href="#">QUALYPSOSS.ANOVA.step2</a>

**Value**

list containing diverse information aboutwith the following fields:

- **g.MCMC**: Smooth effects g: array n x nFull x K where nFull is the number of possible combinations of predictors (discrete AND continuous),
- **g.hat**: Smooth effects estimates: matrix nFull x K where nFull is the number of possible combinations of predictors (discrete AND continuous),
- **Schwarz**: Schwarz criteria
- **BIC**: BIC criteria

**Author(s)**

Guillaume Evin

---

QUALYPSOSS.check.option

*QUALYPSOSS.check.option*

---

**Description**

Check if input options provided in [QUALYPSOSS](#) are valid and assigned default values if missing.

**Usage**

QUALYPSOSS.check.option(listOption)

**Arguments**

listOption      list of options

**Value**

List containing the complete set of options.

**Author(s)**

Guillaume Evin

---

QUALYPSOSS.get.RK      *QUALYPSOSS.get.RK*


---

**Description**

Get reproducing kernel for each discrete predictor

**Usage**

QUALYPSOSS.get.RK(X, nK)

**Arguments**

X	matrix of predictors
nK	number of discrete predictors

**Value**

strongRK: list containing the reproducing kernels, obtained using spectral decomposition

**Author(s)**

Guillaume Evin

---

QUALYPSOSS.process.scenario  
*QUALYPSOSS.process.scenario*


---

**Description**

compute different objects used for the application of Smoothing-Splines ANOVA (SS-ANOVA), these objects being processed outputs of the scenario characteristics

**Usage**

QUALYPSOSS.process.scenario(scenAvail, predContUnique)

**Arguments**

scenAvail	matrix of scenario characteristics nS x nK.
predContUnique	(optional) unique values of continuous predictors.

**Value**

list containing diverse information aboutwith the following fields:

- **scenAvail**: Record first argument of the function,
- **predContUnique**: Record second argument of the function,
- **XFull**: data.frame with all possible combinations of predictors (continuous AND discrete),
- **nFull**: number of rows of XFull,
- **nK**: Number of columns of ScenAvail (i.e. number of discrete predictors),
- **predDiscreteUnique**: List containing possible values for each discrete predictor.

**Author(s)**

Guillaume Evin

---

reproducing.kernel     *reproducing.kernel*

---

**Description**

see par 2.3 in Cheng and Speckman

**Usage**

```
reproducing.kernel(x, y = NULL, type, typeRK = "Cheng")
```

**Arguments**

x	vector of predictors (continuous or discrete)
y	vector of predictors (continuous or discrete)
type	'continuous' or 'discrete'
typeRK	type of reproducing kernels: c('Cheng','Gu','Gaussian')

**Value**

matrix n x n

**Author(s)**

Guillaume Evin

---

scenAvail	<i>scenAvail gives the GCM and RCM which have been used for the 20 climate projections</i>
-----------	--

---

**Description**

scenAvail gives the GCM and RCM which have been used for the 20 climate projections

**Usage**

```
data(scenAvail)
```

**Format**

data.frame with 20 rows and two columns: GCM and RCM

**Author(s)**

Guillaume Evin <guillaume.evin@inrae.fr>

---

vecYears	<i>vecYears gives the years corr. to Y, i.e. from 1971 to 2099</i>
----------	--

---

**Description**

vecYears gives the years corr. to Y, i.e. from 1971 to 2099

**Usage**

```
data(vecYears)
```

**Format**

vectors of length 129

**Author(s)**

Guillaume Evin <guillaume.evin@inrae.fr>

---

Y *climate projections of mean winter (DJF) temperature over the SREX region CEU simulated by 20 combinations of CMIP5 GCMs and RCMs for the period 1971-2099*

---

**Description**

climate projections of mean winter (DJF) temperature over the SREX region CEU simulated by 20 combinations of CMIP5 GCMs and RCMs for the period 1971-2099

**Usage**

data(Y)

**Format**

matrix 129 years x 20 scenarios

**Author(s)**

Guillaume Evin <guillaume.evin@inrae.fr>

**References**

Seneviratne, S. I. et al. Changes in Climate Extremes and their Impacts on the Natural Physical Environment, in: Managing the Risks of Extreme Events and Disasters to Advance Climate Change Adaptation: Special Report of the Intergovernmental Panel on Climate Change, edited by: Field, C., Barros, V., Stocker, T., and Dahe, Q., Cambridge University Press, Cambridge, 109-230, <https://doi.org/10.1017/CBO9781139177245.006>, 2012

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